



The Second Quantum Revolution and Sissa's Computer

Philippe Chomaz

Executive Scientific Director of the
Fundamental Research Department at
CEA-France





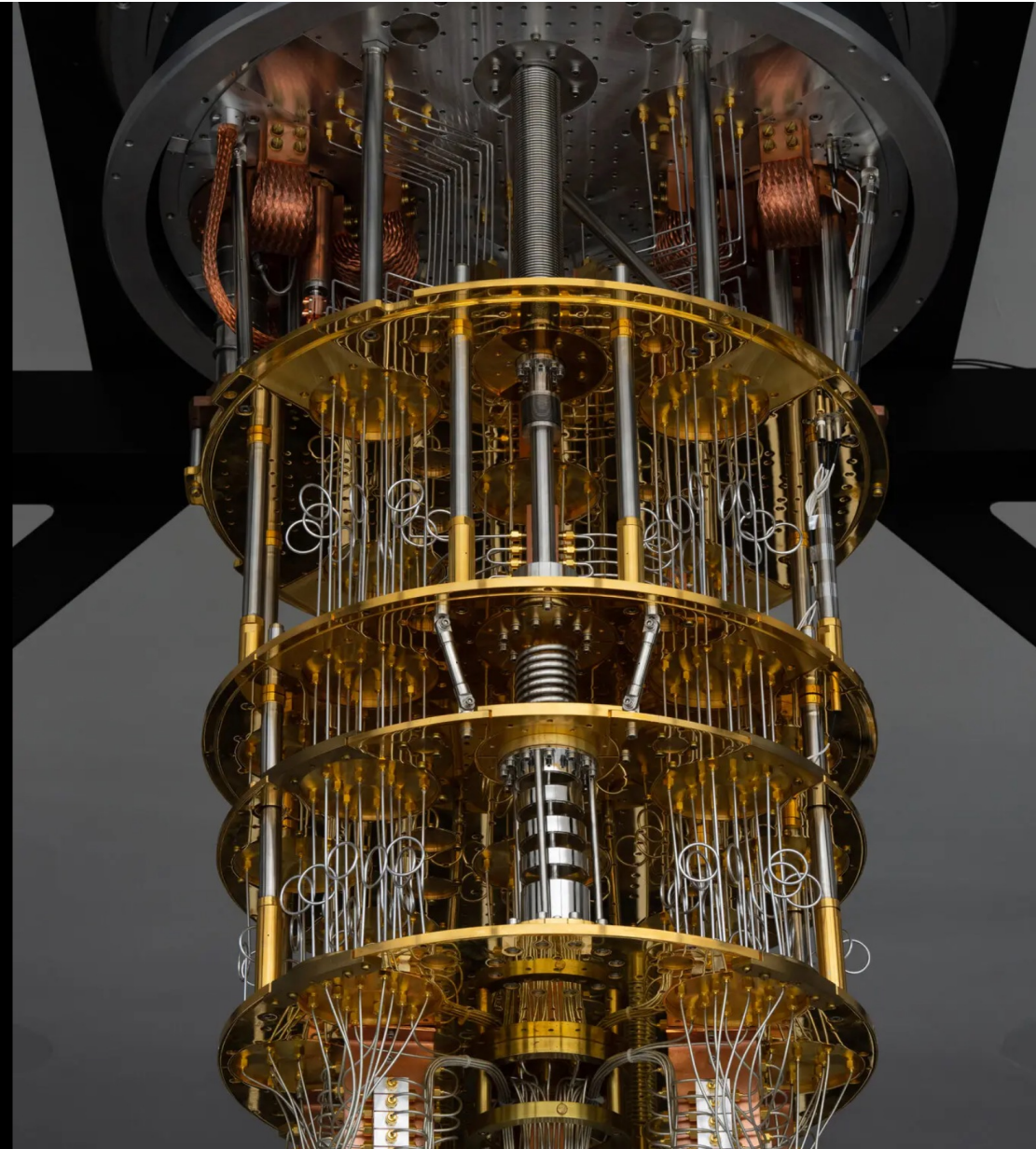
**Today Quantum
Dominates Headlines**



The New York Times

Quantum Computing Advance Begins New Era, IBM Says

A quantum computer came up with better answers to a physics problem than a conventional supercomputer.





The New York Times

Quantum Computing Advance Begins New Era, IBM Says

A quantum computer came up with better answers to a physics problem than a conventional supercomputer.



Le Monde

The New York Times

Se com...

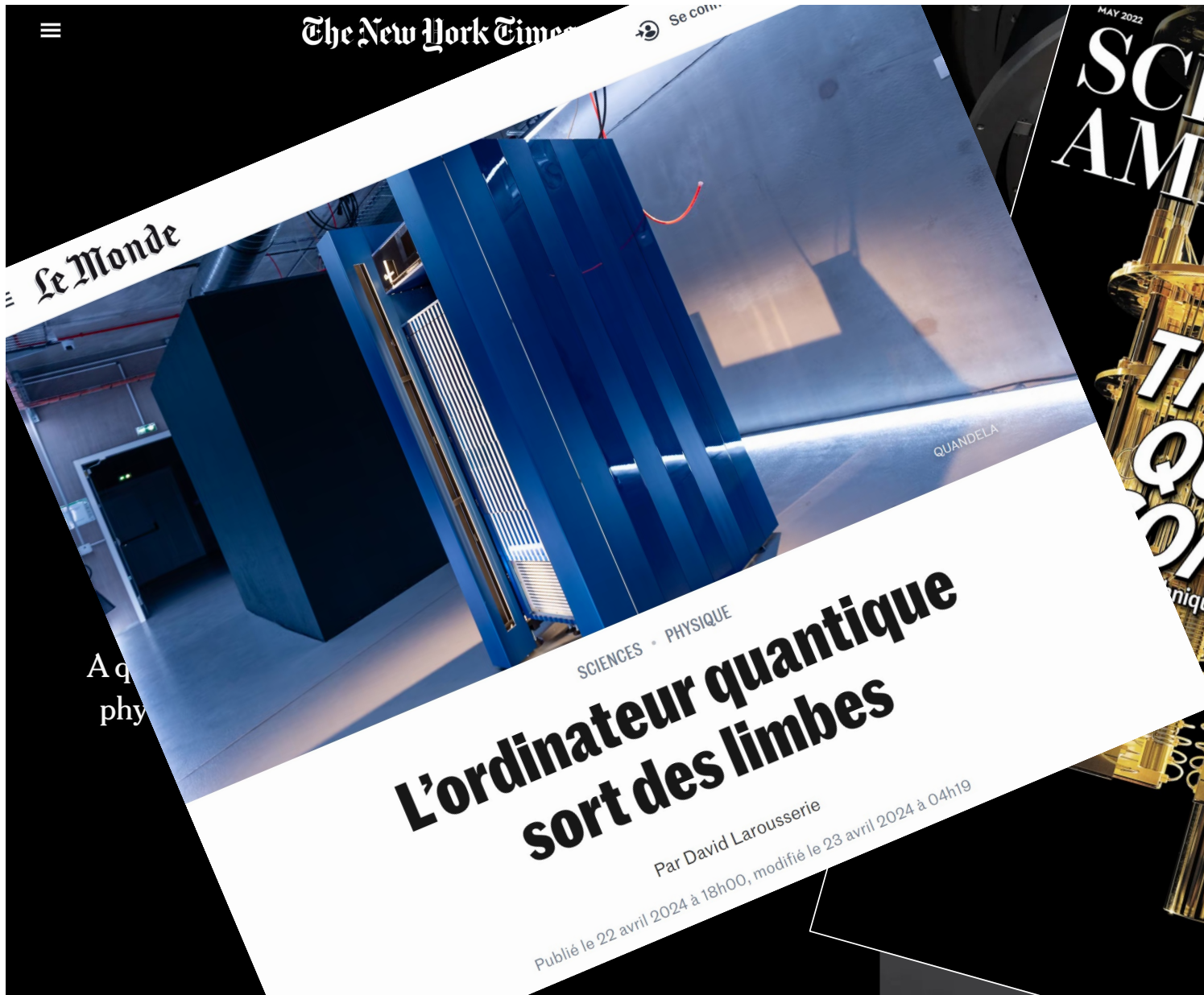
QUANDELA

SCIENCES • PHYSIQUE

L'ordinateur quantique sort des limbes

Par David Larousserie

Publié le 22 avril 2024 à 18h00, modifié le 23 avril 2024 à 04h19



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THE KEY TO QUANTUM COMPUTING

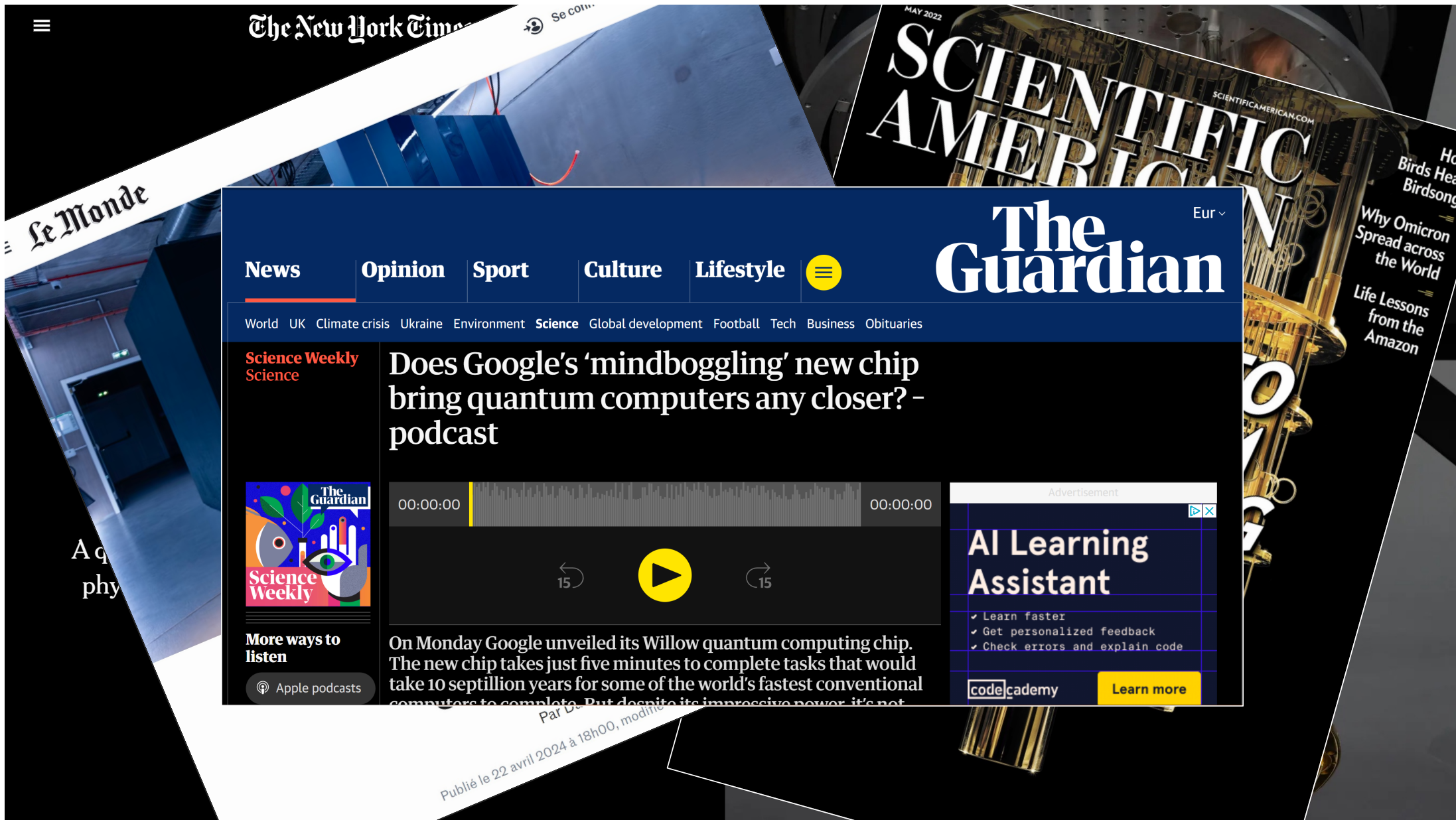
Techniques aim to fix physics errors fast

How Birds Hear Birdsong

Why Omicron Spread across the World

Life Lessons from the Amazon



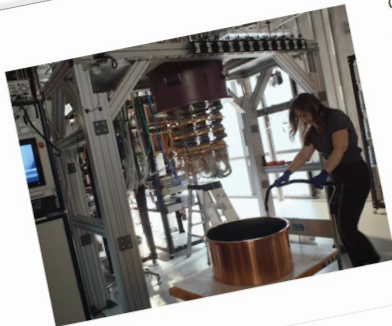








EL PAÍS

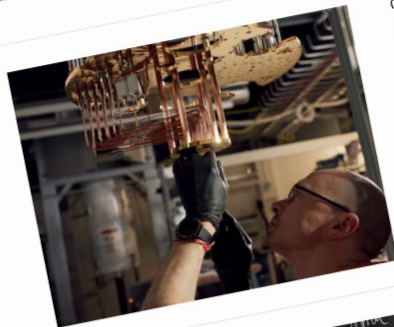


COMPUTACIÓN CUÁNTICA

Google presenta Willow, un chip cuántico que resuelve en 5 minutos una tarea que un superordenador tardaría cuatrillones de años

RAÚL LIMÓN | 09 DIC 2024 - 17:00 C.E.T.

La multinacional asegura que el procesador y la corrección de errores alcanzada anticipan el desarrollo de un ordenador a gran escala y tolerante a fallos



COMPUTACIÓN CUÁNTICA

Microsoft y Atom Computing anuncian un ordenador cuántico tras batir un récord de computación fiable

RAÚL LIMÓN | 30 NOV 2024 - 05:20 C.E.T.

Una investigación de las compañías proclama el entrelazamiento robusto de 24 cúbits lógicos que asegura un procesamiento mejor que con sistemas clásicos

FÍSICA CUÁNTICA

Un equipo chino logra el récord de entrelazamiento de los estados cuánticos del

TIME

Ein Meil
Von Stephan Finsterb

QUANTENCOMPUTER

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The Guardian

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SCIENCES • PHYSIQUE

Le Nobel de physique récompense le Français Alain Aspect, pionnier de la « seconde révolution quantique »

Le chercheur est distingué avec l'Américain John Clauser et l'Autrichien Anton Zeilinger pour la mise en évidence de l'intrication de particules, ouvrant la voie à des applications en information quantique.



