

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BEL, BEX	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX 651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.



1. a) What is periodic and aperiodic signal? Find the necessary condition for the signal $x[n] = \cos(2\pi f_0 n + \theta)$ to be periodic. [2+2]
 - b) Determine whether the given signal is energy signal or power signal. $x(t) = e^{-at}$, $a > 0$ [4]
 2. a) Derive an analysis equation of continuous time Fourier series representation of any signal $x(t)$. [5]
 - b) Describe the time shifting and frequency shifting properties of continuous time Fourier series. Find Fourier series coefficient of signal $x(t) = A \cos(\omega t)$. [6]
 - c) State and prove Parseval's relation for continuous time periodic signals. [4]
 3. a) Find the Fourier transform of the signal $x(t) = e^{-at}$, $a > 0$ and also plot the frequency spectrum. [5]
 - b) Find the Fourier transform of the given signal. [4]
- $$x[n] = 1 \text{ for } -N_1 \leq n \leq N_1$$
- $$= 0 \text{ elsewhere}$$
- c) Show that the convolution in the time domain results multiplication in frequency domain using discrete time Fourier transform. [4]
 4. a) State and prove conjugate and frequency shifting properties of discrete time Fourier transform. [4]
 - b) Derive the convolution integral for continuous time system signal. [6]
 5. a) Define linear time invariant system. Explain causality and time variance properties of continuous time system. [4]
 - b) Find the output of the LTI system with impulse response $h[n] = 2^n \{u[n] - u[n-3]\}$ and $x[n] = \delta[n] + \delta[n-1] + \delta[n-3]$. Also verify the answer. [6]
 6. a) Define frequency response of the discrete LTI system. Derive Formula to calculate the impulse response of continuous time ideal low pass filter. [2+4]
 - b) Find the convolution between signals $x[n] = \{1, 2, 2, 1\}$ and $h[n] = \{1, 2, 2, -1\}$. Choose your own origin. [6]
 7. a) Define sampling theorem. Determine the Nyquist rate and Nyquist interval for the given continuous time signal. [2+4]

$$x(t) = \frac{1}{2\pi} \cos(4000\pi t) \cos(1000\pi t)$$

- b) Find impulse response for the DT system given by the following linear constant coefficient difference equation. $y[n] - \frac{3}{4}y[n-1] + \frac{1}{8}y[n-2] = 2x[n]$ [6]

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Exam.	Back	
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Subject: - Signal Analysis (EX 651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
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1. a) Define even and odd signal with necessary diagram. Check whether the following signal is energy or power signal. (i) $x(t) = 5A \cos(\omega t + \phi)$ (ii) $x[n] = \sin\left(\frac{n}{4}\right)$ [3+4]
 - b) Prove that discrete time complex exponential is periodic if its frequency is rational. [4]
2. a) Derive the exponential form of the Fourier series of a continuous-time signal. [6]
 - b) Find and plot the Fourier series coefficients for the following signal with period N. [5]

$$x[n] = 1 + \sin\left(\frac{2\pi}{N}n\right) + 3\cos\left(\frac{2\pi}{N}n\right) + \cos\left(\frac{4\pi}{N}n + \frac{\pi}{2}\right)$$
 - c) State and prove Parseval's relation for Discrete Time Fourier Series. [3]
3. a) Find the Fourier transform of signal $x[n] = a^n u(n)$, $0 < a < 1$ [6]
 - b) Derive and explain the expression of energy density spectrum for a continuous time aperiodic signal. [6]
4. a) Derive Fourier transform pair equations of a discrete-time signal. [6]
 - b) List out the properties of Discrete Time Fourier Transform. State and prove the convolution property of Discrete Time Fourier Transform. [6]
5. a) State and prove the sampling theorem. Find the Nyquist rate and Nyquist interval for the signal [3+3]

$$x(t) = (1/2\pi) \cos(4000\pi t) \cos(1000\pi t)$$
 - b) Derive the transfer function of a RC low pass filter and plot the magnitude and phase. [5]
6. a) Find the output $y(t)$ of LTI system if the impulse response $h(t) = e^{-t}u(t - 3)$ and input $x(t) = u(t - 2)$. [5]
 - b) Describe the frequency response of a continuous time LTI system. [5]
7. a) Derive convolution sum of a discrete time signal. [5]
 - b) Find out the frequency response of the following signal [5]

$$y[n] = 0.5x[n] - 0.5x[n - 1]$$

$$h[n] = \frac{1}{2} \text{ for } n = 0 \text{ and } -\frac{1}{2} \text{ for } n = 1$$

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- ✓ Candidates are required to give their answers in their own words as far as practicable.
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1. a) Define energy signal and power signal. Determine whether the signal $x(t) = e^{-3t}$ is a power signal or energy signal or neither energy nor power signal. [3+3]
 b) Define continuous time unit step signal. Derive the necessary condition for the signal $x(t) = e^{j\omega t}$ to be periodic. [1+3]
2. a) Derive the trigonometric fourier series expansion of a continuous-time periodic signal $x(t)$. [5]
 b) State and prove the time-scaling property for continuous-time fourier series pair. [5]
 c) State and prove frequency shifting property of discrete time fourier series. [3]
3. a) Find the fourier transform of the signal $x(t) = e^{-at}$, $a > 0$ and also plot the frequency spectrum. [5]
 b) Show that the convolution in time domain results multiplication in frequency domain using continuous time fourier transform. [5]
4. Determine the discrete time fourier transform of signum function ($\text{sgn}[n]$) and use it to find the DTFT of unit-step signal $u[n]$. [6+6]
5. a) State and prove the linearity and time shifting properties of DTFT [6]
 b) Define sampling theorem and Nyquist criteria for sampling. Find the Nyquist rate for the signal: $x(t) = 20 \sin(500\pi t) + 10 \cos(300\pi t) - 50 \cos(1000\pi t)$ [3+3]
6. a) Derive convolution integral for continuous LTI system. [5]
 b) Find convolution between the signals $x[n] = \{3, 5, 6, 9\}$ and $h[n] = \{-1, 3, 5\}$. Choose your appropriate origin. Show the output signal. [6]
7. a) Derive the expression for impulse response of RC filter and plot the magnitude and phase response. [6]
 b) Find the frequency response ($e^{j\omega}$), plot the magnitude and impulse response $h[n]$ for a system characterized by linear constant coefficient difference equation

