## SOLUTIONS

## Part I Investment Basics

## PRODUCTS, MARKETS AND PLAYERS

1. One of the best examples of the use of the prefix "Euro" is in the Eurodollar market where US Dollars are being traded outside of the domestic US Dollar market.

Answer is (c)

## Part I Investment Basics

## INVESTMENT RETURN AND RISK

1. Using a HP17B. Note that the repayments are monthly, so we then need to calculate the interest payable on a monthly basis.

Hence there will be $20 \times 12=240$ payments.
FIN, TVM. NB. Set the payments at 1 P/YR (1 per period). The number of periods then becomes 240 .

PV $+100,000$
IR $\quad 6.85 / 12=0.570833$
FV 0
N 240
PMT -766.32

## Answer is (a)

2. We take the monthly standard deviation and multiply by the square root of time. In this case, $5.25 \times \sqrt{12}=18.19 \%$

## Answer is (d)

3. First we calculate the purchase price of the CD

$$
\begin{aligned}
& =\frac{\$ 1,000,000\left[1+\left(0.10 \times \frac{180}{360}\right)\right]}{\left[1+\left(0.095 \times \frac{90}{360}\right)\right]} \\
& =\frac{\$ 1,050,000}{1.02375}=\$ 1,025,641.03
\end{aligned}
$$

Then we calculate the sale price of the CD 30 days later as a 60 day CD

| PRICE | $=\frac{\$ 1,050,000}{\left[1+\left(0.096 \times \frac{60}{360}\right)\right]}$ |
| ---: | :--- |
|  | $=\$ 1,033,464.57$ |

Then we work out the annual holding period return on a 365 day basis

$$
\begin{aligned}
& \begin{array}{c}
\text { HOLDING PERIOD } \\
\text { RETURN }
\end{array} \\
& =\left\{\frac{\$ 1,033,464.57-\$ 1,025,641.03}{\$ 1,025,641.03}\right\} \times \frac{365}{30} \times 100 \\
& =\quad \underline{\underline{9.28 \%}}
\end{aligned}
$$

## Answer is (b)

4. The loan commences on 30 Sept for 6-months, terminating on 31 March, 2003 [30 March is a Sunday]. Using the time function on the HP calculator, the actual days in this three-month period are 182.

Accordingly, given a act/365 day count convention, the interest payable on a £1m deposit is: $\quad £ 1 \mathrm{~m} \times 0.04125 \times 182 / 365=£ 20,568.49$

Answer is (b)
5. Cash flows =

Years $\quad \frac{1-5}{\$ 1000} \quad \frac{6-11}{\$ 2000}$

| Present Value of the cashflows | $:$ | 3790.79 <br> Total PV |
| :---: | :--- | :--- |
| 5408.55 <br> which gives a Future Value of : <br> Required amount: | $\$ 26,246.79 \times(1.10)^{11}$ |  |
| Deficiency | $\$ 30,000.00$ |  |
|  | $\$ 3,753.21$ |  |

The addtional three years annuity with a FV of $\$ 3,753.21$ would be met by equal instalments of $\$ 1,133.91$.

Answer is (c)

## Part II Investment Basics

## BONDS AND GOVERNMENT SECURITIES

## 1. $\quad$ Answer $=(\mathbf{c})$

2. $\quad$ Answer $=(e)$
3. $\quad$ Answer $=(\mathbf{a})$
4. The accounts are audited by the company's auditors. The investment bank will do all the other things. Note that the lawyers referred to in (b) will be lawyers to the issue - the company may well want to retain separate legal advice.

## Answer is (d)

5. 6-month Bill at issue is 182-day Bill

Price $\quad=\quad 100-\left(5.20 \times \frac{182}{360}\right)=97.3711111111$
$\begin{aligned} \text { Money Market Yield } & =\left\{\frac{100}{97.3711111111}-1\right\} \times \frac{360}{182} \times 100 \\ & =5.34 \%\end{aligned}$
Answer = (d)
6. After 60 days Bill will be a 122-day Bill

Price $\quad=\quad 100-\left(5.00 \times \frac{122}{360}\right)=98.305555556$
Holding Period Yield $=\left\{\frac{98.30555555556}{97.3711111111}-1\right\} \times \frac{360}{60} \times 100$

$$
=\quad 5.76 \%
$$

## Answer = (b)

7. Calculate the terminal wealth of the CD:

Terminal Value $=\$ 1,000,000\left\{1+\left(0.06 \times \frac{180}{360}\right)\right\}=\$ 1,030,000$
Then calculate the CD's value as an 80 days CD at a yield of $5.50 \%$
Value

$$
=\frac{\$ 1,030,000}{\left(1+\left\{0.0550 \times \frac{80}{360}\right\}\right)}=\$ 1,022,050.72
$$