News

World

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the Guardian

Eur

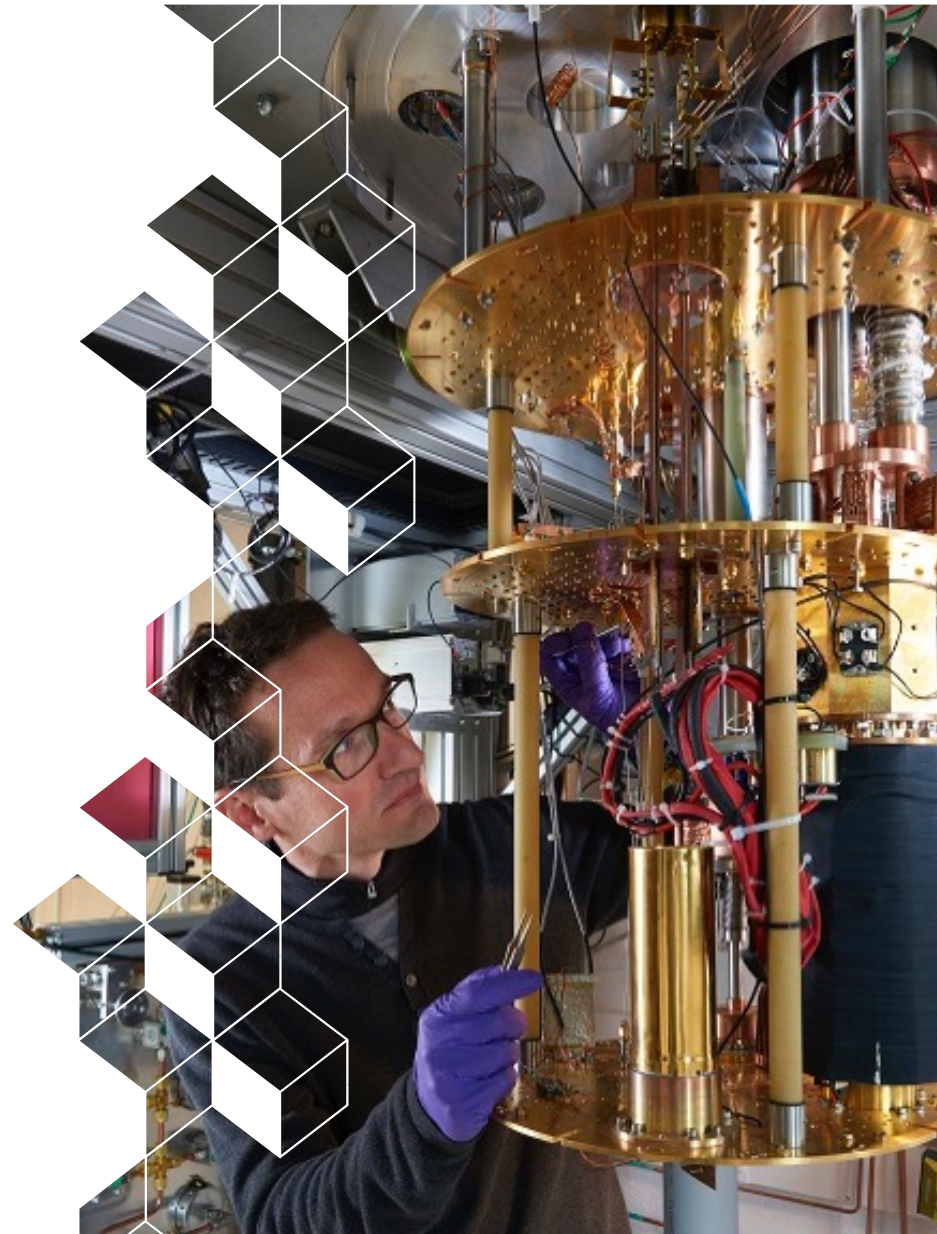
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**The incredible chance to
witness a major scientific
and technological revolution**

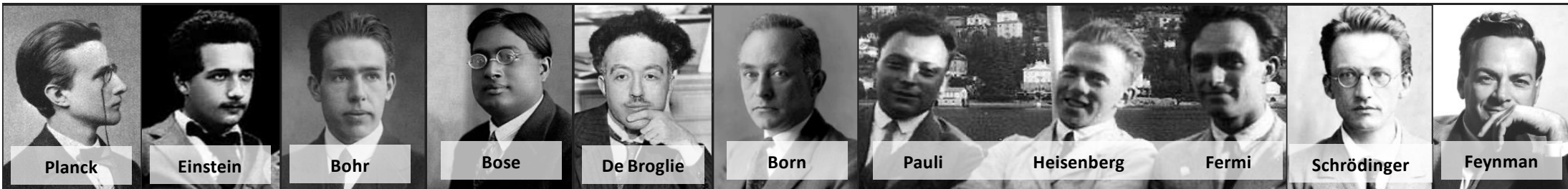
**The second quantum
revolution**



1.

**What is the first quantum revolution?
When was that?**

and by the way what means “quantum”?



Quantum is a Latin word meaning “elementary quantity”



Quantum is a Latin word meaning “elementary quantity”

Used by physicists in the early 20th century

When they discovered the revolutionary laws explaining matter, atoms, electrons, light, and their interactions, ...



$$[X, P] = i\hbar$$

$$\hat{H} = \frac{1}{2}(X^2 + P^2)$$

$$\hat{H}|\psi\rangle = E|\psi\rangle$$

$$a = \frac{1}{\sqrt{2}}(X + iP)$$

$$a^\dagger = \frac{1}{\sqrt{2}}(X - iP)$$

$$\hat{H} = a^\dagger a + \frac{1}{2}$$

$$\hat{H} = \frac{1}{2}(a^\dagger + a)^2$$

$$a^\dagger|\psi_n\rangle = \sqrt{n+1}|\psi_{n+1}\rangle$$

$$a|\psi_n\rangle = \sqrt{n}|\psi_{n-1}\rangle$$

$$a|\psi_0\rangle = 0$$

$$X|\psi_n\rangle = \sqrt{\frac{\hbar}{2m\omega}}\left[\sqrt{n+1}|\psi_{n+1}\rangle + \sqrt{n}|\psi_{n-1}\rangle\right]$$

$$P|\psi_n\rangle = \sqrt{\frac{\hbar m\omega}{2}}\left[\sqrt{n+1}|\psi_{n+1}\rangle - \sqrt{n}|\psi_{n-1}\rangle\right]$$

$$\langle f^{(n)}|\psi\rangle = (f^{(n)}|\psi\rangle) = \int_{-\infty}^{\infty} dx f^{(n)}(x)\psi(x)$$

$$E = \langle H \rangle = \langle U \rangle = \frac{1}{2}M\omega^2 A^2$$

$$\Delta p_x = \left(1 - \frac{v^2}{c^2}\right)^{1/2} \frac{\Delta p_x}{\Delta t} = \left(1 - \frac{v^2}{c^2}\right)^{1/2} \frac{\Delta p_x}{\Delta t}$$

$$\frac{dp_x}{dt} = \left(1 - \frac{v^2}{c^2}\right)^{1/2} \frac{dp_x}{dt}$$

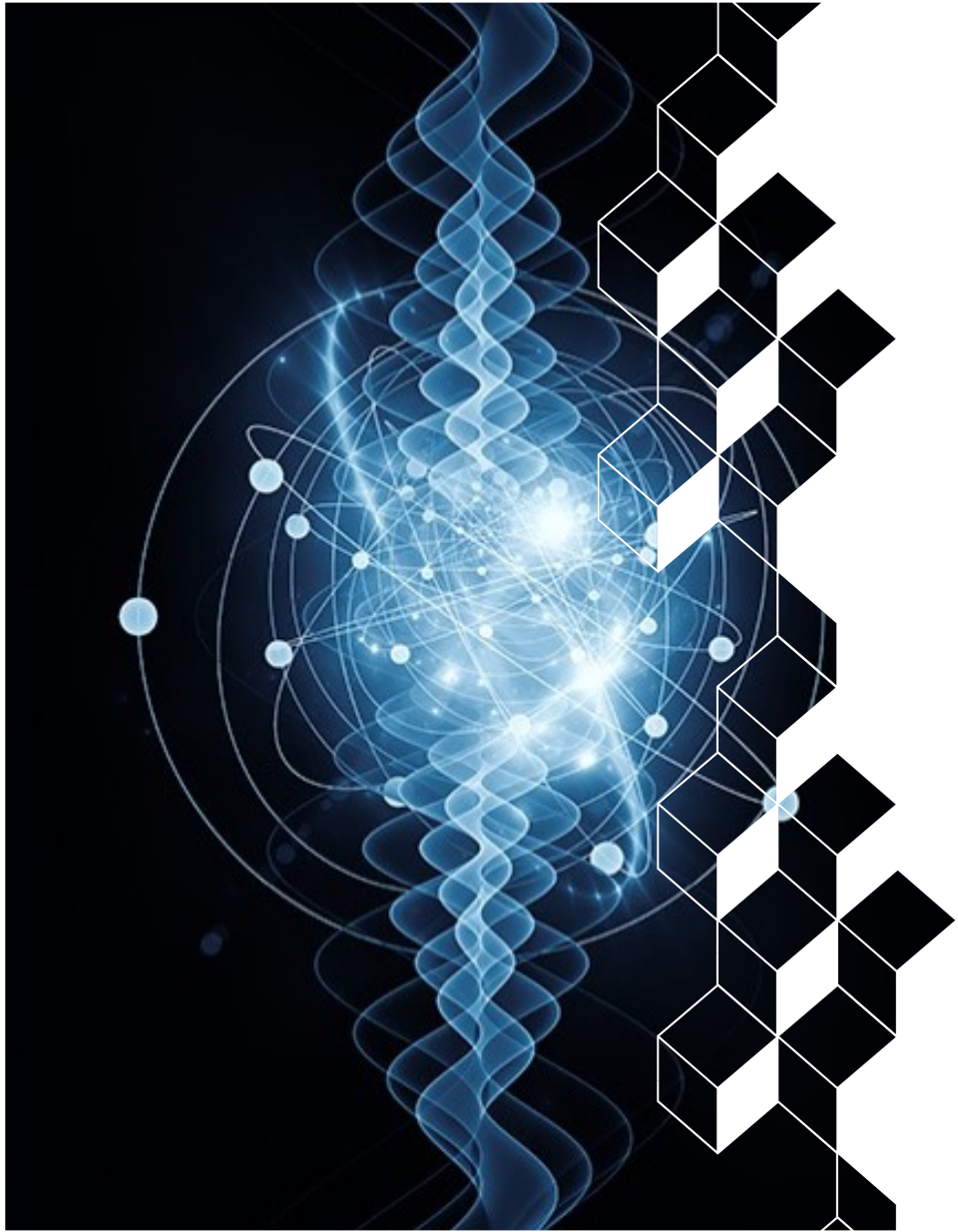
$$\frac{V}{c} = \frac{E}{E_T + M_T c^2}$$

Quantum is a Latin word meaning “**elementary quantity**”

Used by physicists in the early 20th century

When they discovered the revolutionary laws explaining matter, atoms, electrons, light, and their interactions, ...

Because in these laws quantities like energy and objects like light are quantized into elementary grains, called quanta.



A short story of the first Quantum Revolution

**At the end of the 19th century, physics was beautiful and seemed complete!
Everything was understood!...**



Newtonian mechanics and gravity



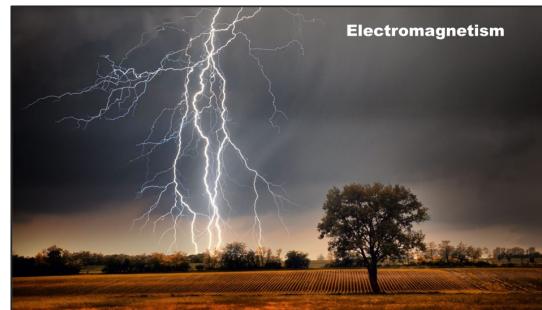
Electromagnetism



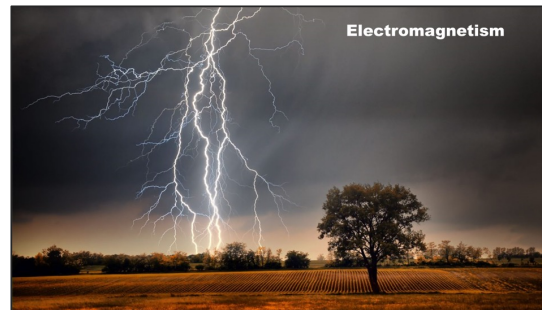
Thermodynamics



**At the end of the 19th century, physics was beautiful and seemed complete!
Everything was understood!...**



**At the end of the 19th century, physics was beautiful and seemed complete!
Everything was understood!...**



Or almost...

**At the end of the 19th century, physics was beautiful and seemed complete!
Everything was understood!...**



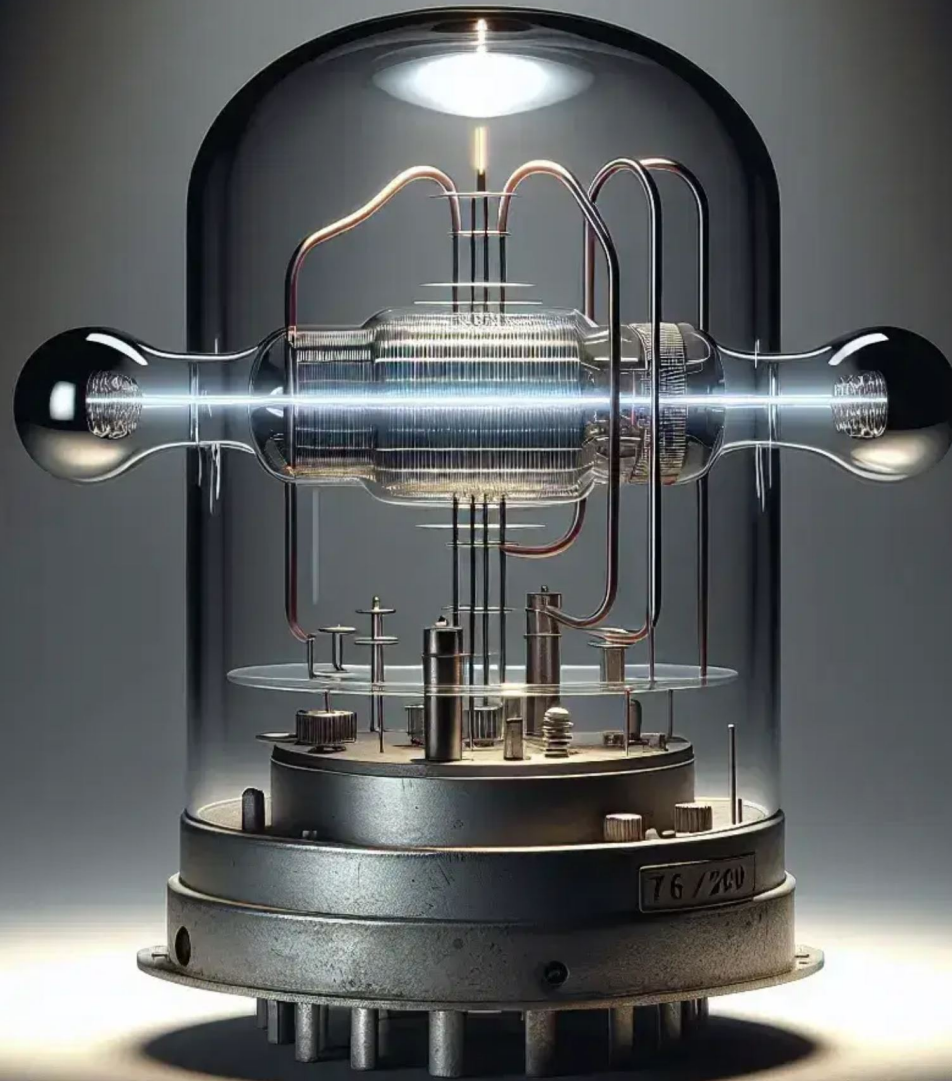
Or almost...

Only, minor issues between light and matter

Light from hot bodies



Electric current from light

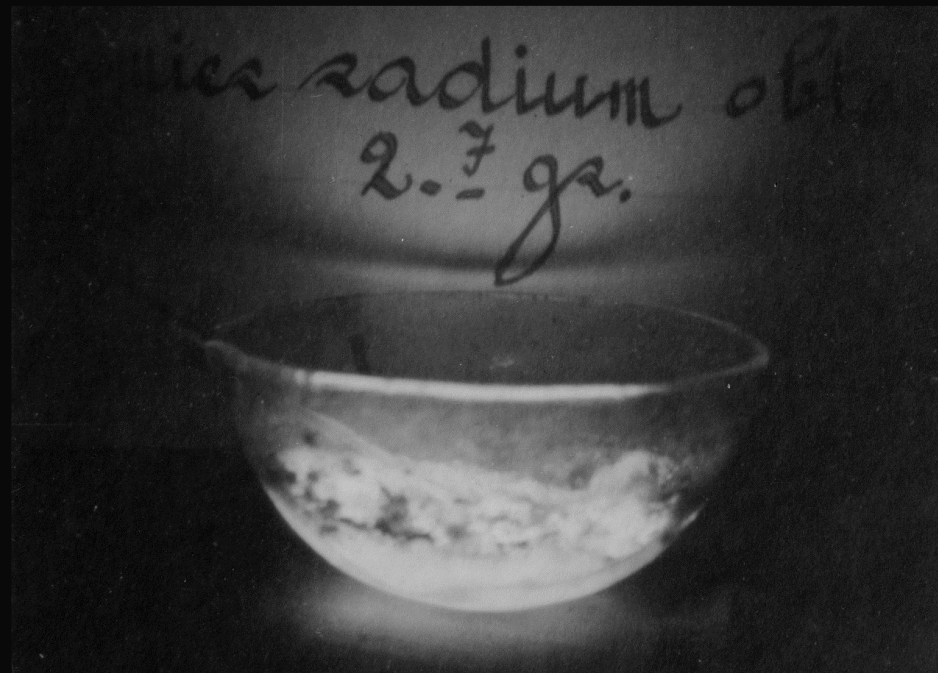


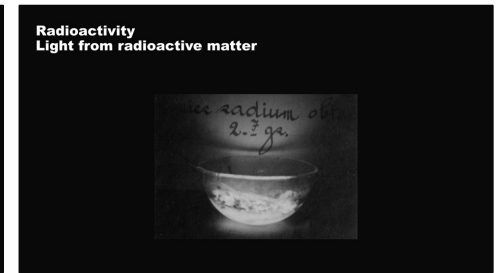
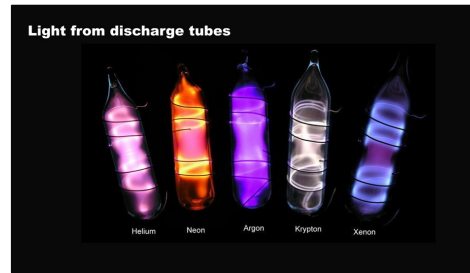
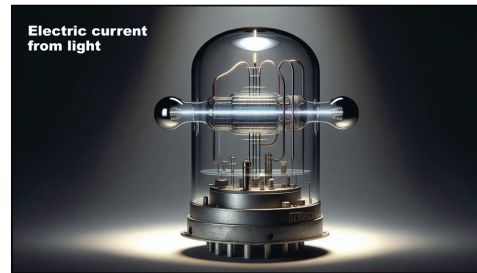
Light from discharge tubes