$$y[n] = 0.5y[n-1] + x[n] \quad [6]$$

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1. a) Define energy and power signal. State whether the given signal is periodic or not? If signal is periodic, find its fundamental period. $x[n] = \cos(\frac{\pi n}{5})\sin(\frac{\pi n}{3})$ [6]
 b) Explain time shifting, time scaling and time inversion of a continuous time signal with example. [3]
2. a) What is Fourier series representation of a signal? Derive an expression for analysis and synthesis equation of the Fourier Series for a CT periodic signal $x(t)$. [6]
 b) Consider a Signal $x[n] = \sin(\omega_0 n)$ with period $N = 6$. Find the Fourier series coefficient of the given signal $x[n]$. Plot spectra. Also find the average power. [6]
3. a) Derive Fourier Transform of discrete time aperiodic signal. Also, prove that DTFT is periodic with 2π . [4+2]
 b) State and prove that convolution in time domain is equivalent to multiplication in frequency domain. [5]
4. a) Explain duality property of continuous time Fourier transform with derivation. [1.5+3.5]
 b) Find the Fourier transform of the signal $(t) = e^{-at}\cos\omega_0(t)$, $a > 0$. [5]
5. Find: a) Inverse Fourier Transform of CT unit impulse signal $\delta(\omega)$ [2]
 b) Fourier Transform of DT signal $\cos\omega_0(n)$ [4]
 c) Show that the multiplication of a signal $x(t)$ by t is equivalent to differentiation of its Fourier Transform. [4]
6. Explain the Nyquist Criteria for sampling and aliasing effect. Find the Nyquist rate for the signal $x(t) = 30 \sin(100\pi t) + 40 \cos(400\pi t) \sin(300\pi t)$. [4+4]
7. a) Derive convolution sum for a LTI system. [6]
 b) Find the output of an LTI system, for input $x[n] = \left\{\frac{1}{4}, -1, 2\right\}$ and $h[n] = \left\{2, \frac{2}{4}, -2\right\}$. [6]
8. Find the frequency response and impulse response of the system characterized by linear constant coefficient difference equation $y[n] = 0.5y[n-1] + x[n]$. [8]

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1. Determine whether the signal $x(t) = e^{-3t}$ is a power signal or energy signal or neither energy nor power signal. [4]
2. Determine whether the signal $x[n] = 5 \sin\left[\frac{3\pi}{8}n - \frac{\pi}{2}\right] - 2 \cos\left[\frac{7\pi}{12}n\right]$ is periodic or not. If the signal is periodic, calculate its fundamental period and fundamental frequency. [4]
3. What are the significance of Fourier series coefficients of a signal? State and prove time scaling and conjugation properties of continuous time Fourier series representation. [2+6]
4. Find the Fourier series coefficient of the signal. [6]

$$X[n] = 1 + \sin\left[\left(\frac{2\pi}{N}\right)n\right] + 3 \cos\left[\left(\frac{2\pi}{N}\right)n\right] + \cos\left[\left(\frac{4\pi}{N}\right)n\right]$$
5. Explain the convolution properties of continuous time Fourier transform. [6]
6. State and prove Parseval's theorem for continuous time aperiodic signal. [2+6]
7. Find the Fourier transform of continuous time Rectangular Pulse and Constant amplitude A. State Prove Duality property of Continuous Time Fourier Transform with suitable example. [4+4]
8. Consider an analog signal $x(t) = 3 \cos 200 \pi t + 2 \sin 300 \pi t - 3 \cos 500 \pi t$. [8]
 - i) Determine the minimum sampling rate required to avoid aliasing.
 - ii) Suppose that the signal is to be sampled at the rate of $F_s = 400$ Hz. What is the discrete time signal obtained after sampling?
 - iii) Find reconstructed signal $x_r(t)$ from sampled signal calculated above in [ii].
9. a) Find the convolution between the signals [6]

$$x(t) = 1 \text{ for } -1 < t < 1$$

$$0 \text{ otherwise}$$
 and,
$$h(t) = 1 \text{ for } -1 < t < 1$$

$$0 \text{ otherwise}$$
 b) Evaluate the Step response of RC filter [5]
10. a) What is the condition for LTI system to be causal? [2]
- b) Determine if the following system is Linear [3]

$$y[n] = ax[n] + b$$
- c) Check if the system is time invariant [3]

$$y[n] = nx[n] - x[n-1]$$
11. a) Perform convolution sum of signal $x[n] = \{1, 2, 0, -1\}$ and $h[n] = \{2, 0, 2\}$ [6]
- b) Derive convolution sum equation for discrete time linear system. [3]

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1. a) Draw the following signal $x[n] = u[n+2] - u[n-3] + nu[n-3] - nu[n-6]$. [3]
 - b) Determine the period of $x[n] = \sum_{k=-\infty}^{\infty} (-1)^k \delta[n-k]$. [2]
 - c) For $x[n] = \{1, 2, 0, -2, 1\}$, find $x[2n-3]$. [3]
2. a) Derive the Trigonometric Fourier Series expansion of a continuous-time periodic signal $x(t)$. [5]
 - b) State and prove the time-scaling property for discrete-time Fourier series pair. [4]
 - c) Find the frequency domain representation (both magnitude and phase plot) of a periodic signal defined as $x[n] = \{1, -0.5, 0, 0, 0.5\}$, with period $N = 5$. [6]
3. a) Find the Fourier Transform of the signal $x(t) = e^{-at}$; $a > 0$ and also plot the frequency spectrum. [5]
 - b) Show that the convolution in time domain results multiplication in frequency domain using continuous time Fourier Transform. [5]
 - c) Determine the discrete time fourier transform of signum function ($\text{sgn}[n]$) and use it to find the DTFT of unit-step signal $u[n]$. [4+8]
4. Determine the 4-point DFT of the signal $x[n] = u[n] + u[n-1] - u[n-3] - u[n-4]$ using linear transformation method. [5]
5. What is aliasing and how can it be prevented? [6]
6. a) Find the convolution between the signals [8]

$$x(t) = \begin{cases} 1 & \text{for } -1 < t < 1 \\ 0 & \text{otherwise} \end{cases}$$

$$h(t) = \begin{cases} 1 & \text{for } -1 < t < 1 \\ 0 & \text{otherwise} \end{cases}$$
 - b) Evaluate the step response of RC filter. [5]
7. a) What is the condition for LTI system to be causal? [5]
 - b) Determine if the following system is Linear $y[n] = ax[n] + b$. [3]
 - c) Check if the system is time invariant $y[n] = nx[n] - x[n-1]$. [3]