Finally, Calculate the CD's value as a 50 days CD at a yield of $5.60 \%$

Value

$$
=\frac{\$ 1,030,000}{\left(1+\left\{0.0560 \times \frac{50}{360}\right\}\right)}=\$ 1,022,050.72
$$

Now we can calculate the 30 days return on a 365 days basis:

$$
\frac{\{\$ 1,022,050.72-\$ 1,017,563.12\}}{\$ 1,017,563.12} \times \frac{365}{30} \times 100=5.37 \%
$$

## Answer = (b)

8. First we calculate the current price of the Treasury Bill

PRICE $=100-\left[4.5 \times \frac{180}{360}\right]=97.75$
The interest cost over the 40 days will be

$$
97.75 \times 0.0475 \times \frac{40}{360}=0.5159
$$

Hence we would need to sell the Bill at a price of 98.2659

The equivalent discount rate would be
$(100-98.2659) \times \frac{360}{140}=4.46 \%$

Answer = (c)
9. $\quad$ Answer $=(b)$

## Part II Bonds and Fixed Income

## BOND STRATEGIES

1. 



Money market yield on T-Bill.

$$
\begin{aligned}
\text { Price of T-bill } & =100-\left[5.75 \times \frac{273}{360}\right] \\
& =95.639583 \\
\text { Money Market Yield } & =\left[\frac{100}{95.639583}-1\right] \times \frac{360}{273} \\
& =6.012155 \%
\end{aligned}
$$

Terminal Value of T-Bond $=4\left[1+R \% x \frac{182}{360}\right]+104$
Price $=101.625 \quad$ Accrued $=2.0109$
Dirty Price $=103.6359$
Hence to breakeven with T-Bill

$$
\begin{aligned}
& (103.6359)\left[1+0.06012155 X \frac{273}{360}\right]=4\left[1+R \% \times \frac{182}{360}\right]+104 \\
& \mathrm{R}=\underline{17.85 \%}
\end{aligned}
$$

2. First we calculate the zero yields

6-month zero $100.50=\frac{103}{1+\mathrm{R}_{1}}$
$\mathrm{R}_{1}=2.4876 \%$
12-month zero $105.28125=\frac{5.5}{1.024876}+\frac{105.5}{\left(1+\mathrm{R}_{2}\right)}$
$\mathrm{R}_{2}=\quad=\quad 2.7570 \%$
Coupon yield is calculated as
$100=\frac{\mathrm{C}}{1.024876}+\frac{(100+\mathrm{C})}{(1.02757)^{2}}$
C $=2.7533 \% \times 2$
Annual Coupon $=\underline{5.5067 \%}=5.51 \%$
Answer = (c)
3. Firstly we must calculate the price of the Treasury Bond

Price $=\frac{2.5}{1.03}+\frac{2.5}{(1.03)^{2}}+\frac{2.5}{(1.03)^{3}}+\frac{102.5}{(1.03)^{4}}=98.142$
Secondly, we calculate the duration of the bond:
Duration $=\frac{\frac{2.5}{1.03}+\frac{2.5(2)}{(1.03)^{2}}+\frac{2.5(3)}{(1.03)^{3}}+\frac{102.5(4)}{(1.03)^{4}}}{98.141}=3.854$ Half Years
Thirdly, we use the duration number to calculate the expected price change for a 100 basis points change in yield:

Expected Change $=\frac{98.141 \times 3.854 \times 0.0050}{1.03}=1.836$
Finally we re-calculate the exact price of the bond using a yield of 7.00\%
Price $\quad=\quad \frac{2.5}{1.035}+\frac{2.5}{(1.035)^{2}}+\frac{2.5}{(1.035)^{3}}+\frac{102.5}{(1.035)^{4}}=96.327$