Radioactivity

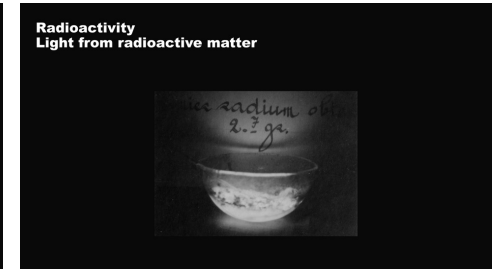
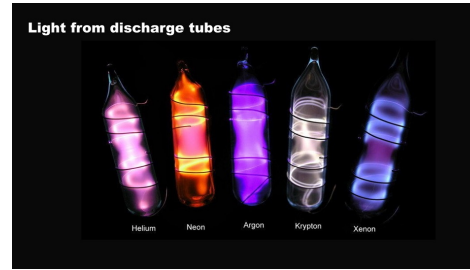
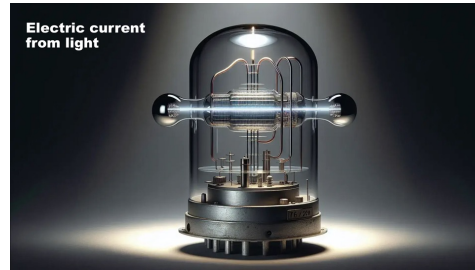
Light from radioactive matter





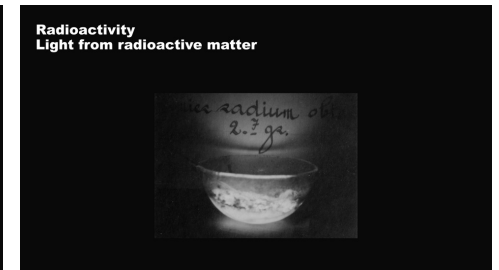
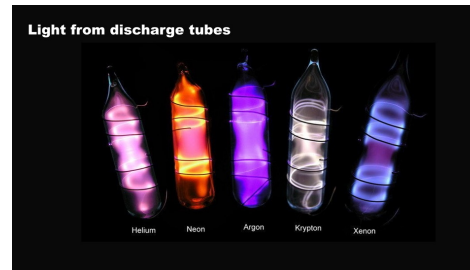
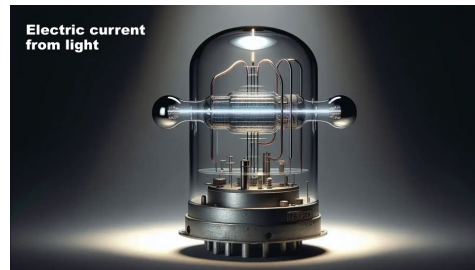
**At the end of the 19th century, physics was beautiful and seemed complete!
Everything was understood!...**

Except, minor issues between light and matter



Except, minor issues between light and matter
that led to the discovery of an entirely new physics
by the best physicist of the early 20th century





Light, ie electromagnetic wave, is quantized into elementary grains

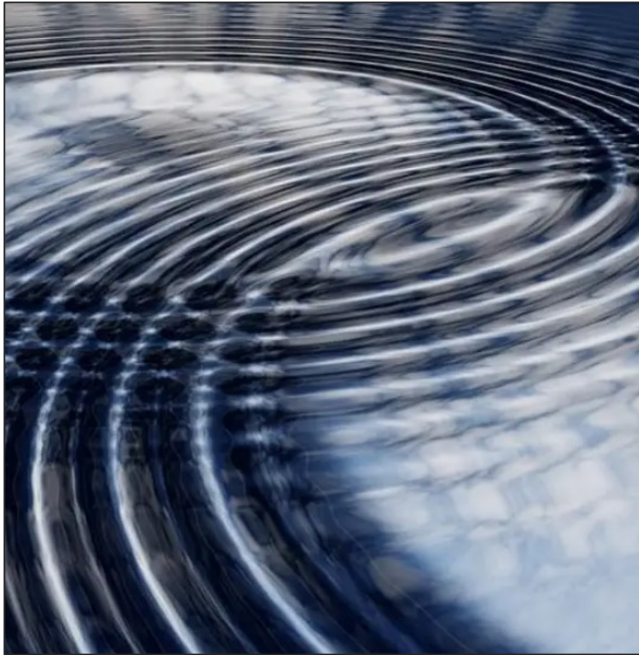
Matter, ie particles, behave like waves

Except, minor issues between light and matter
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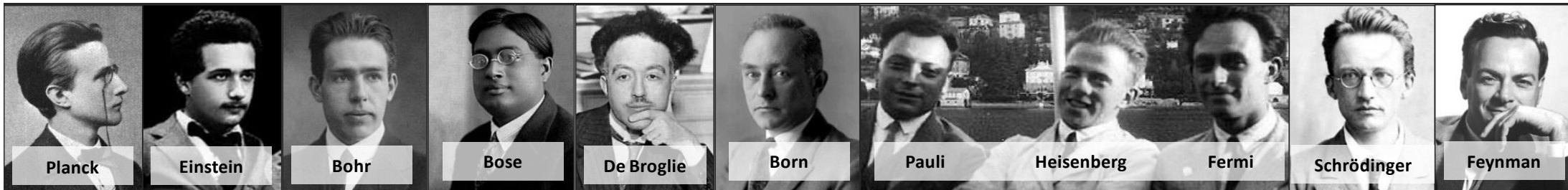


The first quantum scientific revolution

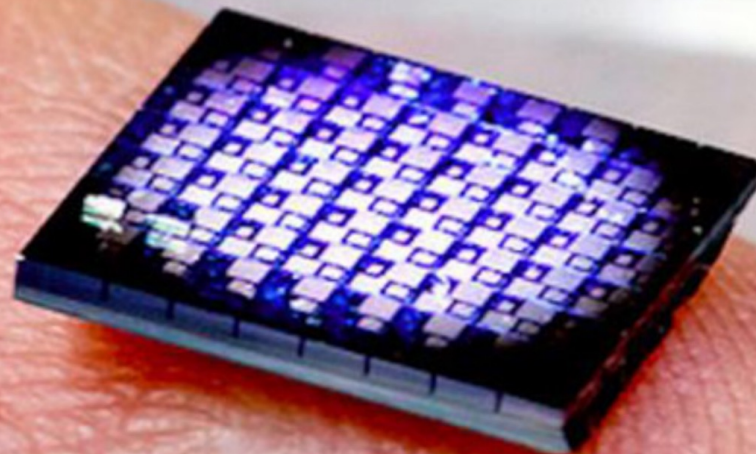


"Wave-particle duality"

**Matter, light, and their interactions
are made up of particles
described as superposition's of states
governed by wave mechanics**



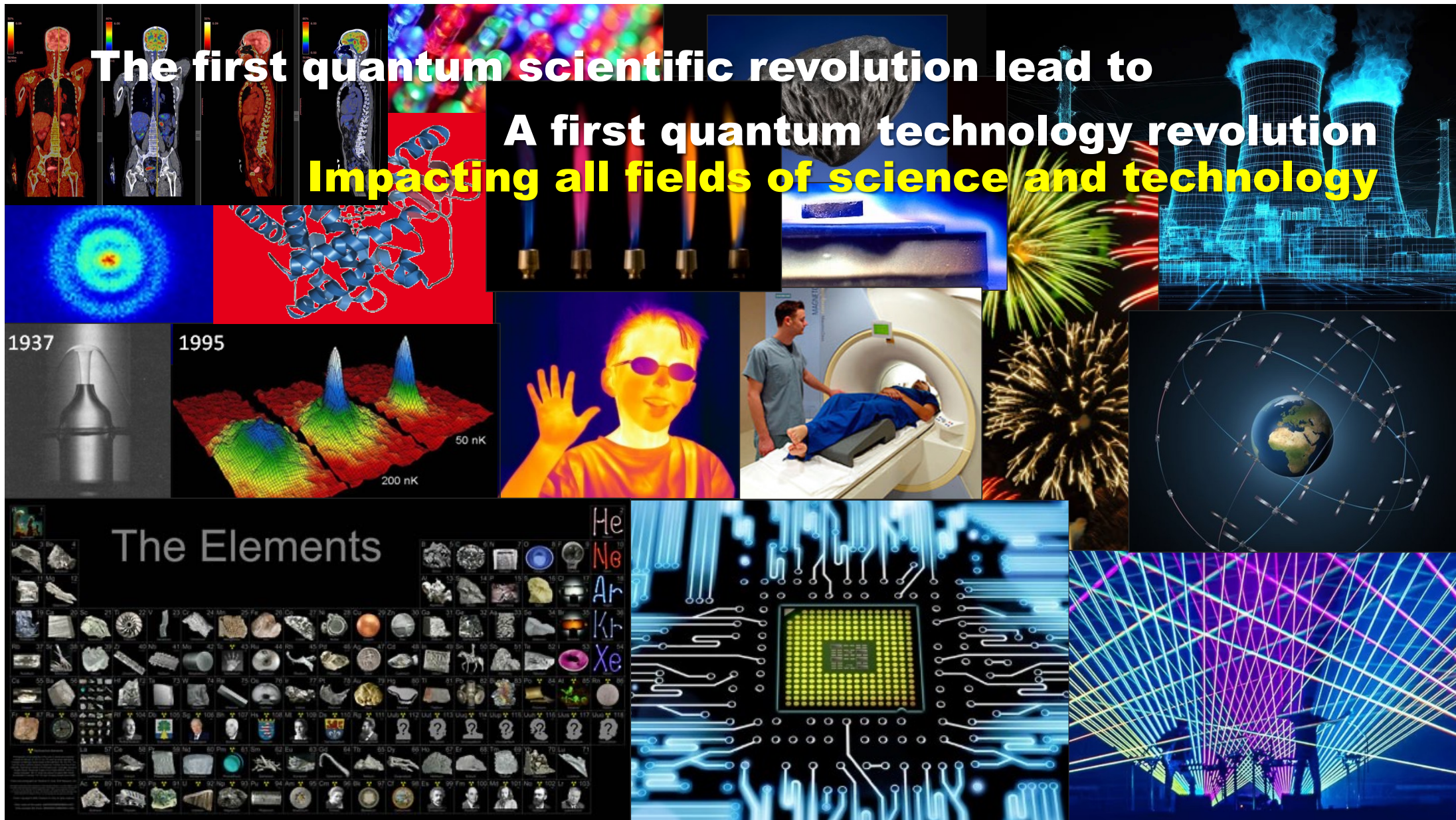
The first quantum scientific revolution lead to
A first quantum technology revolution



The first quantum scientific revolution lead to

A first quantum technology revolution

Impacting all fields of science and technology



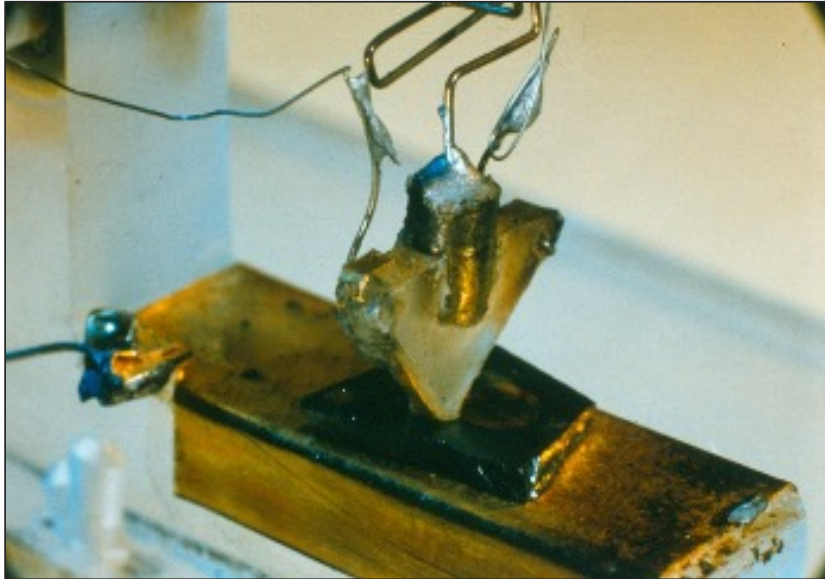


The first quantum scientific revolution lead to The first quantum technologies revolution Impacting all fields of science and technology

- **Physics**, Atomic and Molecular Physics, Solid-State Physics, Nuclear Physics, Statistical Physics, Quantum Optics,
- **Chemistry**, Spectroscopy, new materials, Photochemistry, Catalysis, simulation
- **Biology**, molecular Biology, photosynthesis, enzyme functions, protein folding
- **Medicine and Health**, Medical Imaging (MRI, PET), Radiotherapy, drug modeling
- **Electronics and Computing**, Transistors and Semiconductors, Information Technology, Logic Circuits
- **Energy Applications**, Nuclear Fission, Nuclear Fusion, Photovoltaic, batteries
- **Cryogenics** technologies, Superconductivity, Superfluidity
- **Telecommunications and Timing**, Lasers, Atomic Clocks,
- **Sensing and Imaging**, Magnetometers, LiDAR, Microscopy, Photonics, Radar



Quantum revolution of information treatment

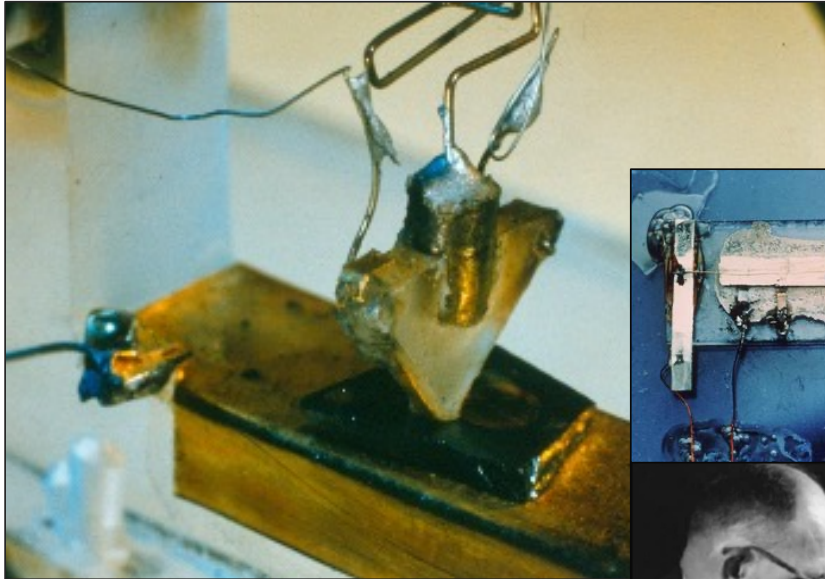


1947 First transistor @Bell-Lab

The first quantum switch controlling electrical signals

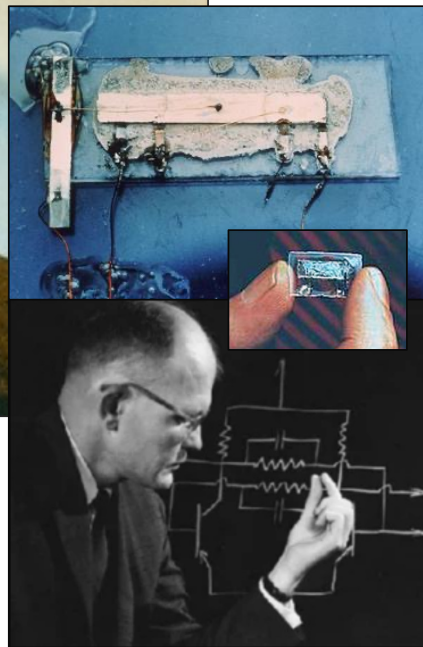


Quantum revolution of information treatment



1947 First transistor @Bell-Lab

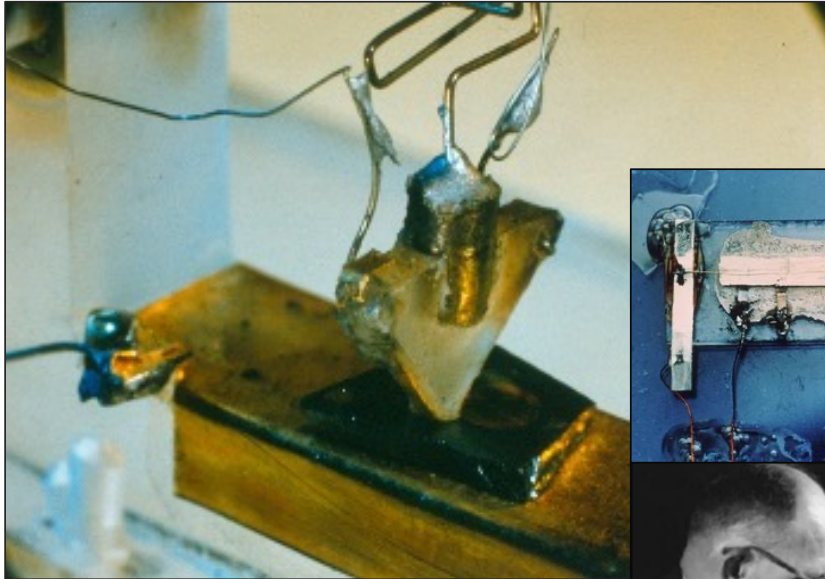
The first quantum switch controlling electrical signals