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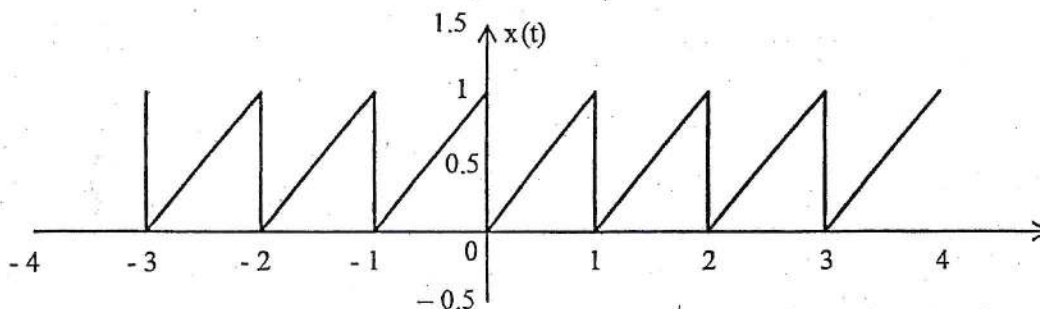
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1. a) Define energy and power signals with examples. [4]
- b) Derive the necessary condition for the signal $e^{j\omega n}$ to be periodic. [4]
2. a) Calculate and plot magnitude and phase spectrum of the following periodic signal. [8]



- b) State and prove Parseval's relation for discrete time periodic signals. [6]
3. State and prove the complex conjugation property for continuous time a periodic signals. Also show that if the CT signal is purely real, its Fourier Transform is conjugate symmetric. [4+4]
4. a) Find the Fourier Transform of discrete time signal $[n] = a^n u[n]$, $0 < a < 1$. [6]
- b) Compute the 4-point DFT for $x[n] = \{3, -2, 1\}$. [6]
5. State Nyquist's sampling theorem. Find the Nyquist rate for the given CT signal [2+4]

$$x(t) = \frac{1}{2\pi} \cos(50\pi t) \cos(500\pi t)$$

6. a) What is an LTI system? Find the output of the LTI system with impulse response $h(t) = e^{-2t} u(t)$ when the input to the system is $\begin{cases} 1; & |t| < 5 \\ 0; & \text{otherwise} \end{cases}$. [2+8]
- b) Show that ideal low pass filter is not practically realizable. [7]
7. Find and plot the convolution sum of the signals $x[n] = \{-0.5, 1, -1, 0.5\}$ and $y[n] = \{1, 2, -1, 0, 2, -1\}$. [8]
8. For a system characterized by linear constant coefficient difference equation $y[n] = 0.4 y[n-1] + x[n]$, find and plot the transfer function and impulse response of the system. [7]

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1. a) Differentiate between continuous time and discrete time signals with examples. [3]
- b) Determine the fundamental period and fundamental frequency of the periodic signal. [5]

$$x[n] = 3 \sin\left(\frac{7\pi}{9}n - 2\right) + \cos\left(\frac{\pi}{13}n + 2\right)$$

2. a) "Even if a signal is periodic, its Fourier series might not exist." Justify the statement using three different examples. [4]
- b) State and prove Parseval's relation for Discrete Time Fourier series. [6]
3. Derive expression for Fourier transform of continuous time periodic signal. Find Fourier transform of signal $x(t) = e^{-2|t|} \sin(t)$. [5+5]
4. a) State and prove convolution properties for continuous time Fourier Transform. [4]
- b) Compute discrete time Fourier transform of the discrete time signal [4]

$$x[n] = \left(\frac{1}{2}\right)^{n-1} u[n-1]$$

5. a) Derive the convolution sum. [4]
- b) Find the convolution between the following sequences. [6]

$h[n] = \{2, 1, 5, 7\}$
 $x[n] = \{1, 3, 5, 9, 6\}$
 Choose origin as per your choice.
6. a) What is impulse train sampling? How do you reconstruct original signal from its sample? [2+6]
- b) Derive and plot the impulse response and frequency response of a system characterized by the difference equation. [6]

$$y[n] + 0.55y[n-1] = x[n]$$

7. a) What do you mean by impulse response of a LTI system? Derive formula to calculate impulse response of continuous time ideal low pass filter. [6]
- b) If the impulse response of a discrete LTI system is $h[n] = u[n]$ and input to the system is $x[n] = 2^n u[-n]$, determine the output $y[n]$ of the system. [6]
8. a) State and prove commutative property of continuous time LTI system. [3]
- b) Explain Invertibility of LTI system and derive the necessary condition for two LTI systems to become inverse of each other. [5]

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1. a) Given: $x(t) = \sin(t)$. Is this signal periodic? Is it an energy signal or power signal or neither? [1+3]
 - b) "Combination of two continuous-time periodic signal might result in an aperiodic signal." Justify this statement using any numerical example. [4]
2. a) Derive the formula for synthesis equation and analysis equation of Fourier series. Mention the three conditions that guarantee the existence of Fourier series. [5+3]
 - b) State and explain four properties of discrete time Fourier series. [6]
3. a) State and prove Parseval's relation for finite energy signal. Describe any three applications of Fourier Transform. [6+3]
 - b) Calculate Fourier transform of a constant DC function. What are the physical meanings of Energy spectral Density and Power spectral Density? [5+3]
 - c) How do you calculate the Fourier transform of periodic sequence? Explain with necessary steps. [5]
4. a) Explain practical sampling method using a circuit diagram. Describe band-pass sampling theorem. [4+2]
5. a) Elaborate the physical meaning of convolution integral using suitable example. [3]
 - b) Derive convolution sum. Prove that an ideal low-pass filter is a non-causal system. [6+6]
6. a) Define transfer function and impulse response in discrete-time. Briefly explain the procedure of drawing a bode plot. [2+3]
 - b) State and explain any six properties of a discrete-time LTI system. [6]
 - c) Determine the range of a and b for which the given LTI system becomes stable whose impulse response is: [4]

$$h[n] = e^{an} U[n] + e^{bn} U[-n]$$
 where, $U[n]$ is discrete-time unit step function.

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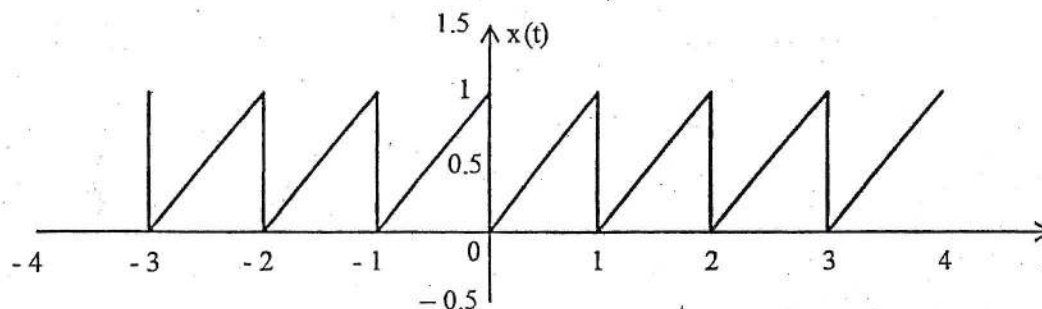
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1. a) Define energy and power signals with examples. [4]
- b) Derive the necessary condition for the signal $e^{j\omega n}$ to be periodic. [4]
2. a) Calculate and plot magnitude and phase spectrum of the following periodic signal. [8]