Actual Price Change is: $98.141-96.327=1.814$

Answer = (a)
4. The Hedge Ratio is obtained from:

$$
\operatorname{HR}=\frac{\underline{\mathrm{P}}_{1}}{\mathrm{P}_{2}} \quad \mathrm{x} \quad \underline{\mathrm{D}}_{1} \quad \mathrm{x} \quad \frac{\left(1+\mathrm{Y}_{2}\right)}{\mathrm{D}_{2}} \quad \mathrm{x} \quad \frac{\text { Change in } \mathrm{Y}_{1}}{\left(1+\mathrm{Y}_{1}\right)} \quad \mathrm{x} \quad \mathrm{Ch}^{1}
$$

Assuming equal absolute changes in yield on both bonds we have:

$$
\mathrm{HR}=\frac{\underline{98.00} \mathrm{x}}{105.00} \quad \underline{5.0} \quad \underset{4.0}{\mathrm{x}} \quad \underline{1.065} 1.064=1.1678
$$

You would therefore require $\$ 10,000,000(1.1678)$ or $\$ 11,678,000$ nominal of the second bond as a hedge.

Answer = (d)
5. Using the HP17B Bond program gives a yield to maturity for a 10-year TBond maturing on March 222013 with settlement on March 222003 as 7.5038\%.

The true annual yield is therefore:

$$
\begin{array}{ll}
(1+\mathrm{R}) & =\left(1+\frac{0.075038}{2}\right)^{2} \\
\mathrm{R} & =7.6446 \%
\end{array}
$$

The price of the zero must be:

$$
\begin{array}{ll}
\mathrm{P} & =\frac{100}{(1.07446)^{10}} \\
\mathrm{P} & =47.87
\end{array}
$$

$\underline{\text { Answer }=(\mathrm{d})}$
6. First we work out the price changes per 100 nominal using the usual equation:

Price x Duration $\mathrm{x} \frac{\text { Basis Point }}{1+\text { Yield }}$
Bond $102 \times 6 \times \frac{0.0001}{1.0675}=0.05733$
Hedge $95 \times 7 \times \frac{0.0001}{1.068}=0.06227$
Hence hedge amount will be

$$
\$ 10,000,000 \times \frac{0.05733}{0.06227}=\$ 9,206,681
$$

or $\$ 9,207,000$ rounded

## Answer is (e)

7. First we must calculate the zero coupon interest rates by bootstrapping.

$$
\begin{aligned}
100 & =\frac{108}{1+\mathrm{R}_{1}} \quad \mathrm{R}_{1}=8 \% \\
98.30 & =\frac{7.5}{1.08}+\frac{107.5}{\left(1+\mathrm{R}_{2}\right)^{2}} \quad \mathrm{R}_{2} \quad=\quad 8.48 \% \\
97.00 & =\frac{7.25}{1.08}+\frac{7.25}{(1.0848)^{2}}+\frac{107.25}{\left(1+\mathrm{R}_{3}\right)^{3}} \quad \mathrm{R}_{3}=8.43 \%
\end{aligned}
$$

Now we use these zero rates to calculate the fair value of the $9 \% 3$ year bond

$$
\begin{aligned}
\text { PRICE } & =\frac{9}{(1.08)}+\frac{9}{(1.0848)^{2}}+\frac{109}{(1.0843)^{3}} \\
& =\underline{101.48}
\end{aligned}
$$

## Answer is (c)

8. Step 1 Work out yield to maturity on bond with HP17B

| Type | $30 / 360$ Annual |
| :--- | :--- |
| Settlement | $30 / 9 / 00$ |
| Maturity | $30 / 9 / 04$ |


| Coupon | $6 \%$ |  |
| :--- | :--- | :--- |
| Call | 100 |  |
| Price | 98 |  |
|  |  |  |
| Gives yield | $=$ | $6.585 \%$ |

Step 2 Calculate bond's duration

$$
\begin{aligned}
\mathrm{D}= & \frac{\frac{6}{1.06585}+\frac{6(2)}{(1.06585)^{2}}+\frac{6(3)}{(1.06585)^{3}}+\frac{106(4)}{(1.06585)^{4}}}{98} \\
& =3.6693
\end{aligned}
$$

Step 3 Calculate duration implied price change for yield reduction of 1\%

$$
\begin{aligned}
\Delta \mathrm{P} & =-3.6693 \times 98 \times\left(\frac{-0.01}{1.06585}\right) \\
& =3.3738
\end{aligned}
$$