1959, First integrated circuit
@Texas Instruments

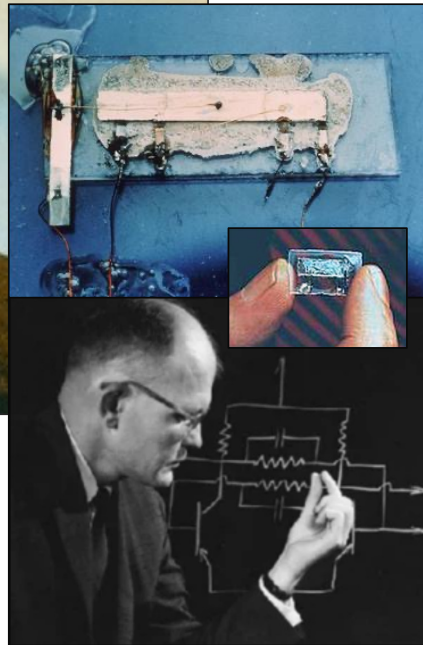


Quantum revolution of information treatment

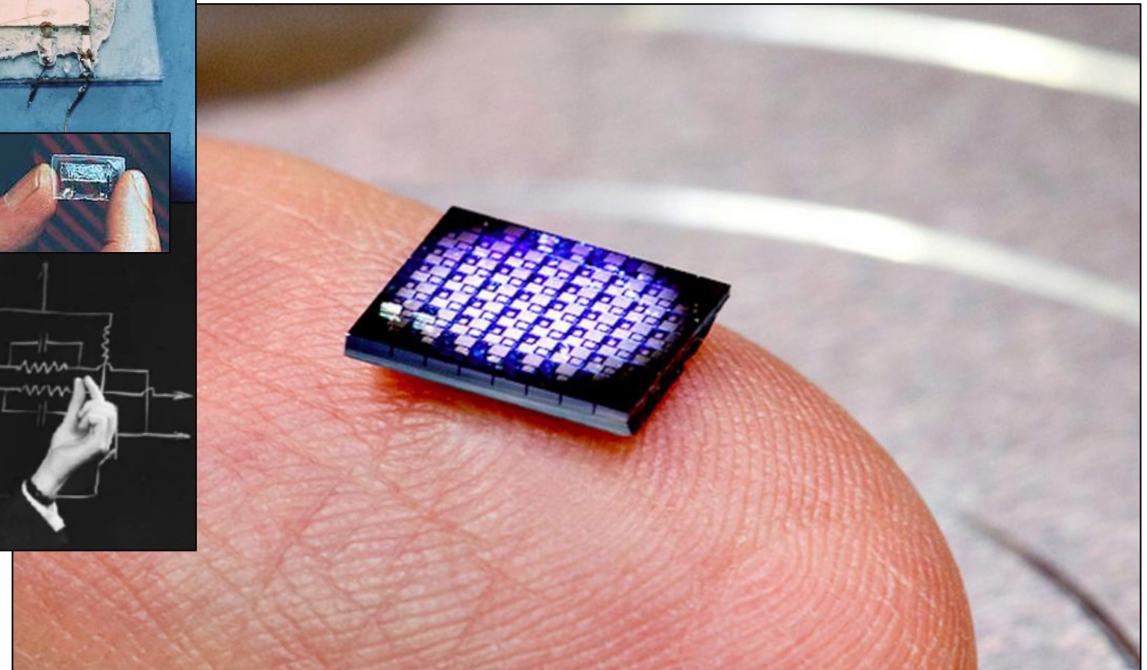


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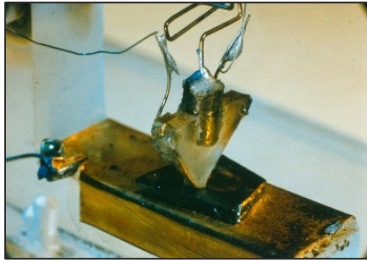


2021 First 2 nm chip with 50 billion transistors @IBM

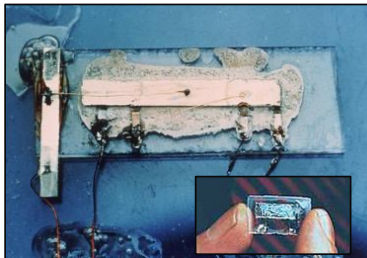


Quantum revolution of information treatment

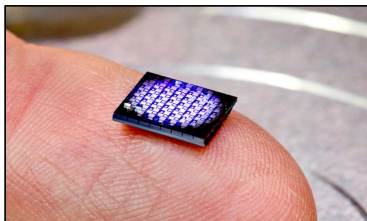
Transistors as quantum switch controlling electrical signals



1947 First transistor
@Bell-Lab



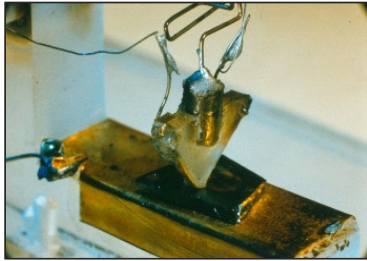
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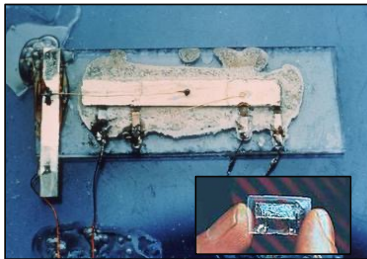
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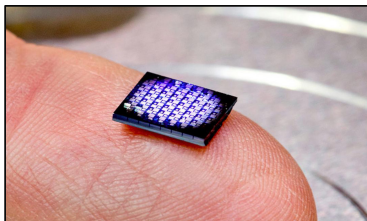
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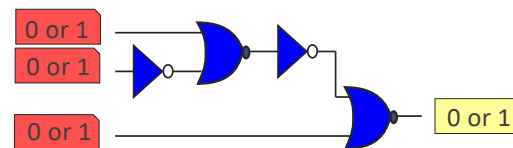
2021 First 2 nm chip with
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Classical computers

Elementary information:

Bit: 0 or 1

Processed with logic gates (transistors)

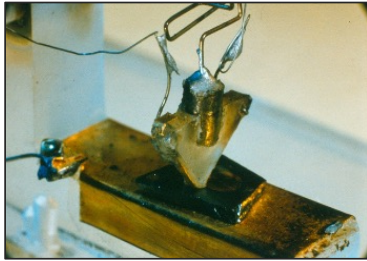


NOT and a single 2 bit gate
(as **XOR**) are enough :

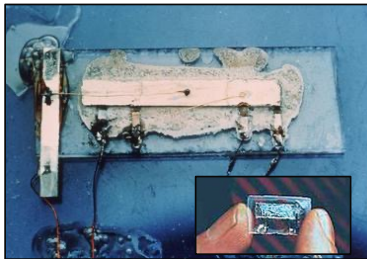
Universal set



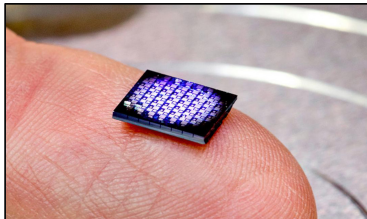
Quantum revolution of information treatment



1947 First transistor
@Bell-Lab



1959, First chip
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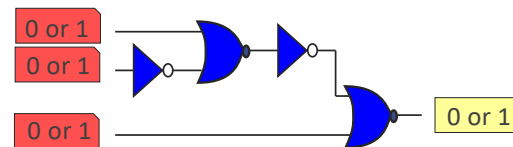
2021 First 2 nm chip with
50 billion transistors @IBM

Classical computers

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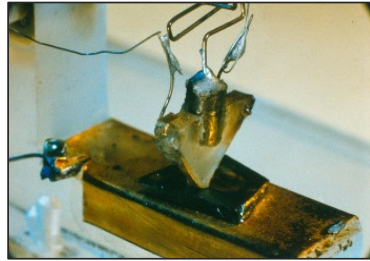


NOT and a single 2 bit gate
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Universal set

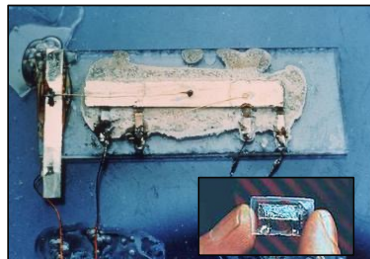




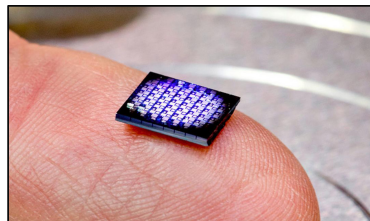
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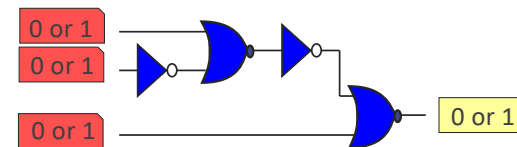
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50 billion transistors @IBM

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Elementary information:

Bit: 0 or 1

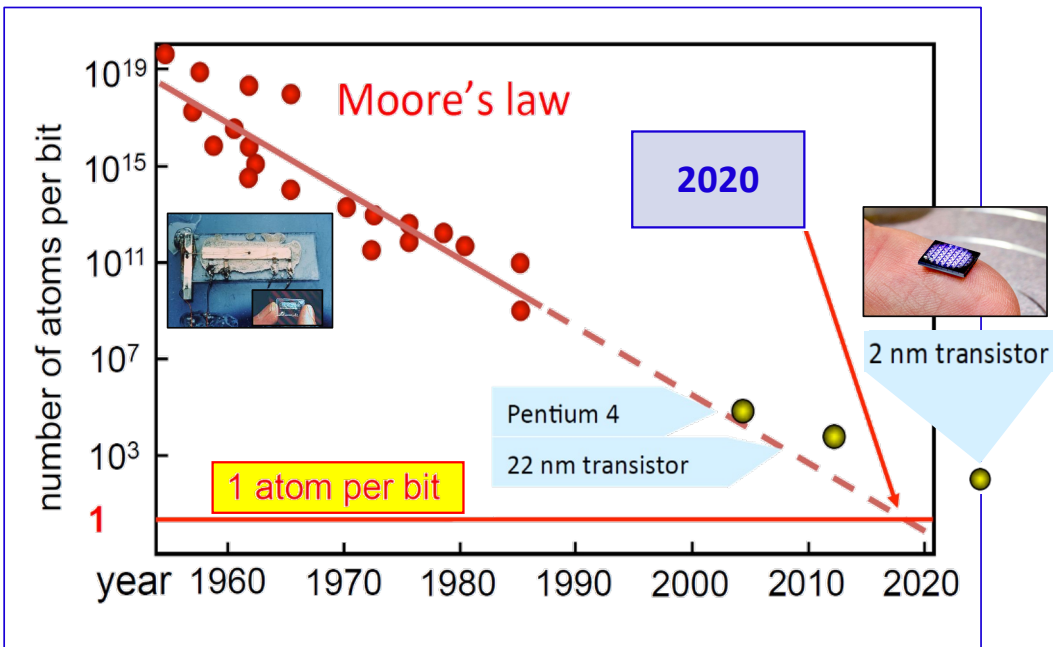
Processed with logic gates (transistors)



NOT and a single 2 bit gate
(as **XOR**) are enough :

Universal set

Are reaching the limit of one atom per bit

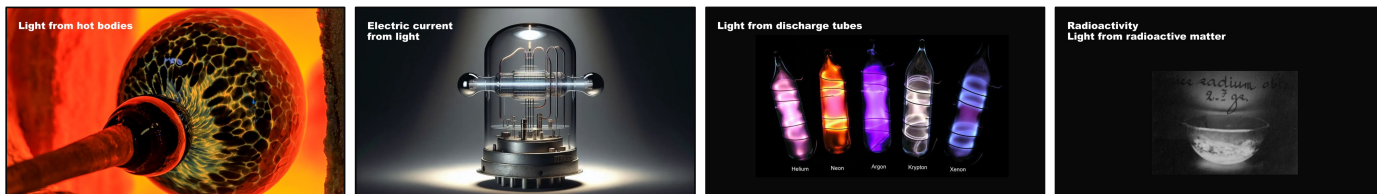


Take home message

Quantum revolution 1.0



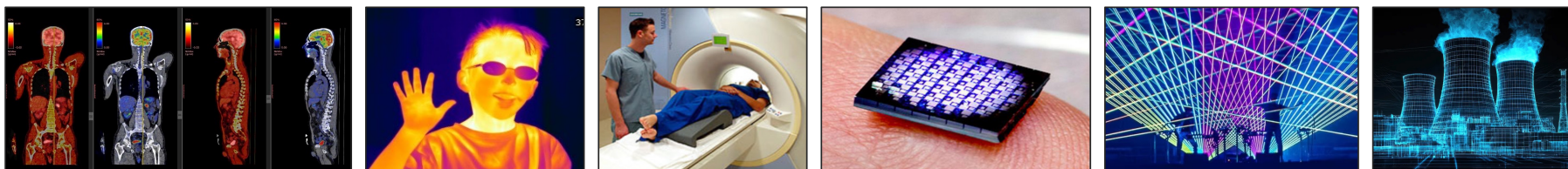
A century ago, **minor issues between light and matter**



Forced the best physicist to invent quantum mechanic
matter and light are particles described as superposition's of states governed by wave dynamics



Which has **revolutionize science and technology**



But reaching now the limits of miniaturization

Is it the end of the quantum revolution?

2.

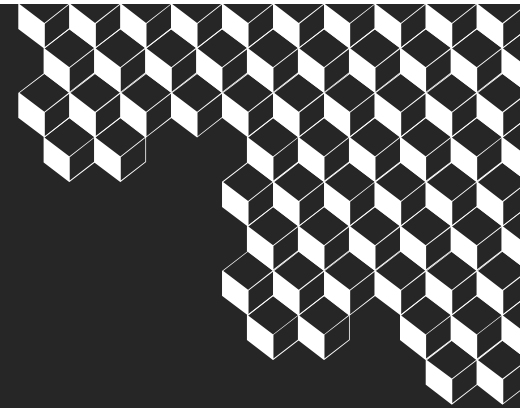
Is it the end of the quantum revolution?

No!

A second quantum revolution is about to reshape our world!



