

## Extension 2 I: An Equation for Multiple Extraction

### 1. Prerequisites

The ideas required to understand this section are:

| Topic                                 | Book page |
|---------------------------------------|-----------|
| Solvent extraction                    | 378       |
| Reasoning behind multiple extractions | 380       |

### 2. Equation for multiple extractions

Aqueous industrial effluent often contains substances which may be separated out using organic solvents. Recovery of the substances may take several stages. The following equation can be used to calculate the mass of a substance left in the aqueous solvent after several extractions:

$$m = m_0 \left[ \frac{V_{\text{aq}}}{K_d \cdot V + V_{\text{aq}}} \right]^n$$

Where:

- $m_0$  = the mass (in g) of the substance to be recovered before extraction begins;
- $m$  = the mass (in g) of the substance left in the effluent after  $n$  extractions;
- $K_d$  = the distribution ratio of the substance to be recovered between the organic solvent and water;
- $V$  = the volume of organic solvent used in each stage of the extraction (in  $\text{cm}^3$ ). (Note that it must always be the same);
- $V_{\text{aq}}$  = the volume of the aqueous effluent (in  $\text{cm}^3$ ); and
- $n$  = number of extractions

Using the equation for the worked example in Box 21.4, p. 380.

For two extractions using ethoxyethane:

$$m_0 = 10.0 \text{ g}$$

$$m = ? \text{ g}$$

$$K_d = 4$$

$$V = 50 \text{ cm}^3$$

$$V_{\text{aq}} = 100 \text{ cm}^3$$

$$n = 2$$

$$m = 10.0 \left[ \frac{100}{(4 \times 50) + 100} \right]^2$$

or  $m = 1.1 \text{ g}$  (or  $10.0 - 1.1 = 8.9 \text{ g}$  is the mass extracted)  
(which agrees with the answer obtained in Box 21.4!)

## EXERCISE 21A

## Using the equation for multiple extractions

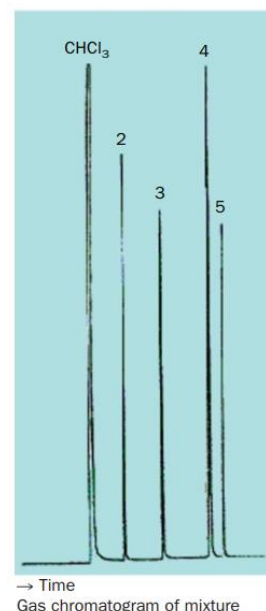
See if you can use the equation for multiple extractions to obtain the answer to the following: The distribution ratio of an organic compound X between toluene (methylbenzene) and water is 7.0. An aqueous mixture ( $100 \text{ cm}^3$ ) contains 1.0 g of X. The mixture is extracted twice using  $100 \text{ cm}^3$  of toluene each time. What mass of X is extracted into the organic layer?

## Revision questions

- Which mixture would be the most difficult to separate, and why?
  - Benzene (boiling point  $80^\circ\text{C}$ ) and cyclohexane (boiling point  $78^\circ\text{C}$ )
  - Benzene (boiling point  $80^\circ\text{C}$ ) and 1,4-dimethylbenzene (boiling point  $138^\circ\text{C}$ )
- A mixture of hydrocarbons was dissolved in trichloromethane and separated by gas chromatography through a column at a temperature of  $150^\circ\text{C}$ . The constituents of the initial mixture and the resulting gas chromatogram are shown below.
  - Assign the hydrocarbons responsible for peaks 2-5.
  - Which hydrocarbon is not shown on the chromatogram (shown on the right), and why?

## Constituents of hydrocarbon mixture

| Compound            | Boiling point/ $^\circ\text{C}$ | Molecular weight/u | Formula                   |
|---------------------|---------------------------------|--------------------|---------------------------|
| Trichloromethane    | 61                              | 119.5              | $\text{CHCl}_3$           |
| Benzene             | 80                              | 78                 | $\text{C}_6\text{H}_6$    |
| Ethylbenzene        | 136                             | 106                | $\text{C}_8\text{H}_{10}$ |
| Propylbenzene       | 159                             | 120                | $\text{C}_9\text{H}_{12}$ |
| Toluene             | 110                             | 92                 | $\text{C}_7\text{H}_8$    |
| 1,2-dimethylbenzene | 144                             | 106                | $\text{C}_8\text{H}_{10}$ |



- You are required to separate a mixture of benzoic acid and charcoal. Benzoic acid is soluble in hot water, but insoluble in cold water. Charcoal is insoluble in both cold and hot water. Describe how you would separate the mixture.
- Lemongrass oil contains citral, an oily substance that is used in the manufacture of vitamin A. Lemongrass oil boils at  $229^\circ\text{C}$ , but it decomposes/polymerizes at temperatures near boiling. What method might you be able to use to extract citral?
- Use the equation for multiple extractions to calculate the number of extraction stages needed to extract 95% by mass of a substance from  $1000 \text{ cm}^3$  of aqueous layer (which initially contains 100 g of substance to be extracted) using  $100 \text{ cm}^3$  of solvent in each stage ( $K_d = 10$ ).

## Answers

### Exercises

#### Exercise 21A

$$m = 1 \left[ \frac{100}{(7 \times 100) + 100} \right]^2$$

$$m = 0.02 \text{ g}$$

### Revision questions

1. Benzene and cyclohexane would be the most difficult to separate by distillation because they have boiling points that are very close.

2.

(i) The hydrocarbons move through the column according to their volatility. The most volatile (lowest boiling point) has the least retention time. The order therefore is: 2 is benzene; 3 is toluene; 4 is ethylbenzene; and 5 is 1,2-dimethylbenzene.

(ii) Propylbenzene has a boiling point of 159°C and the temperature of the column is 150°C, so it will stay on the column.

3. Recrystallization. Stir the mixture in hot water so that the benzoic acid will dissolve. Filter quickly (Buchner filtration) to remove the charcoal. Allow the hot solution to cool and benzoic acid will precipitate. Filter once more to obtain the purified acid.

4. Steam distillation is useful here, since distillation can take place at a much lower boiling point.

5. After 95% extraction, 5 g of the substance is left:

$$5 = 100 \left[ \frac{1000}{(10 \times 100) + 1000} \right]^n$$

$$\text{or } 5/100 = 0.05 = (1/2)^n$$

$$(1/2)^n = 0.05 \text{ for } n = 5$$

therefore, for  $n = 5$ , over 95% has been extracted.