- b) State and prove Parseval's relation for discrete time periodic signals. [6]
3. State and prove the complex conjugation property for continuous time a periodic signals. Also show that if the CT signal is purely real, its Fourier Transform is conjugate symmetric. [4+4]
4. a) Find the Fourier Transform of discrete time signal $[n] = a^n u[n]$, $0 < a < 1$. [6]
- b) Compute the 4-point DFT for $x[n] = \{3, -2, 1\}$. [6]
5. State Nyquist's sampling theorem. Find the Nyquist rate for the given CT signal [2+4]

$$x(t) = \frac{1}{2\pi} \cos(50\pi t) \cos(500\pi t)$$

6. a) What is an LTI system? Find the output of the LTI system with impulse response $h(t) = e^{-2t} u(t)$ when the input to the system is $\begin{cases} 1; & |t| < 5 \\ 0; & \text{otherwise} \end{cases}$. [2+8]
- b) Show that ideal low pass filter is not practically realizable. [7]
7. Find and plot the convolution sum of the signals $x[n] = \{-0.5, 1, -1, 0.5\}$ and $y[n] = \{1, 2, -1, 0, 2, -1\}$. [8]
8. For a system characterized by linear constant coefficient difference equation $y[n] = 0.4 y[n-1] + x[n]$, find and plot the transfer function and impulse response of the system. [7]

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1. a) Define energy signal and power signal. Determine whether the signal $x(t) = e^{-3t}$ is a power signal or energy signal or neither energy nor power signal. [3+3]
 b) Define continuous time unit step signal. Derive the necessary condition for the signal $x(t) = e^{j\omega t}$ to be periodic. [1+3]
2. a) Derive the trigonometric fourier series expansion of a continuous-time periodic signal $x(t)$. [5]
 b) State and prove the time-scaling property for continuous-time fourier series pair. [5]
 c) State and prove frequency shifting property of discrete time fourier series. [3]
3. a) Find the fourier transform of the signal $x(t) = e^{-at}u(t)$; $a > 0$ and also plot the frequency spectrum. [5]
 b) Show that the convolution in time domain results multiplication in frequency domain using continuous time fourier transform. [5]
4. Determine the discrete time fourier transform of signum function ($\text{sgn}[n]$) and use it to find the DTFT of unit-step signal $u[n]$. [6+6]
5. a) State and prove the linearity and time shifting properties of DTFT [6]
 b) Define sampling theorem and Nyquist criteria for sampling. Find the Nyquist rate for the signal: $x(t) = 20 \sin(500\pi t) + 10 \cos(300\pi t) - 50 \cos(1000\pi t)$ [3+3]
6. a) Derive convolution integral for continuous LTI system. [5]
 b) Find convolution between the signals $x[n] = \{3, 5, 6, 9\}$ and $h[n] = \{-1, 3, 5\}$. Choose your appropriate origin. Show the output signal. [6]
7. a) Derive the expression for impulse response of RC filter and plot the magnitude and phase response. [6]
 b) Find the frequency response ($e^{j\omega}$), plot the magnitude and impulse response $h[n]$ for a system characterized by linear constant coefficient difference equation

$$y[n] = 0.5y[n-1] + x[n]$$

[6]

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1. a) Briefly explain CT unit impulse, unit step and unit ramp signal. What is the relationship between unit impulse, unit step and unit ramp signal? [4]
 b) Sketch the signal $x(t) = 5\cos(t)$. State whether the given signal is energy signal or power signal. [4]
2. Write down the condition of convergence of continuous time Fourier series. Find the Fourier series coefficient a_k for the continuous time period signal. [3+5]

$$x(t) = \begin{cases} 1.5, & 0 \leq t < 1 \\ -1.5, & 1 \leq t < 2 \end{cases}$$
3. State and prove:
 - a) Parseval's theorem for a DT aperiodic signal. [4]
 - b) Convolution property of the CT Fourier Transform. [4]
4. a) Derive the expression of Discrete Time Fourier Transform for periodic Sequence. [7]
 b) Differentiate between energy and power spectral density. [4]
5. a) How does Nyquist criteria prevent aliasing? Explain with diagram. [4]
 b) Find the Nyquist rate and interval for the following signal: [4]

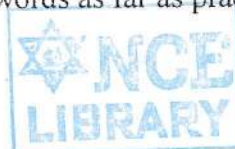
$$x(t) = 2\cos(100\pi t) \cos(300\pi t)$$
6. a) Derive the convolution sum for an LTI system. [6]
 b) Determine if the following system is linear $y[n] = ax[n] + b$ [4]
7. a) Derive the expression for impulse response of ideal low pass filter. [5]
 b) Define LTI system. Explain the properties of discrete time LTI system. [6]
8. Find the output of an LTI System given by: $x[n] = \delta[n] + 2\delta[n-1] - \delta[n-3]$ and $h[n] = 2\delta[n+1] + 2\delta[n-1]$. [8]
9. Find impulse response for the DT system given by the following Linear Constant Coefficient Difference Equation. $y[n] - \frac{3}{4}y[n-1] + \frac{1}{8}y[n-2] = 2x[n]$. [8]

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INSTITUTE OF ENGINEERING
Examination Control Division
2079 Chaitra

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BEL, BEX	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX 651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.



1. Define Power and Energy Type continuous Time signal with suitable examples. Check whether these signals are Energy or Power Type with required calculation. [2+4]
 - a) $x(t) = u(t)$
 - b) $x(t) = \delta(t)$
2. Derive the expression of Fourier Series Coefficient in exponential form for Continuous time periodic signal. Describe the condition for existence of Fourier series with suitable examples. [5+3]
3. a) Find the Fourier Transform of the signal $x(t) = e^{-a|t|}$; $a > 0$ and also plot the frequency spectrum. [5]
 - b) Show that the convolution in time domain results multiplication in frequency domain using continuous time Fourier Transform. [5]
4. Derive the expression of Fourier Transform of Discrete Time aperiodic Sequence. [8]
5. Define sampling theorem. Determine the Nyquist rate for the continuous time signal, $x(t)$. [2+4]

$$x(t) = 1 + \cos(2000\pi t) + \sin(4000\pi t).$$
6. What are the properties of system? Determine whether the given system is time-variant or not. [2+5]

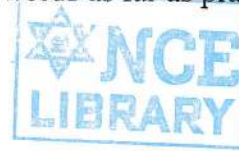
$$y(t) = \sin[x(t)]$$
7. a) Describe different Properties of Discrete time LTI system with suitable example. [5]
 - b) Convolve the signal $x[n] = \{3, 1, 5\}$ and $h[n] = \{1, 4, -2, 3\}$ [5]
8. a) Describe bode plot with example [4]
 - b) Derive the expression for impulsive response of ideal low pass filter and discuss. [5]
9. a) State and prove the Time-Scaling property for discrete-time Fourier series pair. [4]
 - b) Find the frequency domain representation (both magnitude and phase plot) of a periodic signal defined as $x[n] = \{1, -0.5, 0, 0, 0.5\}$, with period $N = 5$. [6]
10. What is aliasing and how can it be prevented? [6]

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2078 Chaitra

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BEL, BEX	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.