Step 4 Calculate actual price change for yield reduction of $1 \%$ using HP17B

| Yield $=5.5$ | 5.585\% |  |
| :---: | :---: | :---: |
| Gives |  |  |
| Price $=10$ | 101.4517 |  |
| PRICE CHANGE | = | 101.4517-98 |
|  | = | 3.4517 |


| Hence DURATION CHANGE | $=$ | 3.3738 |
| :---: | :--- | :--- |
| CONVEXITY CHANGE | $=$ | 0.0779 |
| TOTAL CHANGE | $=$ | 3.4517 |

## Answer is (b)

9. First we must calculate the zero coupon interest rates by bootstrapping.
$100=\frac{108}{1+\mathrm{R}_{1}} \quad \mathrm{R}_{1} \quad=\quad 8 \%$

$$
\begin{aligned}
& 98.30=\frac{7.5}{1.08}+\frac{107.5}{\left(1+\mathrm{R}_{2}\right)^{2}} \quad \mathrm{R}_{2} \quad=8.4768 \% \\
& 97.00=\frac{7.25}{1.08}+\frac{7.25}{(1.084768)^{2}}+\frac{107.25}{\left(1+\mathrm{R}_{3}\right)^{3}} \quad \mathrm{R}_{3}=8.4316 \%
\end{aligned}
$$

Now we use these zero rates to calculate the fair value of the $9 \% 3$ year bond

$$
\begin{aligned}
\text { PRICE } & =\frac{9}{(1.08)}+\frac{9}{(1.084768)^{2}}+\frac{109}{(1.084316)^{3}} \\
& =\underline{\underline{101.48}}
\end{aligned}
$$

## Answer is (c)

## 10. Answer is (a)

11. Assuming even yield, etc., as above, the bond with the call disadvantages the investor compared to the bond with no embedded options, while those with the puts give the investor an advantage compared to the bond with no embedded options.

## Answer is (b)

12. The first step is clearly to calculate the zero coupon interest rates by bootstrapping. To keep things simple, we assume equal 6 -month periods.
$100.50=\frac{100+3.5}{1+R_{1 / 2}} \quad R_{1}=\underline{5.97 \%}$
$99.53125=\frac{3}{1+\left(\frac{0.0597}{2}\right)}+\frac{(100+3)}{\left(1+R_{2 / 2}\right)^{2}}$

$$
R_{2}=\underline{6.50 \%}
$$

$104.1875=$

$$
\frac{5}{1+\left(\frac{0.0597}{2}\right)}+\frac{5}{\left[1+\left(\frac{0.065}{2}\right)\right]^{2}}+\frac{(100+5)}{\left(1+\frac{R_{3}}{2}\right)^{3}}
$$

$$
R_{3}=\underline{7.045 \%}
$$

Then we can calculate the price of an eighteen month zero coupon bond by:

$$
\mathrm{P}=\frac{100}{\left[1+\left(\frac{0.07045}{2}\right)\right]^{3}}=90.1354=90-04
$$

## Answer is (b)

13. First we need to calculate the market price of the bond. Using a bond calculator with a 30/360 annual basis, I get a price of 101.7526.

We then calculate the PV of the cash flows

$$
\begin{aligned}
& \frac{6}{1.055}=5.6872 \\
& \frac{6}{(1.055)^{2}}=5.3907 \\
& \frac{6}{(1.055)^{3}}=5.1097 \\
& \frac{106}{(1.055)^{4}}=85.5650
\end{aligned}
$$

Now we calculate the duration from

$$
\begin{aligned}
D & =\frac{5.6872(1)+5.3907(2)+5.1097(3)+85.5650(4)}{101.7526} \\
& =\underline{\underline{3.676}} \text { years }
\end{aligned}
$$

Answer is (d)

## Part III Equities

## EQUITIES: ANALYSIS AND VALUATION

## 1. Answer is (d)

2. Since the historic P/E ratio is 10.0 , the last dividend payment was 20 p and the payout ratio is $40 \%$, we can determine the current stock price:

$$
P_{0}=20 p(10)\left\{\frac{1}{\{0.40\}}\right\}=500 p
$$

Using Gordon’s Growth Model to determine the expected return on the stock:

$$
\begin{aligned}
& \mathrm{R}=\frac{\mathrm{D}_{1}}{\mathrm{P}_{0}}+\mathrm{G} \\
& \mathrm{R}=\frac{20(1.12)}{500}+0.12=16.48 \%
\end{aligned}
$$

The incremental return over the Risk-Free rate is therefore 8.48\%

## Answer = (d)

3. If last dividend was 30P and dividend payout ratio is $30 \%$, most recent earnings were 100P.

Given a P/E ratio of 20 the current price is evidently 2000P.
We know expected return on equity from Gordon Model is sum of dividend yield in period 1 and growth rate.

$$
R=\frac{30(1.12)}{2000}+0.12=0.1368 \quad(\text { or } 13.68 \%)
$$

Hence the premium over the riskless rate of $6 \%$ is $7.68 \%$.