**What makes a second
revolution possible ?**



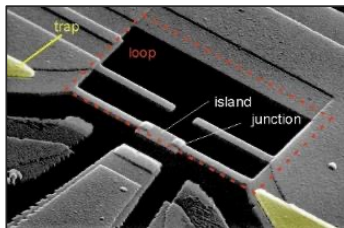
The same reason why the first one is ending





The same reason why the first one is ending

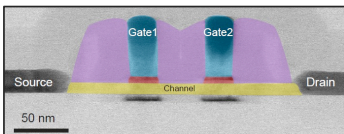
Technology reaching the limit of individual quantum object / degree of freedom



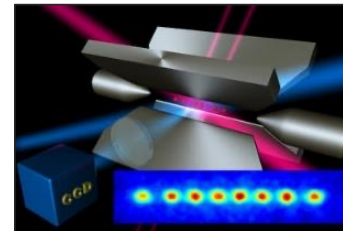
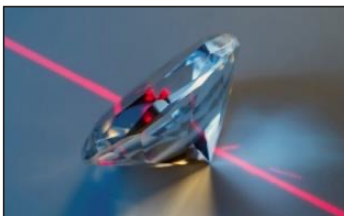
- Individual electron pair / individual quantum of superconductor current
 - In qantronium - transmon



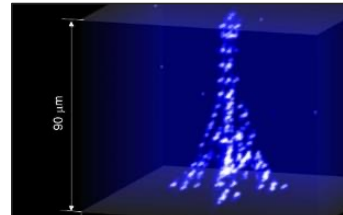
- Individual photon
 - Detection
 - Emission



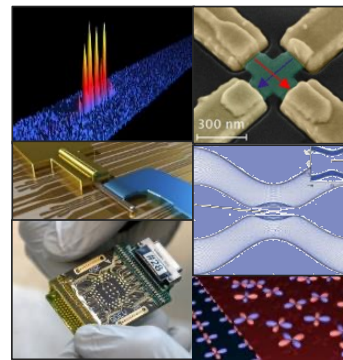
- Individual spin
 - Electrons or holes in semiconductors (AsGa, Si, Ge, ...)
 - Individual NV centers NV in diamond (Nitrogen vacancy)



- Individual ions
 - In traps



- Individual atoms or Molécules
 - In laser trapping and cooling systems

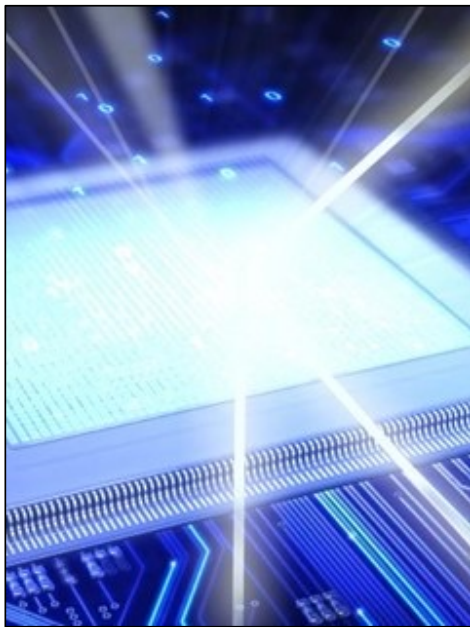


- Individual novel quantum degree of freedom in new quantum materials
 - Flying qubits, levitons, pseudospin, Skyrmions, spin-orbit coupling, 2D systems, topological materials, Majorana fermions, anti/multi-ferroelectric materials...

From quantum 1.0 to quantum 2.0

► Quantique 1.0: Reaching its end

Manipulating macroscopic quantum systems
ie with many quantum “objects”/ degrees of freedom



Germanium laser

► Same quantum degrees of freedom
but
going from a macroscopic ensemble
to individual states

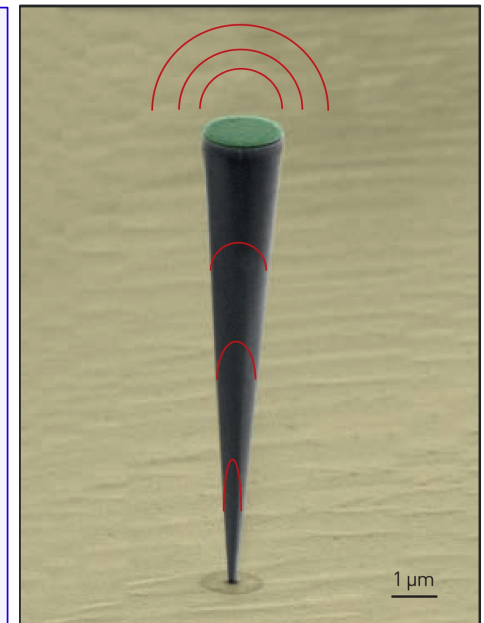
► Huge paradigm shift
for the accessible space of possibilities
=> access to the **huge** space of quantum states
(Hilbert/Fock space)

=> access the "strangest" quantum phenomena

- **Superposition**
- **Non-locality**
- **Entanglement**

► Quantique 2.0: Opens a new world

Mastering individual quantum “objects”
ie individual quantum degrees of freedom



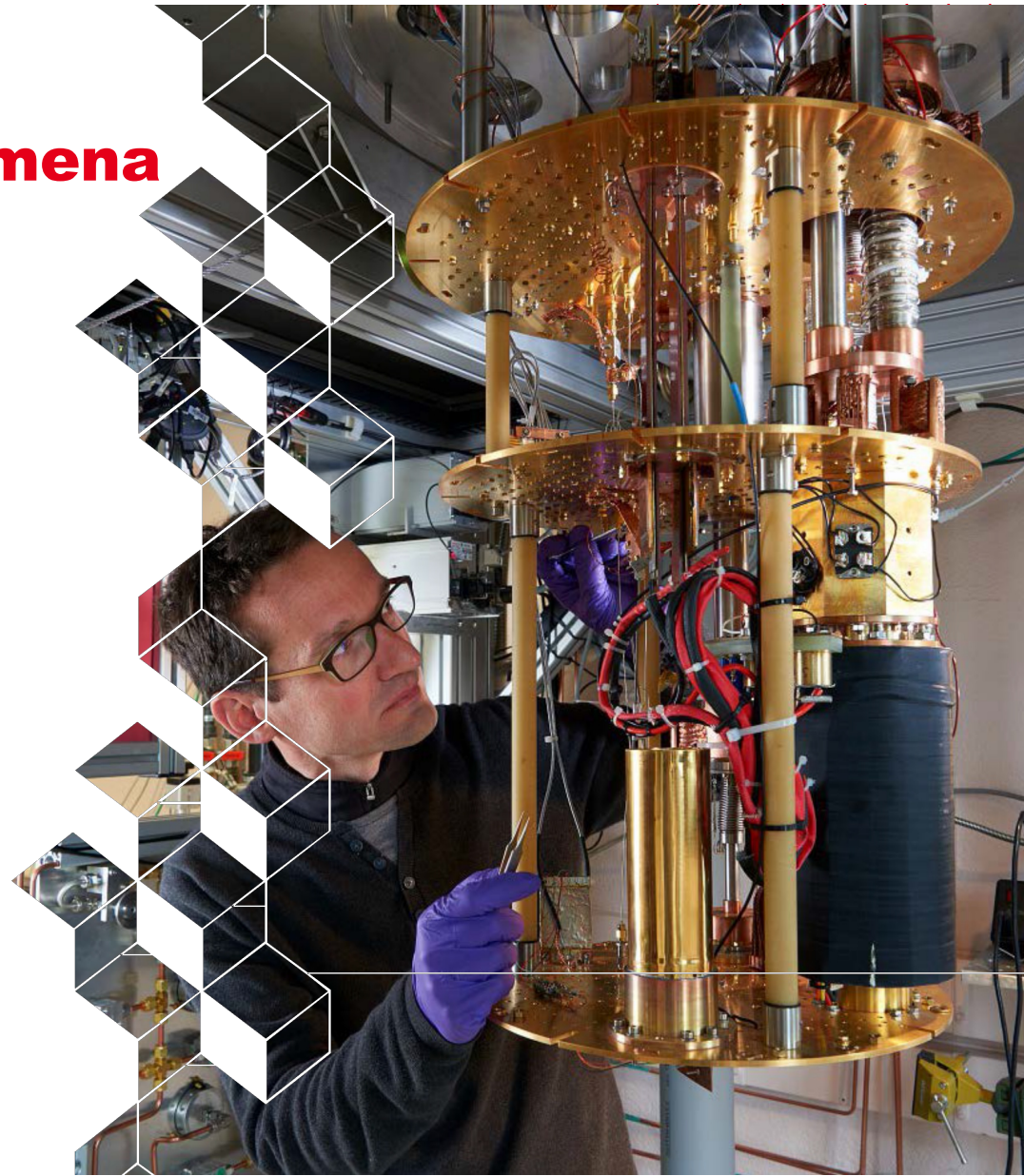
Single photon source

**Accessing
"strangest" quantum phenomena**

**What means
Superposition?**

Non-locality?

Entanglement?



Superposition



Superposition since waves overlap

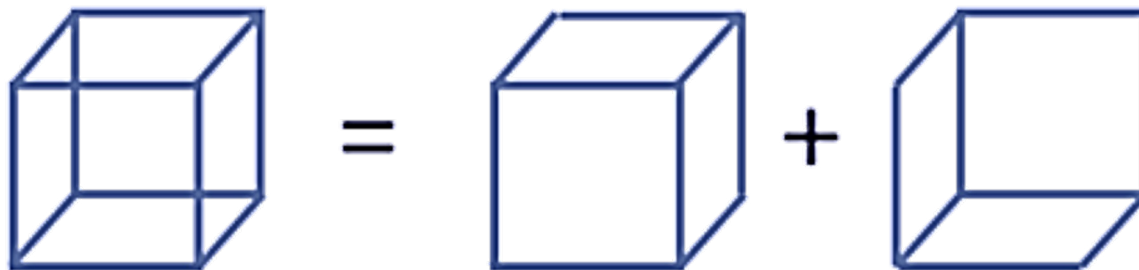


Matter and light are particles described as
superposition's of states governed by wave dynamics

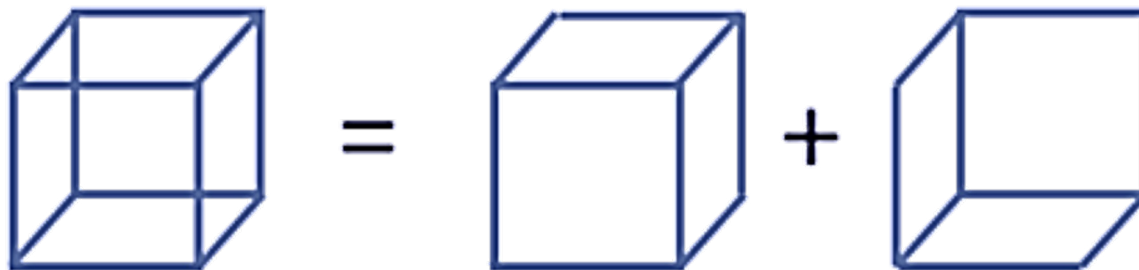
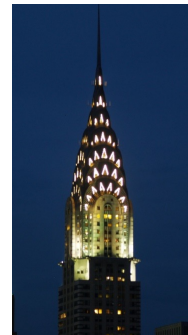
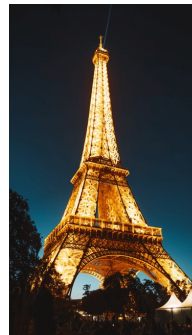
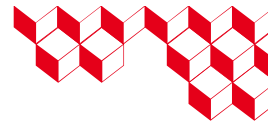