1. Show that any signal can be decomposed into an odd and even component. Is the decomposition unique? Illustrate your argument using the signal.
 $x[n] = \{2, 3, 4, 5, 6\}$ [3+5]
 2. a) Derive the Trigonometric Fourier series expansion of a continuous- time periodic signal $x(t)$. [5]
 b) State and prove the Time- Shifting property for discrete – time Fourier series pair. [4]
 3. a) State and prove convolution property of discrete time periodic signals. [2+3]
 b) What is Parseval's relation? Prove Parseval's relation for continuous-time periodic signal. [2+3]
 4. a) Find the Fourier Transform of the signal $x(t) = e^{-at}$; $a > 0$ and also plot the frequency spectrum. [5]
 b) Obtain the Fourier transform of the continuous-time signal. [6]
 5. a) What is convolution? Obtain the expression for convolution sum. [6]
 b) Find and plot the convolution between [8]
- $$x[n] = \begin{cases} |n|; & -2 \leq n \leq 2 \\ 0; & \text{otherwise} \end{cases} \quad \text{and} \quad y[n] = \begin{cases} 2n; & 2 \leq n \leq 5 \\ 0; & \text{otherwise} \end{cases}$$
6. a) What do you mean by aliasing? Compute Nyquist rate for [2+4]
 $x(t) = 5\cos(1500\pi t) - 2\sin(2000\pi t) + 3\sin(1850\pi t)$
 b) Evaluate the Step response of RC filter. [5]
 7. a) What is the condition for LTI system to be causal? [5]
 b) Determine if the following system is Linear [3]
 $y[n] = ax[n] + b$
 c) Check if the system is time invariant [3]
 $y[n] = nx[n] - x[n-1]$
 8. a) Define energy and power signal. [2]
 b) Determine the energy of the signal [4]
 $X(t) = 5\cos\pi t + \sin 5\pi t, -\alpha < t < \alpha$

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Examination Control Division
2077 Chaitra

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BEL, BEX	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX 651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. a) Define energy signal and power signal. Determine whether the signal $x(t) = e^{-5t}u(t+2)$ is energy signal or power signal or neither energy nor power signal. [3+4]

- b) $x(t)$ and $y(t)$ are continuous time signals defined as:
 $x(t) = \sin 6\pi t$ and $y(t) = \cos 8t$
Determine whether:

- (i) $x(t)$ is periodic.
- (ii) $y(t)$ is periodic.
- (iii) $x(t) + y(t)$ is periodic

If periodic, find the fundamental time period of $x(t)$, $y(t)$ and $x(t)+y(t)$. [3]

2. a) A continuous time Fourier Series is evaluated over infinite duration while a discrete time Fourier series is evaluated over one time period only. Why? [2]

- b) Obtain fourier series coefficients of the signal:

$$x[n] = 1 + 3 \cos\left(\frac{2\pi n}{N} + \frac{\pi}{3}\right)$$

Where,

N is the fundamental time period of $x[n]$.

Also, Plot magnitude and phase spectrum of the coefficients. [2+2+2]

- c) Derive exponential form of Fourier series for discrete time signal. [4]

3. a) Derive the Fourier Transform equation for discrete time aperiodic signals. Also prove that the DTFT is periodic with period 2π . [4+2]

- b) Given discrete time signal is :

$$x[n] = a^n U[n], |a| < 1$$

Given that Fourier transform of $x[n]$ is continuous in nature, plot magnitude and phase response of the transformed signal. [4]

4. a) State and prove duality property of continuous time Fourier Transform. [5]

- b) State and explain Energy density spectrum. [5]

5. a) Derive the convolution integral. [4]

- b) Find the convolution between the following sequences.

$$h[n] = \{2, 0, -1, 2\}$$

$$x[n] = \{1, 2, -1, 3\}$$

Choose origin as per your choice.

[6]

6. a) What do you mean by causal and non causal systems? Derive the condition for a continuous time LTI system to be causal. [2+3]
- b) Prove, with necessary derivations, that an ideal low pass filter is not physically realizable. Also derive the expression for step response of ideal low pass filter. [3+3]
7. a) Define Nyquist sampling theorem. Explain using frequency domain analysis of impulse train sampling. [6]
- b) Find the frequency response and impulse response for a system characterized by linear constant coefficient difference equation $y[n] = 0.5y[n-1] + x[n]$. [4+2]
8. Consider a continuous time system with input $x(t)$ and output $y(t)$ related by $y(t) = x(t-2) + x(2-t)$. Is the system Linear Time invariant? Explain. [5]

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Examination Control Division
2076 Baisakh

Exam.	Back		
Level	BE	Full Marks	80
Programme	BEL, BEX	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX 651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. a) Define even and odd signal in both continuous time and discrete time with examples. [4]
b) Explain time shifting, time scaling and time inversion of a continuous time signal with example. [3]
2. a) Derive necessary condition for a discrete time signal to be periodic. Find the energy and power of the discrete time signal $x[n] = e^{j\omega_0 n} u[n]$, where $u[n]$ is unit step function. [3+4]
b) Explain the behaviour of discrete time complex exponential $x[n] = c\alpha^n$ where c and α are real. [4]
3. a) What is Parseval's relation? Prove Parseval's relation for continuous-time periodic signal. [2+4]
b) State and prove time scaling properties of exponential fourier series. [4]
4. a) Derive Fourier series synthesis and analysis equation for discrete time periodic signal. [6]
b) Explain with necessary derivation that the discrete time Fourier Transform is periodic in frequency with period 2π . [4]
5. a) State and prove frequency derivative property of fourier transform. Use same property to find fourier transform of $x(t) = t \exp(-a^*t)u(t)$, $a > 0$ [3+4]
b) Find Discrete time Fourier transform of the discrete time signal $x[n] = u[n-2] - u[n-6]$. [5]
6. a) What is aliasing in sampling? Determine the Nyquist rate for the continuous time signal $x(t) = 1 + \cos(2,000\pi t) + \sin(4,000\pi t)$ [2+4]
b) Derive formula to calculate the impulse response of Ideal low pass filter in discrete time. [5]
7. a) Derive convolution sum. [4]
b) Find the convolution sum of $x[n] = \{1, 3, 4, 3, 1\}$ and $h[n] = \{2, 2, -2\}$ [6]
8. Write short notes: [3x3]
 - a) Frequency shifting DT FT
 - b) LTI system
 - c) Bode plot

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BEL, BEX	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX 651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Derive necessary condition for a discrete time signal $x[n] = e^{j\omega_0 n}$ to be periodic.