## Answer is (e)

4. Remember we have the usual dividend valuation model
$\mathrm{P}_{0}=\frac{\mathrm{D}_{1}}{1.14}+\frac{\left(\mathrm{D}_{2}+\mathrm{P}_{2}\right)}{(1.14)^{2}}$

$$
\begin{aligned}
& \mathrm{P}_{0}=45 \begin{array}{l}
\mathrm{D}_{1}=2.5(1.08)=2.70 \\
\mathrm{D}_{2}=2.5(1.08)^{2}=2.916 \\
(1.14)^{2}
\end{array}=45-\frac{2.70}{(1.14)}-\frac{2.916}{(1.14)^{2}} \\
& \mathrm{P}_{2} \\
& \mathrm{P}_{2}=04(1.14)^{2}-2.70(1.14)-2.916 \\
& =5 \underline{52.488}
\end{aligned}
$$

We can check this by calculating

$$
\begin{aligned}
\mathrm{P}_{2} & =\frac{\mathrm{D}_{3}}{\mathrm{R}-\mathrm{g}}=\frac{2.5(1.08)^{3}}{0.14-0.08} \\
& =\underline{52.488}
\end{aligned}
$$

And rounded to the nearest quarter the share price will be $\$ 52.50$
Answer = (d)
5.

| $\frac{\mathrm{P}_{0}}{\mathrm{E}_{0}}$ | $=15$ |
| :--- | :--- |
| $\mathrm{D}_{1}$ | $=10 \mathrm{p}$ |
| $\frac{\mathrm{D}_{1}}{\mathrm{E}_{1}}$ | $=50 \%$ |
| $\mathrm{E}_{1}$ | $=20 \mathrm{p}$ |
| $\mathrm{E}_{0}$ | $=20 \mathrm{p} / 1.07=18.69 \mathrm{p}$ |
| $\mathrm{P}_{0}$ | $=15 \times 18.69=280.35 \mathrm{p}$ |

Formula for Gordon's growth model
$P_{0} \quad=\quad \frac{D_{1}}{R-G}$
$280.35=\frac{10}{\mathrm{R}-0.07}$
$\mathrm{R} \quad=\quad 10.57 \%$

Answer is (c)
6. Answer is (d)

## Part III Equities

## PORTFOLIO THEORY

## 1. Answer is (a)

2. This is given as follows:

$$
\begin{aligned}
& S^{2}=(0.5)^{2}(28)^{2}+(0.5)^{2}(35)^{2}+2(0.5)(0.5) 196=600.25 \\
& S=24.50 \%
\end{aligned}
$$

3. For a perfectly negatively correlated security, we can write

$$
\mathrm{S}^{2}=\left(\mathrm{W}_{1}\right)^{2}\left(\mathrm{~S}_{1}\right)^{2}+\left(\mathrm{W}_{2}\right)^{2}\left(\mathrm{~S}_{2}\right)^{2}-2\left(\mathrm{~W}_{1}\right)\left(\mathrm{W}_{2}\right)\left(\mathrm{S}_{1}\right)\left(\mathrm{S}_{2}\right)
$$

Setting this $=0$ for a risk-free portfolio and recognising that the above equation is a perfect square of $\left(\mathrm{W}_{1} \mathrm{~S}_{1}-\mathrm{W}_{2} \mathrm{~S}_{2}\right)$, we can write
$0=\mathrm{W}_{1} \mathrm{~S}_{1}-\mathrm{W}_{2} \mathrm{~S}_{2}$ or $\mathrm{W}_{1} / \mathrm{W} 2=\mathrm{S}_{2} / \mathrm{S}_{1}$
Substituting, $\mathrm{S}_{1}=10$ and $\mathrm{S}_{2}=20$ gives $\mathrm{W}_{1}: \mathrm{W}_{2}=2: 1$
Answer is (c)

## Part III Equities

## THE CAPITAL ASSET PRICING MODEL

## 1. Answer is (c)

2. If the stock has an alpha of $1 \%$, it is expected to outperform its CAPM return of $6 \%+$ (expected return on market $-6 \%$ ) x 2.0. So, $20 \%=1 \%+6 \%$ $+2(\mathrm{E}(\mathrm{Rm})-6 \%)$. Solving, gives $\mathrm{E}(\mathrm{Rm})=12.5 \%$.