Superposition since waves overlap



Non-locality since waves are extended

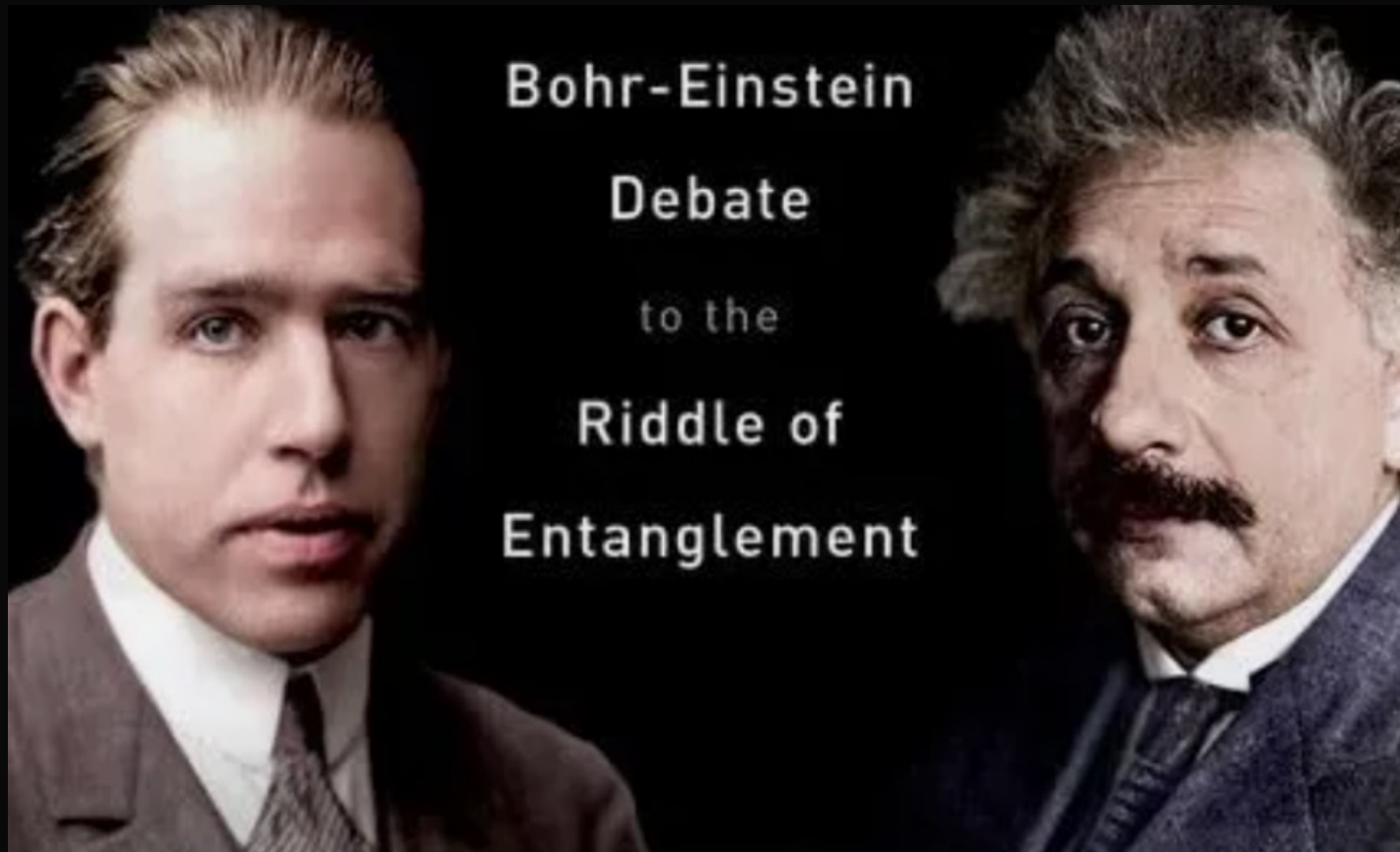


Entanglement

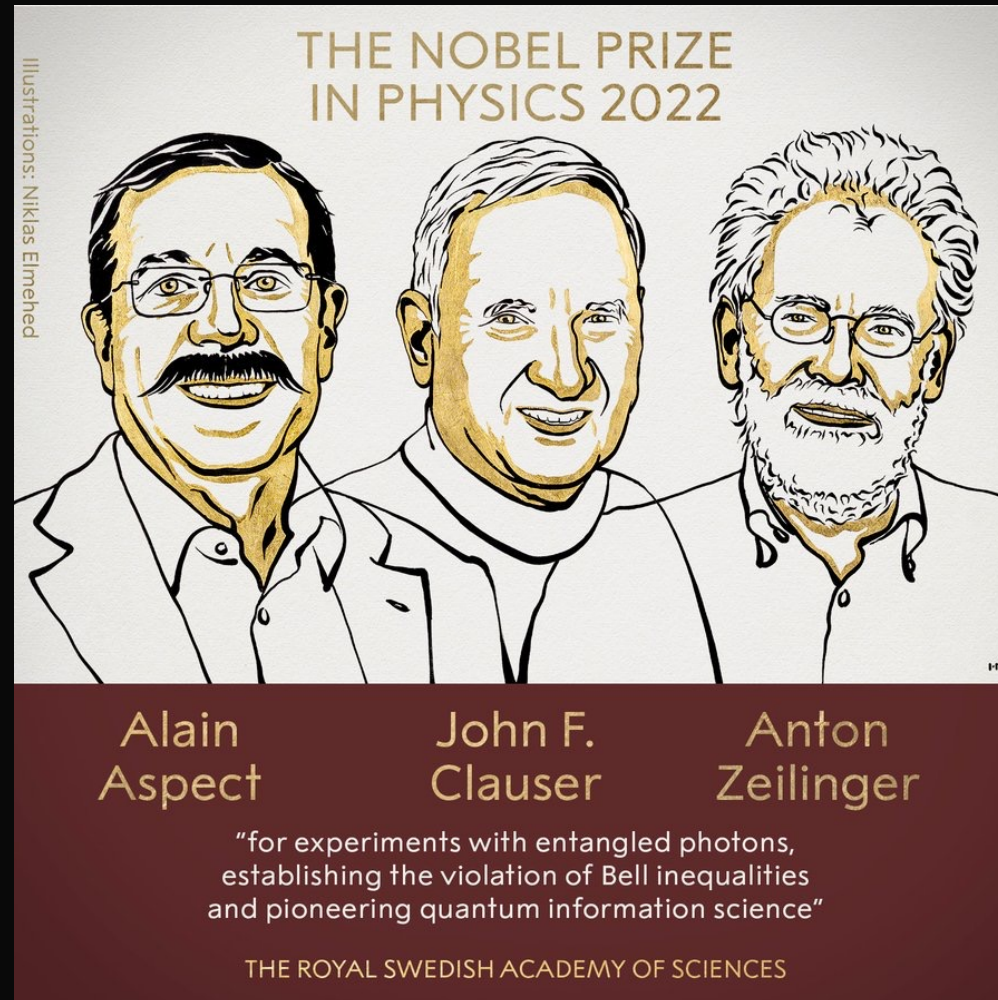
Entanglement



Entanglement



Entanglement



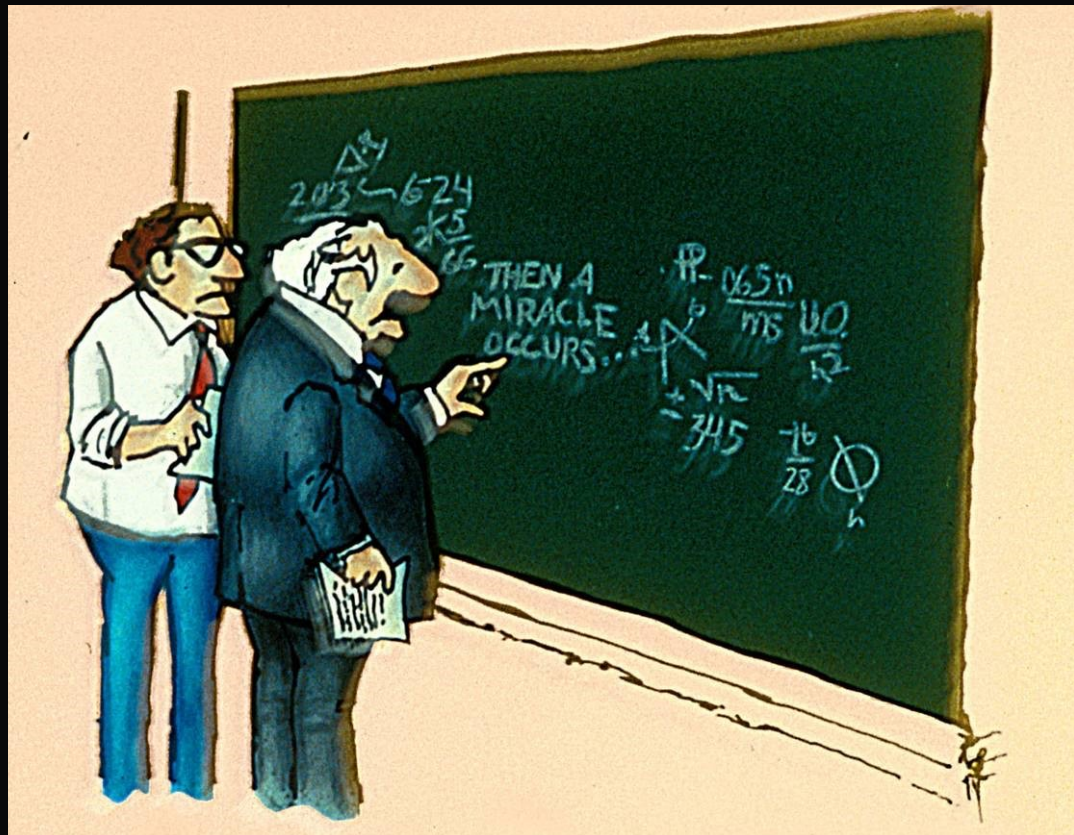
Entanglement



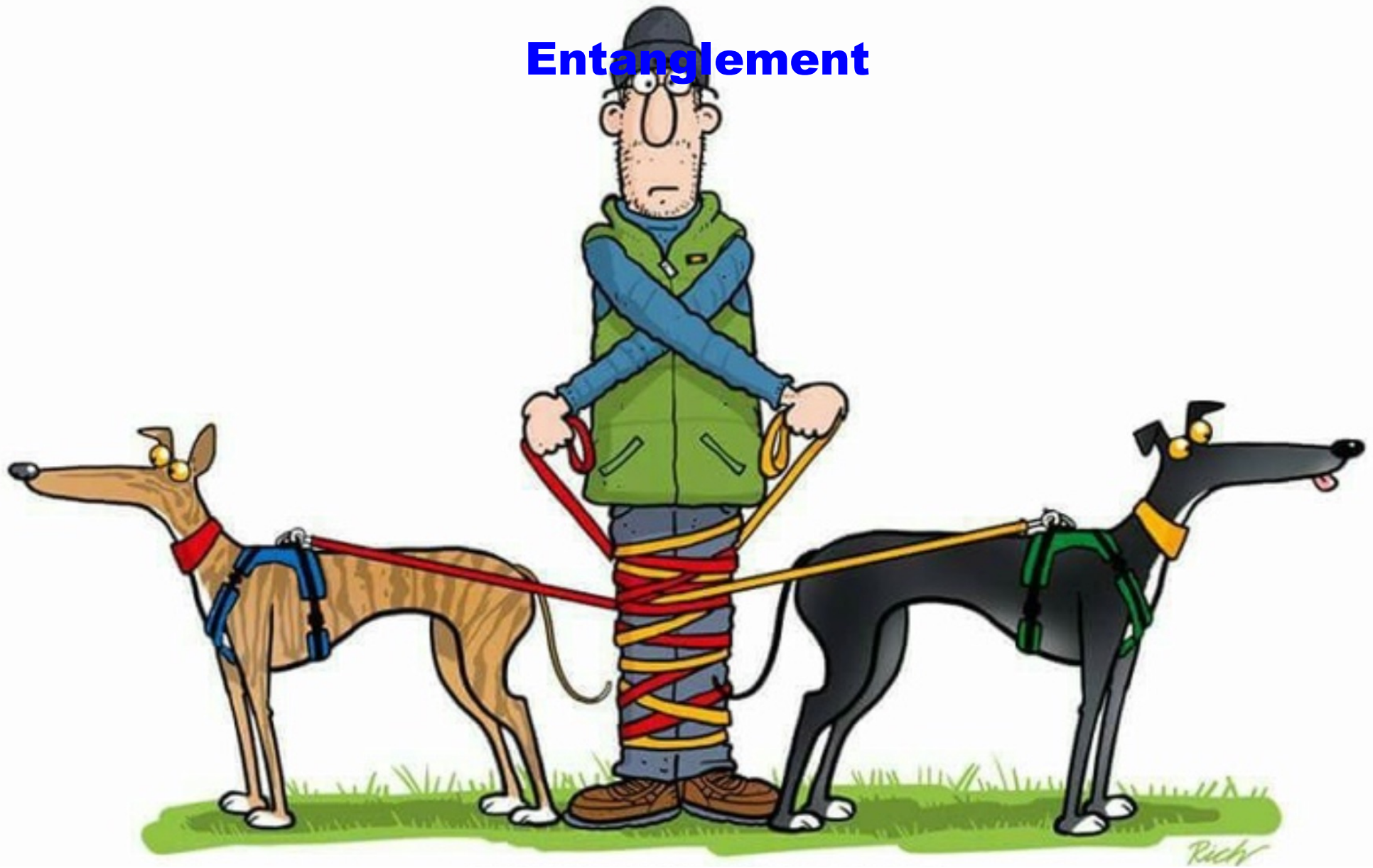
Entanglement



Entanglement



Entanglement



Entanglement



+



Entanglement



+



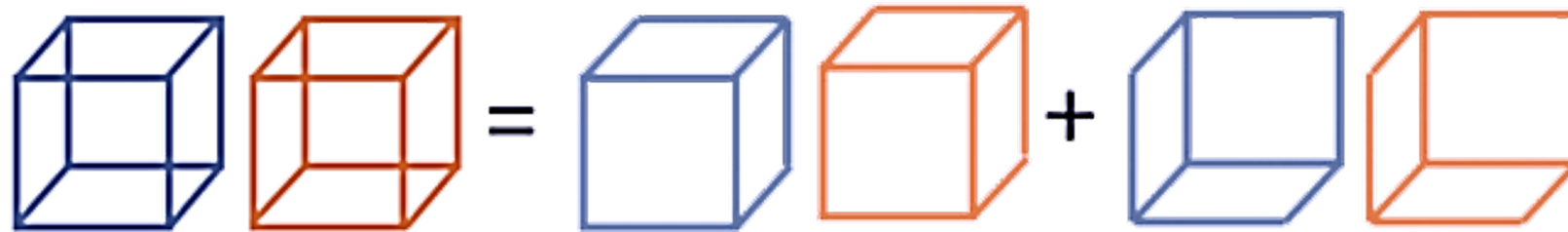
Superposition

2 or more quantum objects/degrees of freedom



Entanglement

Superposition 2 or more quantum objects



Coupled quantum objects cannot be considered separately => they are intertwined: entangled



EINSTEIN ATTACKS

MAY 15, 1935

PHYSICAL REVIEW

VOLUME 47

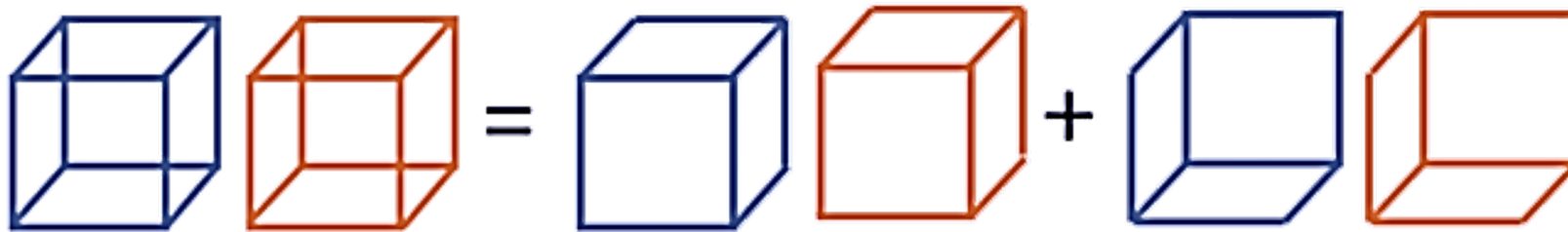
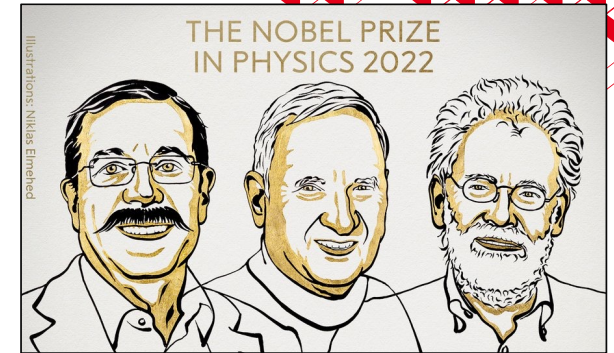
Can Quantum-Mechanical Description of Physical Reality Be Considered Complete?

A. EINSTEIN, B. PODOLSKY AND N. ROSEN, *Institute for Advanced Study, Princeton, New Jersey*

(Received March 25, 1935)

Entanglement

Superposition
2 or more quantum objects

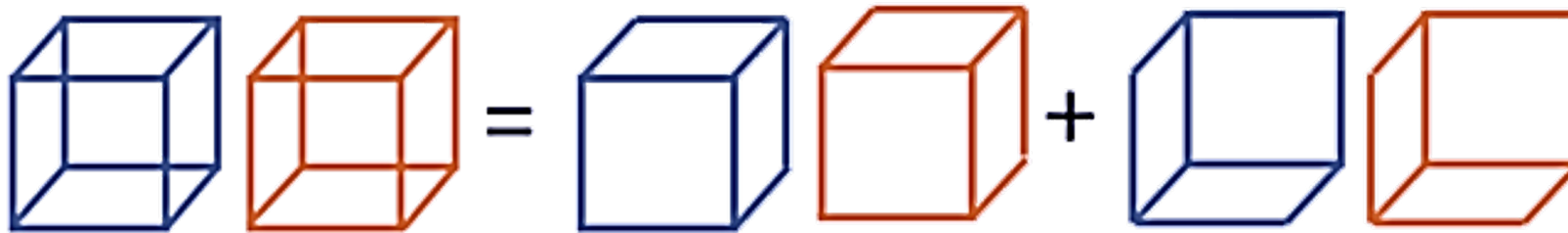


Coupled quantum objects cannot be considered separately => they are intertwined: entangled

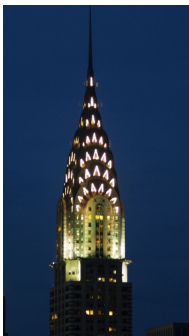
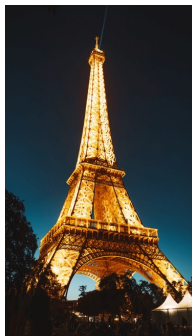


Entanglement

Superposition
2 or more quantum objects



Coupled quantum objects cannot be considered separately => they are intertwined: entangled



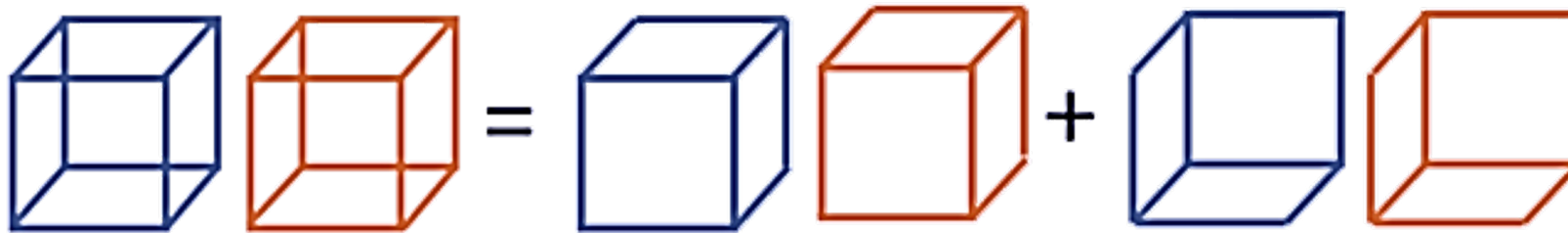
Non locality

If the blue in Paris is observed pointing left, then the red in New York points left
Conversely,
If the blue in Paris is observed pointing right, the red in New York points right



Entanglement and computing

Superposition
2 or more quantum objects



Coupled quantum objects cannot be considered separately => they are intertwined: entangled

Entanglement and the exponential growth of the space of states

N quantum objects with 2 states each (N quantum bits / Qubits) => 2^N possible entangled states

- ⇒ Access to the enormous space with 2^N dimensions for entangled states
- ⇒ Evolutions of 2^N solutions "simultaneously"

Sissa's Chessboard



Sissa's Chessboard

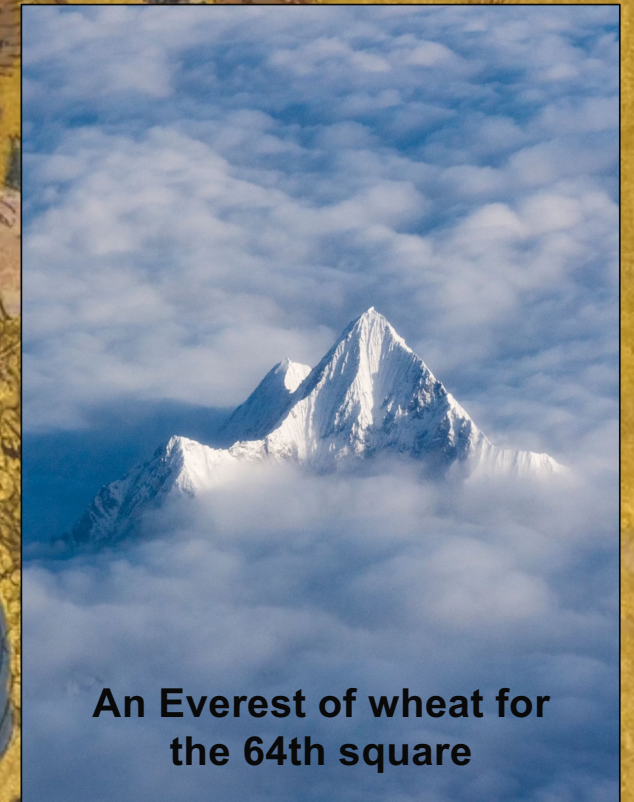


The Grand Vizier Sissa ben Dahir presents his new game, chess, to the Indian king Shirham and requests his reward: "Just 1 grain of wheat on the first square, 2 on the second, 4 on the third, 8 on the fourth, ... and so on, doubling the number of grains on each square up to the sixty-fourth."