Determine whether the discrete time signal $x[n] = 3e^{j3\pi(n+\frac{1}{2})/5}$ is periodic or not. [4+4]

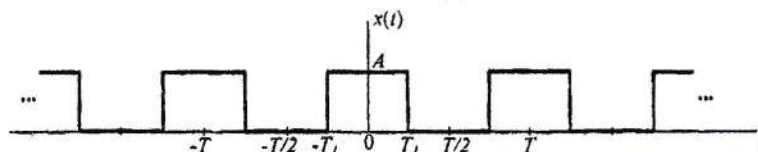
2. Derive the expression to compute Fourier series coefficients of exponential Fourier series. Explain Gibbs phenomenon. [8]

3. a) State and prove Parseval's relation for Discrete-Time Fourier Series (DTFS). [5]

- b) A periodic square wave as shown in figure below is defined over one period as: [5]

$$x(t) = \begin{cases} A, & |t| < T_1 \\ 0, & T_1 < |t| < T/2 \end{cases}$$

Determine the Fourier series coefficients for $x(t)$.



4. a) State and prove the convolution property of continuous-time Fourier Transform. [5]

- b) Find the Fourier Transform of the signal $x(t) = e^{-at} u(t)$, where a is real constant. Also, draw its amplitude and phase spectra. [6+2]

5. What is aliasing? Determine Nyquist rate for the continuous time signal $x(t) = 1 + \cos(2,000\pi t) + \sin(4,000\pi t)$ [2+4]

6. Derive formula to calculate convolution integral for continuous time LTI system. Find convolution between following continuous time signals $x(t) = e^{-t} u(t)$ and $y(t) = e^{-2t} u(t-3)$ [5+6]

7. a) The impulse response of a LTI system is

$$h[n] = \{1, 2, 1, -1\}$$



Determine the response of the system to the input signal

$$x[n] = \{1, 2, 3, 1\}$$



- b) Check whether the discrete-time system described by the following input-output relation is linear or non-linear. [4]

$$y[n] = 2 \times x[n] + 5$$

8. Define invertibility of LTI system with suitable example if impulse response $h[n] = U[n]$ and inverse system $h'[n] = \delta[n] - \delta[n-1]$. Prove that their convolution must be $\delta[n]$. [3+4]

9. Find the frequency response $H(e^{j\omega})$ and impulse response $h[n]$ for a system characterized by linear constant coefficient difference equation $y[n] = 0.3y[n-1] + x[n]$. [7]

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INSTITUTE OF ENGINEERING
Examination Control Division
2075 Bhadra

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BEL, BEX	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. a) Define 'continuous' and discrete time signals giving suitable examples. [3]
b) Show that any signal can be decomposed into an odd and even component. [4]
2. a) Derive necessary condition for a discrete time signal to be periodic. Determine whether the following signals are energy or power signal $f(t) = 5 \cos \pi t + \sin 5 \pi t$ [3+3]
b) Explain the behaviour of continuous time complex exponential signal $x(t) = c e^{at}$. [3]
3. State Parseval's relation for discrete time Fourier series. Find the average power of discrete time periodic signal $X[n] = \sin\left(\frac{\pi n}{3}\right)$ using Fourier series coefficient. [2+5]
4. a) Obtain the expression for analysis equation for DTFS. [6+4]
b) Show that fourier series coefficient of discrete time signal is periodic in nature. [6]
5. a) State and prove Time shifting property of continuous time Fourier Transform. [2+5]
b) Find the Fourier transform of continuous time unit step signal. [5]
6. a) What do you mean by sampling, state the requirement of sampling frequency? Determine Nyquist rate for $x(t) = \frac{1}{2\pi} \cos(100\pi t) \cos(300\pi t)$ [2+4]
b) Derive the transfer function for discrete time low pass filter. [4]
7. a) Determine whether the given system is linear or not. [4]
 $Y(t) = A x(t) + B$
b) Derive convolution integral of a continuous time signal. [6]
8. Write short notes [3×3]
 - i) Discrete data function
 - ii) Energy and power signal
 - iii) Causal and non causal system

Exam.	Batch		
Level	BE	Full Marks	80
Programme	BEL, BEX	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Define even and odd signals. Develop the even/odd decomposition of a general signal $x(t)$. [4+4]
2. a) Derive the Fourier Series Expansion of a continuous – time periodic signal $x(t)$. [5]
 b) Find Fourier series coefficients and associated phase of the signal with fundamental frequency ω_0 : $x(t) = 1 + \sin(\omega_0 t) + 2 \cos(\omega_0 t) + \cos(2\omega_0 t + \pi/4)$ [5]
 c) State and prove the time shifting property of Discrete – time Fourier series. [4]
3. a) Explain energy density spectrum of a continuous – time aperiodic signal with necessary derivation. [5]
 b) Find and sketch the Fourier Transform of exponential signal: $x(t) = \exp(-a|t|) u(t)$, $a > 0$. [5]
4. a) State and prove convolution theorem of discrete – time aperiodic signal. [6]
 b) Compute four – point DFT of four – point sequence: $x[n] = \{0, 1, 2, 3\}$. [6]
5. Define sampling theorem and Nyquist criteria for sampling. Find the Nyquist rate for the signal: $x(t) = 20 \sin(500\pi t) + 10 \cos(300\pi t) - 50 \cos(1000\pi t)$ [6]
6. a) Define system. Explain causality and time variance properties of continuous – time LTI [2+4] system.
 b) Find output $y(t)$ of LTI system if input $x(t) = \exp(-at) u(t)$ and impulse response $h(t) = u(t)$. [5]
 c) Derive the conditions for distortionless transmission for continuous – time LTI system. [4]
7. a) Derive the convolution sum for discrete – time LTI system. [5]
 b) Perform convolution between signals: $x_1[n] = \{1, 2, 1, -1\}$ with origin at second position from left and $x_2[n] = \{1, 2, 3, 1\}$ with origin at first position from left. [5]
 c) Find $H(e^{j\omega})$ and $h[n]$ for a discrete – time LTI system with difference equation: [5]