## Answer is (c)

3. Using the CAPM, gives E (R ) $=8 \%+2(15 \%-8 \%)=22 \%$. Using the Gordon Growth Model with $\mathrm{g}=5 \%$ and $\mathrm{D} 1 / \mathrm{P} 0=5 \%$, gives an expected return of $10 \%$. Comparing with $22 \%$ gives an overvaluation using the CAPM of 12\%.

## Answer = (a)

4. Answer is (d)
5. An increased use of equity versus debt will decrease the leverage of the Company. Hence it will do better in bad markets but not so well in good markets.

## Answer is (d)

## Part IV Risk Management Products

## FUTURES

1. Remember that the gross basis is simply found from

BOND PRICE - [FUTURES PRICE x CONVERSION FACTOR]
$=124.28125-[109 \times 1.13]=1.11125$
$1.11125 \times 32=35.6$ 32nds

## Answer is (d)

2. We simply take the dividend yield and interest rate into account

$$
\begin{aligned}
F & =S(1+(R-D) T) \\
& =1200\left[1+(0.06-0.025)\left(\frac{90}{360}\right)\right] \\
& =1210.5
\end{aligned}
$$

Answer is (d)

## Part IV Risk Management Products

## SWAPS (PART OF FUTURES CHAPTER)

1. Obviously candidates need to check the arrows for each of the positions. For (a) we have:


NET IS PAY FIXED EURO, RECEIVE FLOATING USD. THIS IS CORRECT. ALL THE OTHER COMBINATIONS GIVE THE WRONG RESULT.

Answer is (a)
2. 1. If we receive fixed on a swap, we pay the floating;
2. If we own a floating rate note, we receive the floating;

Therefore, the net effect of receiving fixed on a swap and owning a floating rate note is to receive fixed on an asset package, which is the equivalent of owning a bond.

Answer is (a)
3. We can see the net saving by drawing the swap box diagram:


Net cost to XYZ is:

1. Negative Libor +40 bps
2. Positive Libor +5 bps

## 3. Negative 7\% Fixed <br> Net: 7.35\%

When compared to a fixed funding rate of $7.50 \%$ this is a saving of 15 bps .
Answer = (c)
4. The six month period October 1, 2001 through April 1, 2002 is 182 days.

| LIBOR Payment | $=$ | $-\$ 100,000,000 \times 0.05 \times 182$ |
| :--- | :--- | :--- |
|  | $=$ | $-\$ 2,527,777,78$ |
| Dividend | $=$ | $\$ 100,000,000 \times 0.015 \times 182$ |
|  | $=\$ 758,333.33$ |  |
|  |  |  |
| Capital Gain | $=\$ 100,000,000100$ |  |
|  |  |  |
|  |  | $\$ 8,333,333.33$ |

Net Payment $=\quad+\$ 6,563,889$
Answer = (c)
5.


The net cost of fixed rate funding for XYZ is
$10 \%-($ LIBOR -0.20$)+$ LIBOR +0.50$)$
$=-\underline{-10.70 \%}$
When compared to XYZ's usual fixed rate funding of $11 \%$ this represents a saving of 30 basis points

Answer = (a)
6. The question is the same as asking what would be the par yield on a three period bond given the specific zero curve.

Hence we have to find R in the following
$100=\frac{\mathrm{R}}{1.05}+\frac{\mathrm{R}}{(1.0525)^{2}}+\frac{\mathrm{R}}{(1.055)^{3}}+\frac{100}{(1.055)^{3}}$
$\mathrm{R}=5.48$
Hence the 3-period swap rate on the fixed side is 5.48\%

## Answer is (b)

7. Here we use simple bootstrapping to find the 3-year spot rate.

## ONE YEAR

$100=\frac{100}{1.05}$

## TWO YEAR

$100=\frac{5.25}{1.05}+\frac{105.25}{\left(1+\mathrm{R}_{2}\right)^{2}}$
$R_{2}=5.256579 \%$