The king agreed, not realizing that it would require a cube 10 km wide and 10 km high to contain the 2^{63} grains of wheat for the sixty-fourth square... and 1,000 years of global wheat production to fill it!



Sissa's Chessboard



**An Everest of wheat for
the 64th square**

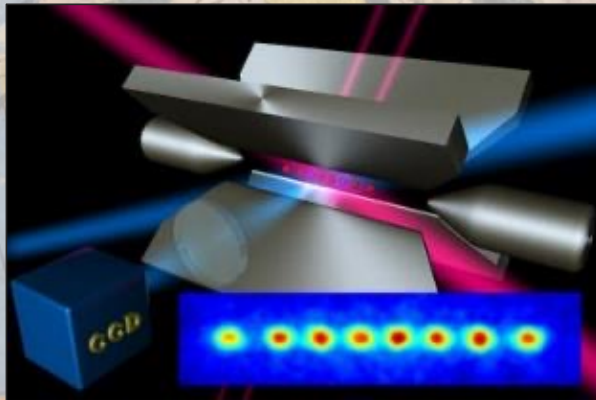
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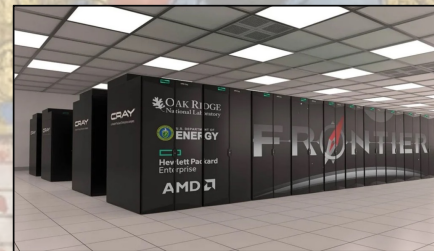
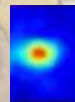


Sissa's Computer

Adding a **single** quantum object/qubit **doubles** the size of the space of entangled states
To manipulate this space on classical computers we must **double** their size



+

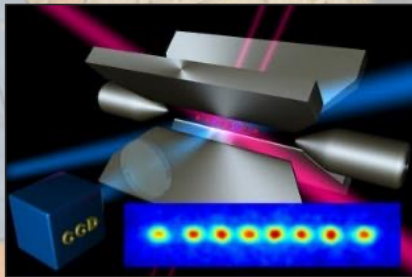


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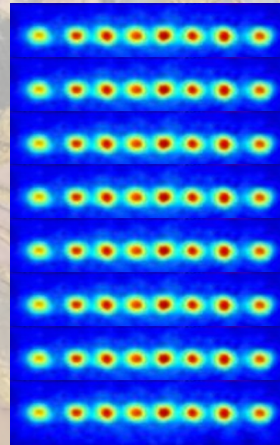


Sissa's Computer

Adding 64 quantum object/qubit multiplies by 2^{64} the size of the space of entangled states
To manipulate this space on classical computers we must multiply by 2^{64} their size



+



Several Everest of
computers





2.0 quantum revolution disrupting information and communication society



Mastering individual quantum objects: ultimate sensitivity



QUANTUM
Sensing
metrology



Entangling distant quantum objects: unbreakable communications



QUANTUM
Communication



Massive entanglement: unprecedented computational power



QUANTUM
Computing



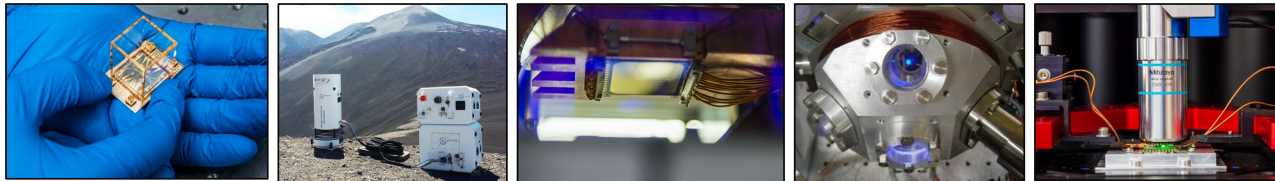
QUANTUM
Simulation



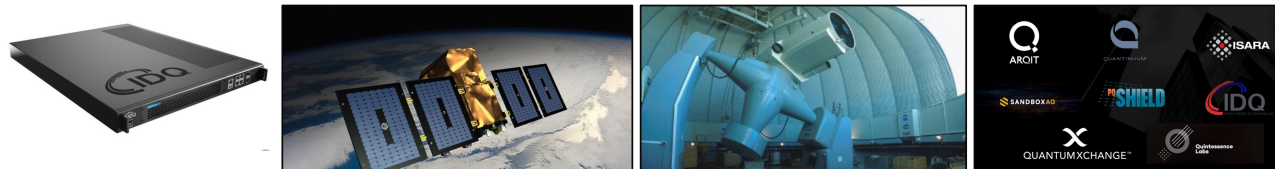
2.0 quantum revolution disrupting information and communication society



Mastering individual quantum objects: ultimate sensitivity



Entangling distant quantum objects: unbreakable communications



Massive entanglement: unprecedented computational power

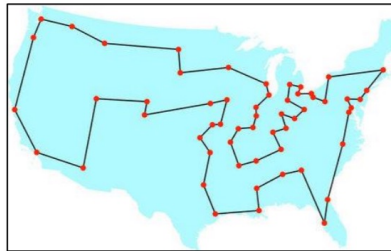




Quantum computing: Disruptive potential

Changing the World

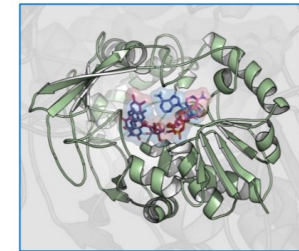
TIME
“Quantum
Will Change
Everything”



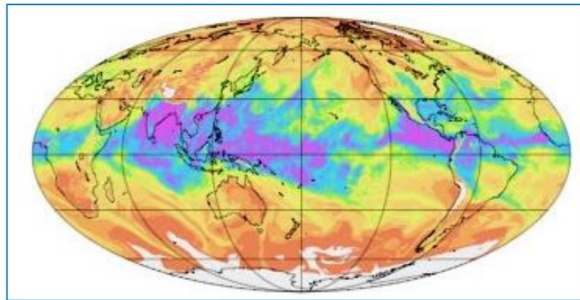
Travel and Logistics



Image Processing



Pharmacology



Improved Forecasting



Improved Stock ROI



Cryptography

Take home message

Quantum revolution 2.0

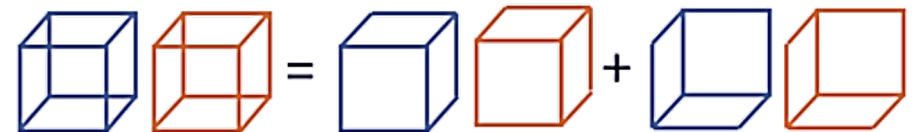
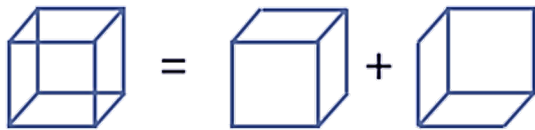


Technology mastering **individual quantum object** / degree of freedom



Is giving access to powerful quantum phenomena

Superposition of quantum states, **Non-locality** of quantum states, **Entanglement** of quantum states



With a huge disruption potential

ultimate **sensitivity**, unbreakable **communications**, unprecedented **computational power**



Is it the end of the story?



3.

Is it the end of the story?

No!

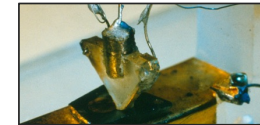
This only the beginning and success is not guaranteed!



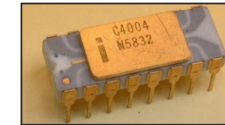
Quantique 2.0: Major difficulties

► Fabrication challenges:

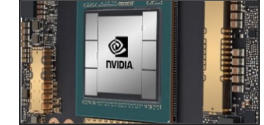
- Even more difficult than the 1st quantum revolution



1947, 1st Transistor

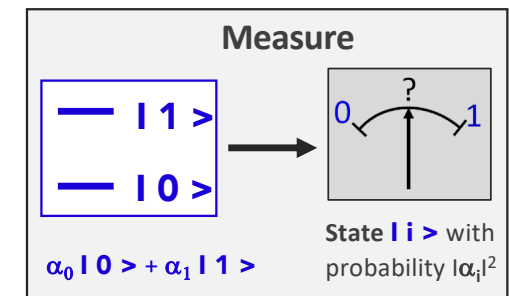
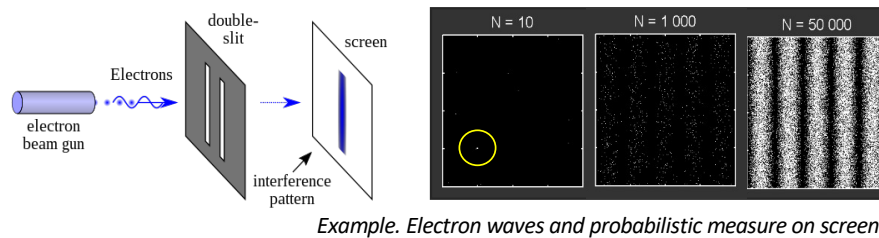


1971, 2 300 transistors.



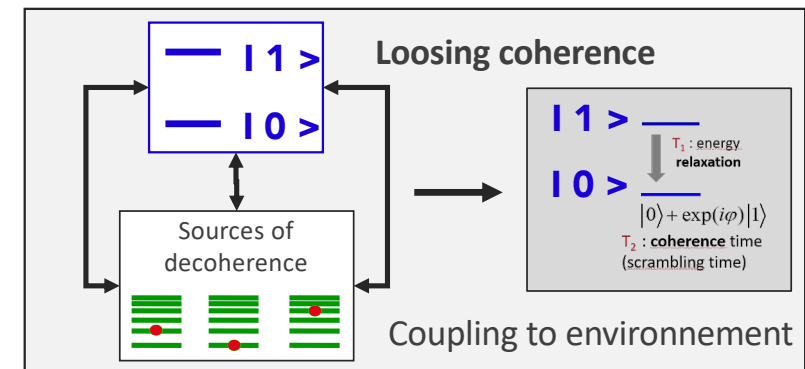
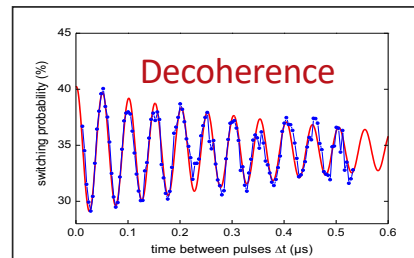
2020, 54 milliard transistors

► Quantum is probabilistic: the measure destroys the superposition

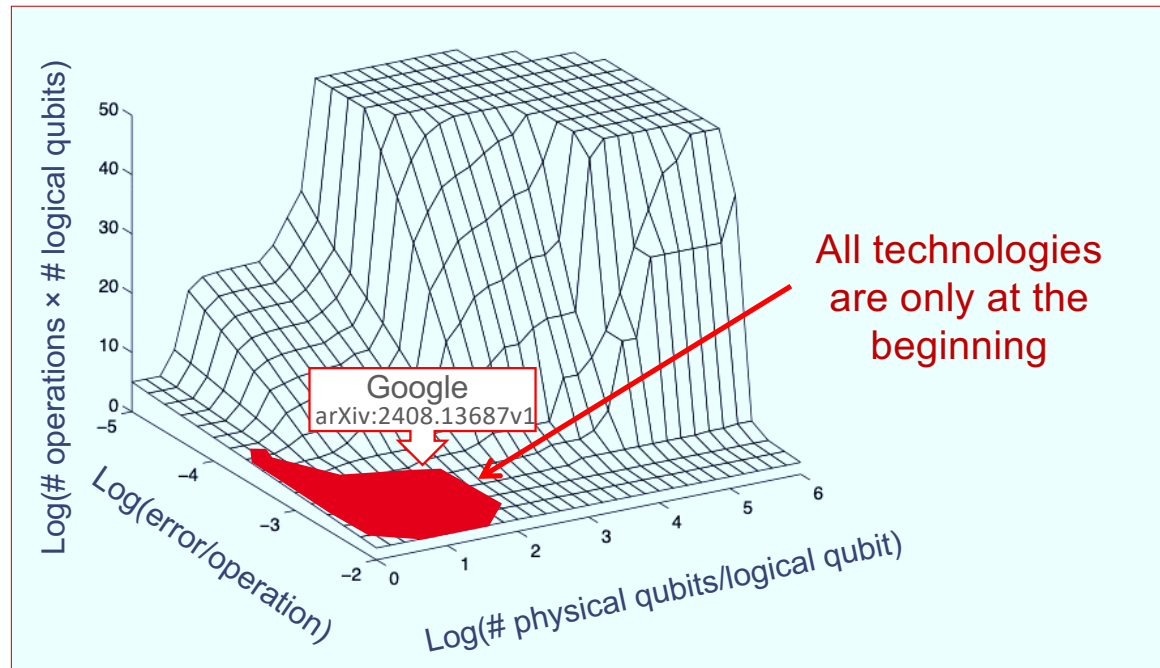


► Coupling to environment is destroying coherence: Superposition & entanglement

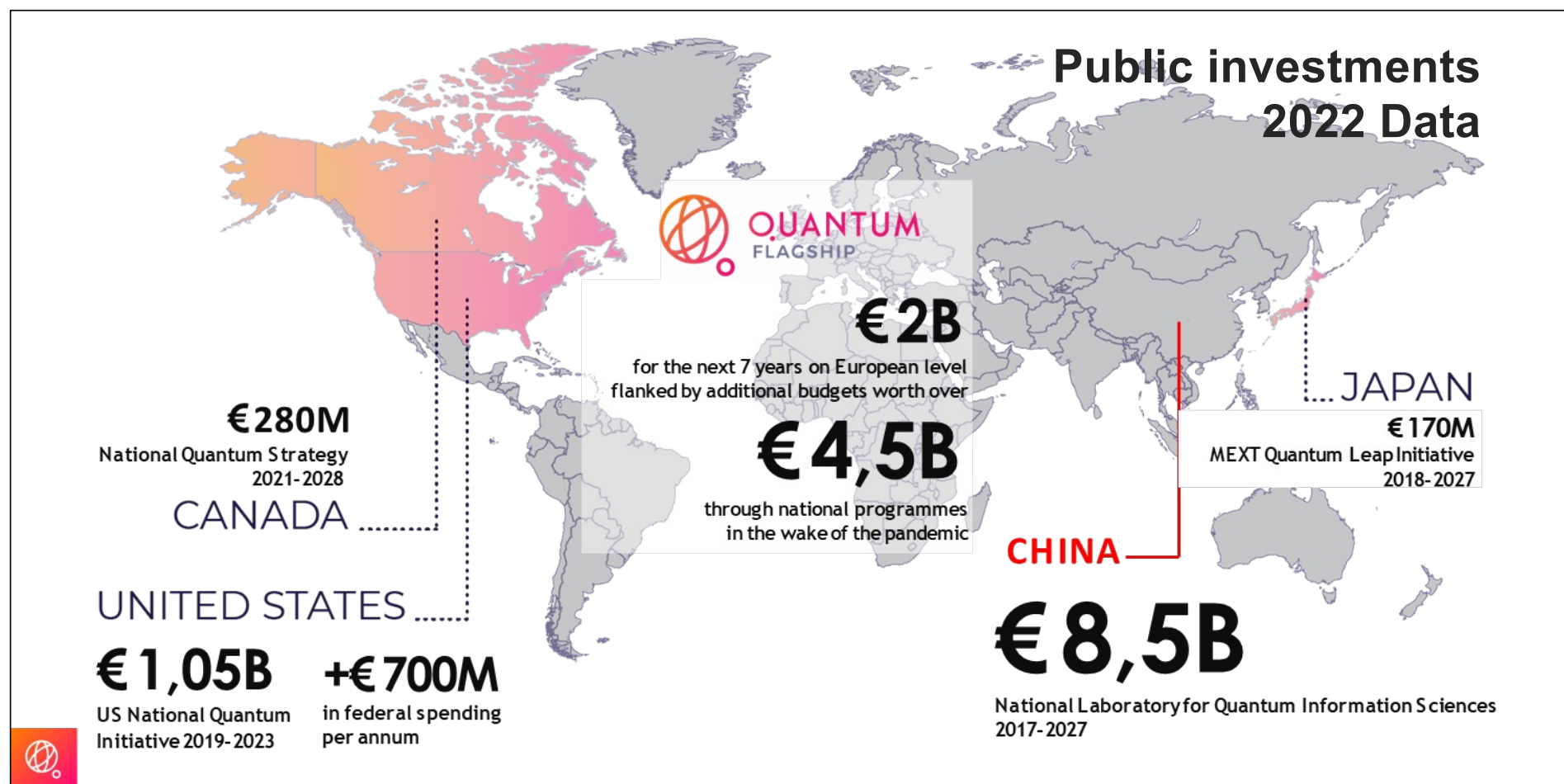
- Error correction codes needed
=> thousands of physical qubits to protect a single logical qubit
- Or new robust qubits protected from decoherence