$$y[n] = 0.5 y[n-1] + x[n]$$

Exam. Level Programme Year / Part	Regular		
	BE	Full Marks	80
	BEL, BEX	Pass Marks	32
	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Differentiate between energy signal and power signal. Show by giving suitable example that power of the energy signal is zero and energy of the power signal is infinite. [2+5]
2. a) Derive necessary condition for a discrete time signal to be periodic. [3]
b) Determine whether the following discrete time signals are periodic or not [4]
 - (i) $\sin 5n$
 - (ii) $\cos\left(\frac{2\pi n}{5}\right) + \cos\left(\frac{2\pi n}{7}\right)$
3. a) Derive the expression to compute Fourier series coefficients of exponential Fourier series. [5]
b) Explain the Dirichel Conditions for convergence of Fourier series. [3]
4. a) State and prove time shifting and time scaling properties of continuous time Fourier series. [4]
b) Find Fourier series coefficient of discrete time periodic signal

$$x[n] = \sin w_0 n \quad \text{where } w_0 = \frac{2\pi}{N}$$
 Plot the signal when $N = 5$. [4]
5. How do you find the Fourier transform of periodic signals? Find the Fourier transform of continuous time rectangular pulse and constant amplitude A and explain the result. [5+5]
6. Show that convolution in time domain results multiplication in frequency domain using continuous time Fourier transform. Determine discrete time Fourier transform of the discrete time signal $x(n) = 2^n U[n]$ and also plot magnitude and phase spectrum. [5+5]
7. State and prove frequency shifting property of Fourier transform. [2+3]
8. What is aliasing? Determine the Nyquist rate for the continuous time signal

$$x(t) = 1 + \cos(2,000\pi t) + \sin(4,000\pi t)$$
 [2+4]
9. a) Derive convolution integral for continuous time LTI system. [6]
b) Compute convolution sum of signal $x[n] = \{1, 2, 0, -1\}$ and $h[n] = \{2, 0, 2\}$. [7]
10. For a system characterized by linear constant coefficient difference equation:

$$y(n) = 0.3y(n-1) + x(n)$$
 find the transfer function, plot magnitude and find the impulse response of the system. [6]

Examination Control Division
2073 Magh

Exam.	New Back (2066 & Later Batch)		
Level	BE	Full Marks	80
Programme	BEL, BEX	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Define Energy signal and power signal. Determine whether the signal $x(t) = e^{-3t}$ is a power signal or energy signal or neither energy nor power signal. [3+4]
2. Derive the necessary condition for the discrete time signal $x[n] = e^{j\omega n}$ to be periodic. [4]
3. Derive the expression of continuous time exponential Fourier series $x[n] = A \sin \omega_0 n$ [6]
4. Find Fourier series coefficients of signal and plot the coefficients. [5]
5. State and prove the frequency shifting and convolution properties for discrete time Fourier series pair. [3+3]
6. State and prove the Parseval's relation for energy density spectrum. [2+4]
7. Find Fourier transform of signal $x[n] = a^n u[n]$ (where $0 < a < 1$) and plot magnitude and phase spectrum. [3+2]
8. What is aliasing effect and how can we overcome it? Determine Nyquist rate for a continuous time signal $x(t) = 2 \sin 40\pi t + 10 \cos 200\pi t + 5 \cos 100\pi t$. [3+3]
9. What is LTI system? For LTI system, describe the properties: (a) linearity (b) stability (c) time invariance and (d) causality. [2+8]
10. Derive the expression for impulse response of RC filter and plot the magnitude and phase. [4+2]
11. What do you mean by convolution? Derive the expression for convolution of two discrete time signals. [2+6]
12. A discrete time LTI system is defined by the impulse response $h[n] = \begin{cases} n & -2 \leq n \leq 2 \\ 0 & \text{otherwise} \end{cases}$. If the input to the given system is $x[n] = \{1, -0.25, 0, -1, 0.5, -0.5\}$, find and plot the output of the system. [7]
13. Find the Fourier Transform of the unit step signal. [4]

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BEL. BEX	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Differentiate between continuous time and discrete time signals with examples. Show that

$$U[n] = \sum_{k=0}^{\infty} \delta[n-k]$$
[2+4]
2. Calculate the fundamental period and fundamental frequency of the periodic signal

$$x[n] = 3 \sin\left(\frac{7\pi}{5}n + \frac{\pi}{2}\right)$$
[4]
3. Derive the expression for finding even and odd part of signal $x(t)$. Explain time scaling and time folding.
 [2+3]
4. Define discrete time complex exponential signal and its different types of behavior.
 [2+3]
5. a) Derive the expression for Fourier transform equation and inverse Fourier transform equation for continuous time aperiodic signals.
 [8]
 b) State and prove Frequency shift property of the continuous time Fourier Transform.
 [3]
6. State and prove Parseval's relation for the Discrete time periodic signal.
 [5]
7. What are the differences between Fourier series and Fourier Transform? Find the Fourier transform of the discrete time signal $x[n] = a^n \begin{cases} |a| < 1 \\ 0 < a < 1 \end{cases}$
[2+6]
8. Derive the expression for convolution integral for continuous time signal.
 [6]
9. What is LTI system? In a LTI system show that convolution operation is commutative, find $y[n]$ when $x[n] = \{1, 2, 3, 4\}$ and $n[n] = \{2, 1, 2\}$
[2+3+5]
10. What is sampling? Determine the Nyquist rate for the following signal:

$$x(t) = 1 + \cos(200\pi t) + \sin(4000\pi t)$$
[2+3]
11. Derive Formula to calculate the impulse response of continuous time ideal low pass filter. Is this system practically realizable or not.
 [4+2]
12. Write short notes on:
 [3×3]
 - i) Energy and power signals
 - ii) Invertibility of LTI system
 - iii) Nyquist theorem