THREE YEAR
$100=\frac{5.5}{1.05}+\frac{5.5}{(1.05256579)^{2}}+\frac{105.5}{\left(1+\mathrm{R}_{3}\right)^{3}}$
$R_{3}=\underline{\underline{5.51867 \%}}$

ANSWER IS (c)
8. First we estimate the one, two and three year discount factors:

$$
\begin{aligned}
& \frac{1}{1.10}=0.90909091 \\
& \frac{1}{(1.10)(1.11)}=0.81900082 \\
& \frac{1}{(1.10)(1.11)(1.1225)}=0.72962211
\end{aligned}
$$

Then we can find the three year per swap rate by finding the coupon yield on a three year bond priced at par.
$100=\mathrm{C}(0.90909091)+\mathrm{C}(0.81900082)+\mathrm{C}(0.72962211)+100(0.72962211)$
$C=11.001194 \%$

## ANSWER IS (b)

## Part IV Risk Management Products

## OPTIONS

## 1. Answer is (d)

2. We simply remember that the expected drift of the stock in a simple BlackScholes model, with a continuous dividend yield, is given by

## $\begin{gathered}\text { INTEREST } \\ \text { RATE }\end{gathered}-\begin{gathered}\text { DIVIDEND } \\ \text { YIELD }\end{gathered} \quad-\frac{(\text { VOLATILITY })^{2}}{2}$

In this case over one year we have

$$
(0.06)-(0.02)-\frac{(0.20)^{2}}{2}=0.02
$$

Hence the stock price is expected to drift up at $2 \%$ per annum.

## Answer is (b)

3. Remember the probability of exercise in the Black-Scholes model for a put option is $\mathrm{N}\left(-\mathrm{d}_{2}\right)$
$d_{2}=\frac{L N(S / x)+\left[(r-d)-\sigma^{2} / 2\right] T}{\sigma \sqrt{T}}$
$=\frac{\mathrm{LN}(100 / 100)+\left[(0.05-0.02)-\frac{(0.20)^{2}}{2}\right] 0.25}{0.20 \sqrt{0.25}}$
$=0.025$
$\mathrm{N}(-0.025)$ is, from the normal distribution tables provided, 0.4900 . Hence there is a $49 \%$ chance that this option will be exercised.

## Answer is (b)

4. The first thing we need to do is work out the probability of an up step and a down step.
$P(103.75)+(1-P)(98.75)=100(1.0125)$
$\mathrm{P}=0.50$
$(1-\mathrm{P})=0.50$

We can construct the price tree:


Now we value the put in period 1 on the up step and the down step.

UPSTEP

$$
\mathrm{P}=\frac{0.50(0.046875)+.050(0)}{1.0125}=0.02315
$$

DOWNSTEP

$$
\mathrm{P}=\frac{0.50(4.984375)+0.50(0.046875)}{1.0125}=2.48457
$$

Note that 2.48457 is well below the intrinsic value along the down step of ( $102.50-98.75$ ) or 3.75 . Hence we substitute this value to find the option price at period 0 .

$$
P=\frac{0.50(0.02315)+0.50(3.75)}{1.0125}=1.86328
$$

Since this is less than the intrinsic value at period 0 of 2.50 , the value of the option is 2.50 .

Answer is (d)
5. This is a simple application of put-call parity

$$
\begin{aligned}
& \mathrm{C}-\mathrm{P}=\frac{\mathrm{F}-\mathrm{K}}{1+\mathrm{RT}} \\
& \text { or } \mathrm{C}-\mathrm{P}=\frac{\mathrm{S}-\mathrm{K}}{1+\mathrm{RT}} \\
& \text { so } \mathrm{P}=\mathrm{C}-\mathrm{S}+\frac{\mathrm{K}}{1+\mathrm{RT}} \\
& \qquad=2-100+\frac{105}{1.0125}=\underline{\underline{5.7037}}
\end{aligned}
$$

Answer is (c)

## $\underline{\text { Part V Institutions and International Investment }}$

## INTERNATIONAL INVESTMENT

1. The equilibrium forward rate (FR) is simply the rate that prevents arbitrage. But remember that Sterling money markets operate on a 365 day year and US Dollar rates on a 360 day year.