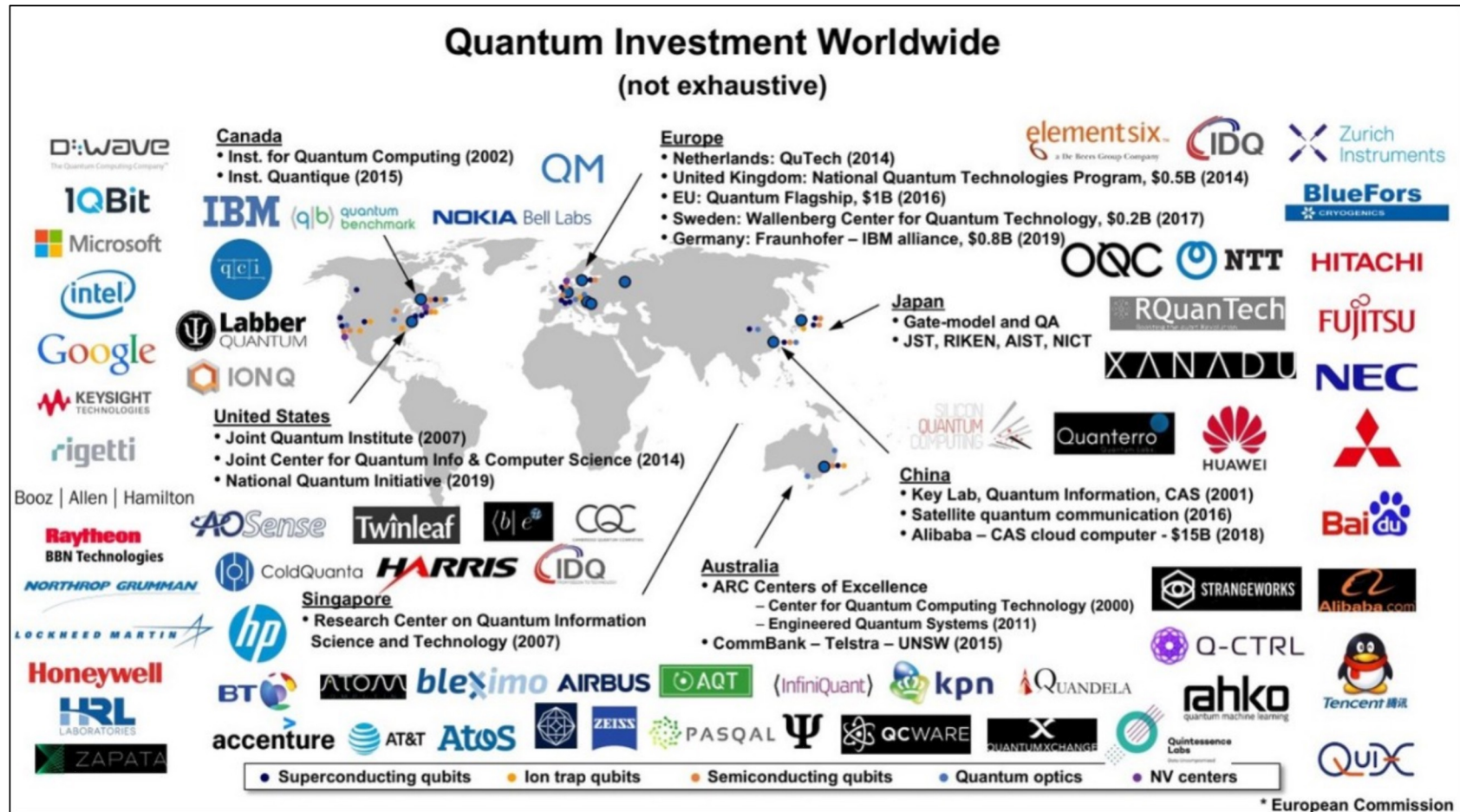
Reduction of quantum errors needed before any applications of quantum computing



2022 International competition and collaboration



2022 International competition and collaboration



Conclusion: a revolution to come

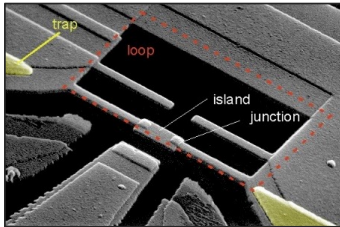




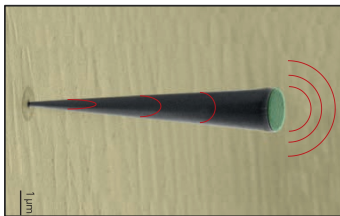
4. ■ Back-up

Many possible technologies/degrees of freedom

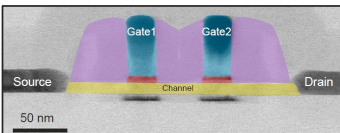
Quantum “objects”/degrees of freedom



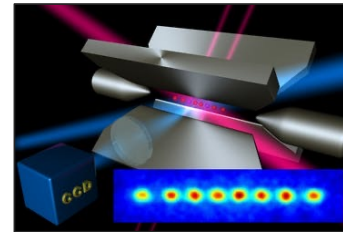
- Electrons pairs / superconducting current
 - Quantonium - transmon



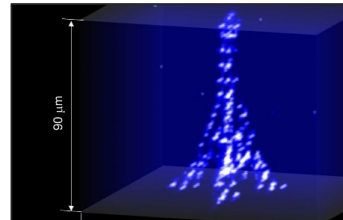
- Photons



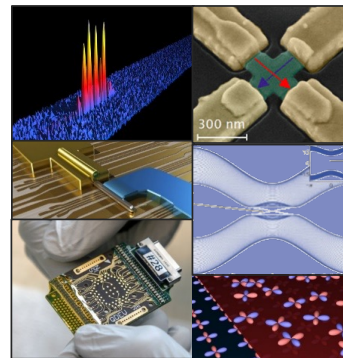
- Spin
 - Electrons or holes in semiconductors (AsGa, Si, Ge, ...)
 - NV centers in diamond (Nitrogen vacancy)



- Ions



- Atoms
- Molecules



- New quantum degrees of freedom / quantum materials
 - Flying qubits, surface states, leviton, pseudospin, Skyrmions, spin-orbital, 2D systems, topological materials, Majorana fermions, anti/multi-ferroic ...

Different quantum computing strategies



► Quantum annealing

$$|\psi\rangle \Rightarrow |\psi_0\rangle$$

Looking for ground states

- adiabatic optimization
- exploring many paths
- using tunnel effects

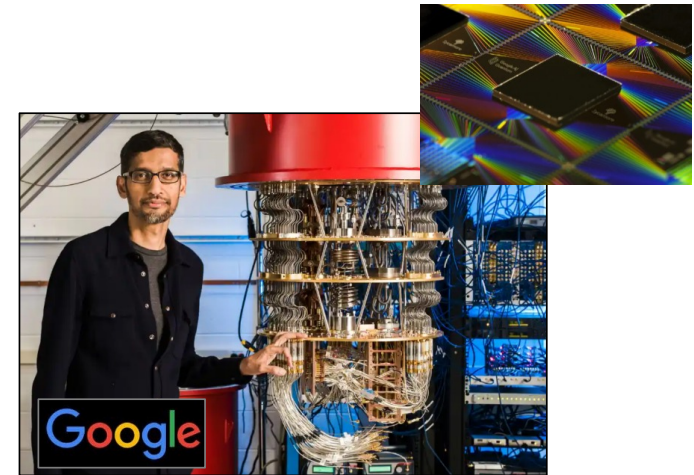


► Quantum simulation

$$|\psi(t)\rangle = \hat{U}(0,t) |\psi(0)\rangle$$

Quantum evolution

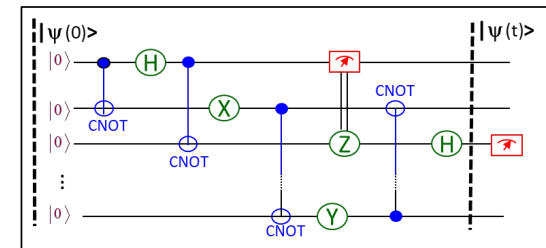
- analogue computing



► Quantum digital computing

$$|\psi(N\Delta t)\rangle = \hat{U}_N(\Delta t) \dots \hat{U}_1(\Delta t) |\psi(0)\rangle$$

Gate based evolution

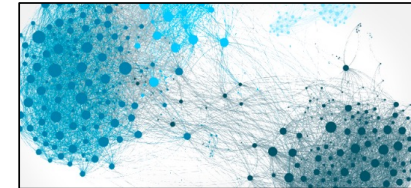


Main classes of quantum algorithms

► Search

based on Deutsch-Jozsa, Simon and Grover's algorithms

- Polynomial acceleration



Exploring graphs and data bases

► Quantum Fourier transforms (QFT)

such as Shor's algorithm for factorization (&Bitcoin)

- Exponential acceleration



Cryptography

► Optimization

searching equilibrium point of a complex system
such as neural network and optimal path (PCA)

- Exponential acceleration



Image processing



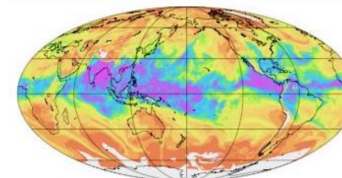
Market evolution

► Quantum simulation and variational approach

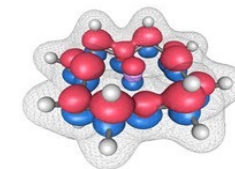
Quantum many body problems

Resolution of linear differential equations (HHL)

- Exponential acceleration



Weather broadcast



Molecules

Computing in the 2^N dimensions' space of quantum states (Hilbert/Fock)

Classical computers

Classical bit: $|i\rangle = |0\rangle \text{ ou } |1\rangle$

(2 possibilities)

Classical Register: $|X\rangle = |i_1\rangle |i_2\rangle \dots |i_N\rangle$

(2^N possibilities)

Classical computing: $|X\rangle \rightarrow |Y\rangle = T |X\rangle$

(Turing machine)

← completely different computing paradigm →

Quantum computers

$\alpha |0\rangle + \beta |1\rangle$: QuBit, Quantum bit
(R^3 possibilities, 3D)

$|X\rangle = \sum \alpha_{i_1, i_2, \dots, i_N} |i_1, i_2, \dots, i_N\rangle$: Quantum register
(C^{2^N} possibilities, 2^N D)

$|X\rangle \rightarrow |X\rangle = \sum \alpha_{i_1, i_2, \dots, i_N} \hat{U} |i_1, i_2, \dots, i_N\rangle$

: Quantum Computing

(Unitary transformation
+ measuring, statistical projection)

Evolution of 2^N states simultaneously

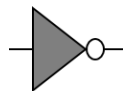
$\Rightarrow$ Computing power and memory beating all classical computers as soon as $N \sim 50$ qubits
(since 2^N soon larger than any classical memory)

Similar “gate” vocabulary but very different paradigms: Turing versus Unitary

Classical computers

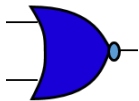
Logic gates in classical computing

Single bit



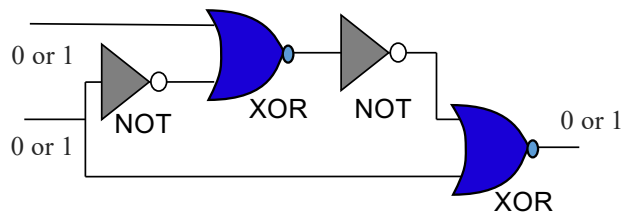
NOT

Double bit



XOR

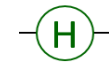
Algorithm: Turing machine



Quantum computers

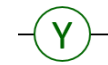
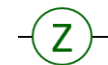
Unitary gates and measurement in quantum

Single Qubit



Pauli matrices
Hadamar

Double Qubit



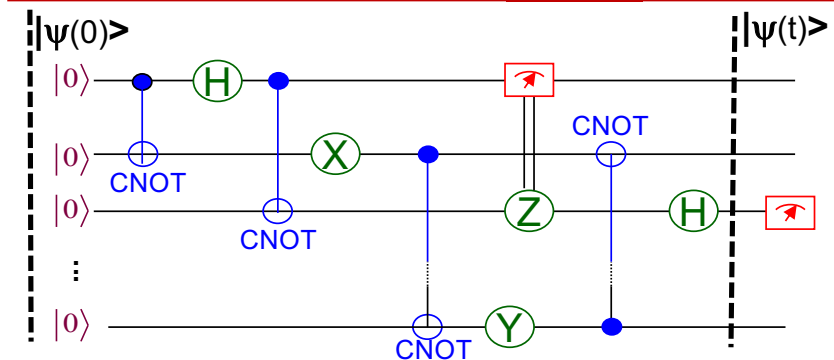
CNOT
(Quantum XOR)

Measurement



Z measurement

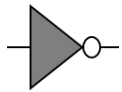
Algorithm: Unitary evolutions + projections



Similar “gate” vocabulary but very different paradigms: Turing versus Unitary

Logical gate in classical computing

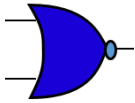
Single bit



NOT

0 → 1
1 → 0

Double bit



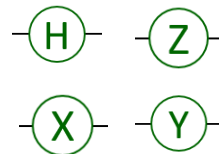
XOR

00 → 0
01 → 1
10 → 1
11 → 0

Function in the space of bits {0,1}

Unitary gates and measurement in quantum computing

Single Qubit



Pauli matrices
Hadamard

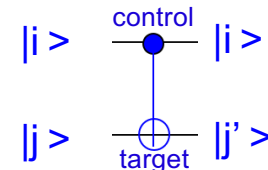
$$|i\rangle \rightarrow \hat{U}|i\rangle = U_{0i}|0\rangle + U_{1i}|1\rangle$$

Ex: Hadamard gate

$$\begin{cases} |0\rangle \rightarrow \frac{|0\rangle + |1\rangle}{\sqrt{2}} \\ |1\rangle \rightarrow \frac{|0\rangle - |1\rangle}{\sqrt{2}} \end{cases}$$

Superposition

Double Qubit



CNOT
(Quantum XOR)

$$|ij\rangle \rightarrow \hat{U}|ij\rangle = U_{00ij}|00\rangle + U_{01ij}|01\rangle + U_{10ij}|10\rangle + U_{11ij}|11\rangle$$

Ex CNOT:

$$\begin{cases} |00\rangle \rightarrow |00\rangle \\ |01\rangle \rightarrow |01\rangle \\ |10\rangle \rightarrow |11\rangle \\ |11\rangle \rightarrow |10\rangle \end{cases}$$

Entanglement

Qubit Measurement



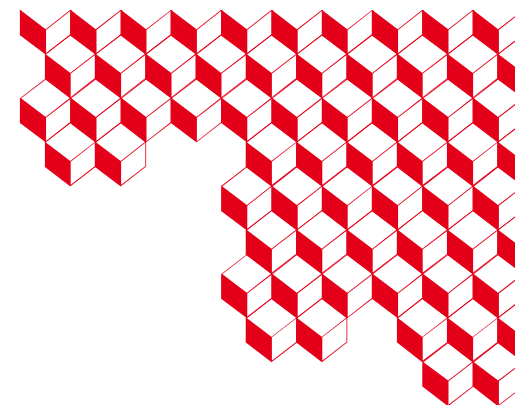
Z measurement

$\alpha_0|0\rangle + \alpha_1|1\rangle \rightarrow$
either
|0> with $p=|\alpha_0|^2$
or
|1> with $p=|\alpha_1|^2$
when measuring
either 0 or 1.

Projection

Unitary transformation

Probabilistic



Merci pour votre attention