Therefore we have:

$$
\begin{aligned}
& \left\{1+\left(0.06 \times \frac{91}{365}\right)\right\}=1.5500\left\{1+\left(0.0525 \times \frac{91}{360}\right) \frac{1}{\mathrm{FR}}\right\} \\
& \mathrm{FR}=1.5500 \times \frac{\left\{1+\left(0.0525 \times \frac{91}{360}\right)\right\}}{\left\{1+\left(0.06 \times \frac{91}{365}\right)\right\}}=1.5474
\end{aligned}
$$

## Answer = (d)

2. $\quad$ Answer $=(\mathbf{d})$

Standard role of economic or operating exposure
3. We can calculate the forward rate in the usual manner.
$\$ 1.5250 \frac{\left[1+\left(0.075 \times \frac{90}{360}\right)\right]}{\left[1+\left(0.065 \times \frac{90}{365}\right)\right]}=\quad$ FORWARD RATE

$$
\mathrm{F}=\$ 1.5291
$$

## Answer is (e)

4. Answer is (e)
5. The bank will:
6. Borrow USD 1.5250 at $7.50 \%$ for 90 days $=$ USD $1.525\left(1+\left[0.075 \times \frac{90}{360}\right]\right)=$ USD 1.5536
7. Sell USD 1.5250 for GBP 1 Spot Value
8. Invest GBP 1 at $6.50 \%$ for 90 days $=1+\left(0.065 \times \frac{90}{365}\right)=$ GBP1.0160

Therefore in 90 days:
GBP 1.0160 = USD 1.5536
GBP 1 = USD 1.5536 / 1.0160 = $\underline{\text { USD } 1.5291}$
Note that USD are 360 day base whilst GBP are 365 day base.

## Answer is (e)

6. The bank will work through the USD to achieve the quote:
7. The bank will buy CHF and sell USD at 1.4130
8. The bank will sell GBP and buy USD at 1.5860

Therefore if USD 1 = CHF 1.4130
And GBP 1 = USD 1.5860
Then GBP 1 must be the equivalent of : CHF $1.4130 \times$ USD 1.5860
$=\underline{\text { CHF } 2.2410}$

## Answer is (d)

7. We use the usual FRA payment formula

PAYMENT $=\frac{[\mathrm{R}-0.07] \$ 100,000,000[\mathrm{~N} / 360]}{1+\mathrm{R} / 360}$
The number of days between July 15, and October 15, is 92 days.

$$
\begin{aligned}
\text { PAYMENT } & =\frac{[0.085-0.07] \$ 100,000,000[92 / 360]}{\left[1+\left(0.085 \times \frac{92}{360}\right)\right]} \\
& =\$ 375,184
\end{aligned}
$$

## Answer is (d)

8. If the company has to go through the dollar FX market, then he will rationally buy dollars for Swiss Francs and sell dollars for Sterling.

He will pay CHF 1.4130 for his dollars and pay $\$ 1.5860$ for his Sterling. Hence, the effective CHF/Sterling rate will be

CHF (1.4130) (1.5860) per $£$ or CHF 2.2410

## Answer $=(\mathbf{d})$

9. We can calculate the forward rate in the usual manner.
$\$ 1.5250 \frac{\left[1+\left(0.075 \times \frac{90}{360}\right)\right]}{\left[1+\left(0.065 \times \frac{90}{365}\right)\right]}=\quad$ FORWARD RATE
$\mathrm{F}=\$ 1.5291$
Answer = (e)
10. We work out the rate at which pounds can be offered in three months for dollars to avoid an arbitrage.

Borrow dollars 3-months
Sell dollars for sterling spot
Invest sterling 3-months
At what rate sell sterling for dollars in 3-months to breakeven

$$
\begin{aligned}
& \begin{array}{l}
\begin{array}{l}
\text { Borrow } \$ \text { at } 41 / 8 \% \\
\text { Sell } \$ \text { at } 1.9010 \\
\text { Invest } £ \text { at } 10 \%
\end{array} \\
\\
\frac{1}{1.9010}\left[1+0.10 \frac{92}{365}\right] X \text { Forward Rate } \\
\\
=\left[1+0.04125 \times \frac{92}{360}\right] \\
\mathrm{F}= \\
\\
\\
\\
\\
\\
\end{array} .965 \text { day year year } \\
& {\left[1+0.010 \times \frac{\left[1+0.04125 X \frac{92}{360}\right]}{365}\right]}
\end{aligned}
$$

## Answer = (d)

11. $\quad$ Answer $=(\mathbf{d})$

## Part VI Strategies and Issues

INVESTMENT OBJECTIVES, STRATEGIES AND ISSUES

1. $\quad$ Answer $=(\mathbf{d})$