Exam.	Regular		
Level	BE	Full Marks	80
Programme	BEL, BEX	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. a) Define energy signal and power signal. Determine whether the signal is a power signal or energy signal. [3+3]
 $x(t) = e^{-at}$ for $a > 0$
- b) Define discrete time unit step signal. Derive the necessary condition for the signal $x[n] = e^{j\omega n}$ to be periodic. [1+3]
2. a) Derive exponential form of Fourier series for continuous time signal. [5]
- b) State and prove Parseval's relation for the Discrete time periodic signal. [5]
3. Derive the expression for Fourier transform of continuous-time periodic signals. Using this expression obtain the Fourier transform of periodic signal. [4+4]
 $x(t) = 1$ for $0 < t < T, 0$ otherwise
4. a) State and prove the linearity and time shift properties of discrete time Fourier series representation. [6]
- b) State and prove the conjugation property for continuous time Fourier transform. Show that if the signal is real valued in time domain, its spectrum is conjugated symmetric. [4+2]
5. Obtain the DTFT of the signal $x[n] = (n+1)a^n u[n], 0 < a < 1$ [6]
6. What is convolution? Obtain the expression for convolution integral. [2+6]
7. What is impulse train sampling? Explain the aliasing effect that may occur in impulse train sampling. How do you reconstruct original signal from its sample? [1+2+3]
8. What is LTI system? Explain the commutative, associative and distributive properties of discrete time LTI systems. [2+6]
9. The impulse response of a discrete time LTI system is $h[n] = \{1, 1, 2, -1\}$ if input is $x[n] = \{1, 2\}$, find the convolution sum and sketch the output $y[n]$. [6]
10. Find the frequency response $H(e^{j\omega})$ and impulse response $h[n]$ for a system characterized by linear constant coefficient difference equation $y[n] = 0.5y[n-1] + x[n]$. [6]

New Batch (2066 & Later Batch)			
Exam. Level	BE	Full Marks	80
Programme	BEX, BEL	Pass Marks	32
Year / Part	III / II	Time	3 hrs.

Subject: - Signal Analysis (EX651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Find the energy and power of the signal $x[n] = e^{j\omega n} u[n]$. $u[n]$ is unit step function. What is the period of signal $x[n] = \cos\left(\frac{41\pi}{7}n\right)$? [6]
2. Plot the signal $x(t) = t(u(t+3) - u(t-3))$. [2]
3. Find Fourier series coefficients for periodic rectangular pulses with unity amplitude. Draw the magnitude spectrum. [5+1]
4. Derive the expression for discrete time Fourier series representation of the signal $x[n]$ periodic with period of N . [7]
5. Determine the expression of Fourier Transform for continuous time aperiodic signal. [7]
6. Perform the convolution and draw output $y[n]$ $x[n] = \{1 \quad 2 \quad 2 \quad 3\}$ and $h[n] = \{1 \quad 4 \quad 3\}$. [7]
 $\uparrow \qquad \qquad \qquad \uparrow$
7. State and prove Parseval's theorem for continuous time aperiodic signal. [2+4]
8. What is aliasing effect and how can we overcome it? Determine the Nyquist rate for a continuous time signal $x(t) = 6 \cos 50 \pi t + 20 \sin 300 \pi t - 10 \cos 100 \pi t$. [3+3]
9. Find convolution between two signals $x(t) = \begin{cases} e^{0.5t} & \text{for } 0 < t < 5 \\ 0 & \text{otherwise} \end{cases}$ and $h(t) = \begin{cases} 1 & \text{for } 1 < t < 3 \\ 0 & \text{otherwise} \end{cases}$. [7]
10. Derive the expression for impulse response and step response of ideal low pass filter. [4+4]
11. For the LTI system, describe following properties: (a) linearity (b) causality (c) stability (d) time invariance. [6]
12. If the impulse response of continuous time linear time invariant system is $h(t) = e^{-t}u(t-3)$ and input to the system is $x(t) = u(t-2)$, determine the output $y(t)$ of the system. [8]
13. Describe bode plot with example. [4]

Exam.	Regular / Back		
	BE	Full Marks	80
Level	BEL, BEX	Pass Marks	32
Programme	III / II	Time	3 hrs.
Year / Part			

Subject: - Signal Analysis (EX6541)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Define energy and power signal with examples. Describe time shifting, time scaling of a signal. [3+4]
2. Derive convolution integral for continuous time LTI system. [8]
3. State and prove Parseval's Relation for Continuous Time Periodic Signal. [6]
4. Explain aliasing that may occur in any arbitrary band-limited signal $x(t)$ with band-width 'W'. [5]
5. Derive the expression for continuous time Fourier series in exponential form. [7]
6. Explain the convolution properties of continuous time Fourier transform. [6]
7. Discuss the following properties of continuous time Fourier series. (a) Time shifting (b) Time scaling (c) Conjunction. [6]
8. Derive the expression of Fourier transform for continuous time signal. [8]
9. Derive the expression for impulse response of ideal low pass filter and discuss. [5]
10. Find the Fourier Transform of a continuous time unit step signal. [5]
11. Discuss different methods to reconstruct a signal. Determine the Nyquist rate for a continuous time signal $x(t) = \frac{1}{2\pi} \cos(200\pi t) \cos(300\pi t)$. [4+4]
12. Convolve the signals $x[n] = \{1, 2, 1\}$ and $h[n] = \{1, 2, 3, 1\}$. [6]
13. If the signal is periodic, find the fundamental period of the signal $x[n] = \cos\left(\frac{\pi}{2}n\right) \cdot \cos\left(\frac{\pi}{4}n\right)$. [3]

Subject: - Signal Analysis (EX651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Calculate the total energy and total average power of the signal given below:

$$x(t) = (3+4j)e^{2t}u(-t)$$

Also state whether the signal is energy signal, power signal or neither.

[3+1]

2. Determine whether the signal $x[n] = 5\sin\left(\frac{3\pi}{8}n - \frac{\pi}{2}\right) - 2\cos\left(\frac{7\pi}{12}n\right)$ is periodic or not. If the signal is periodic, calculate its fundamental period and fundamental frequency.

[4]

3. How could you represent a signal $x(t)$ with harmonically related exponentials? State and prove conjugation and conjugate symmetry property of CTFS.

[4+4]

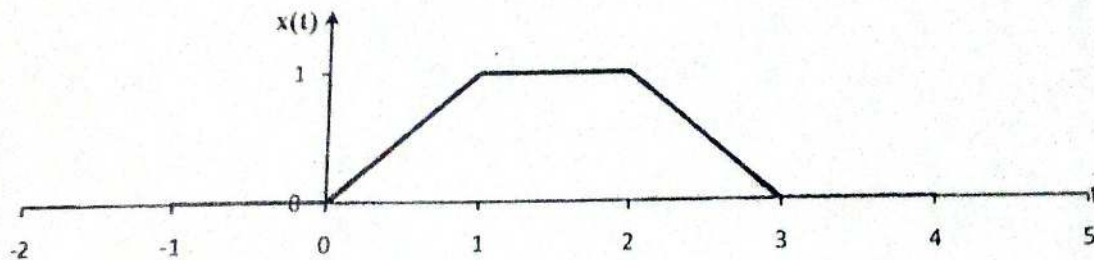
4. Find the Fourier series coefficients of the signal

[6]

$$X[n] = 1 + \sin(2\pi/N)n + 3\cos(2\pi/N)n + \cos(4\pi/N)n$$

[8]

5. Find the Fourier transform of a trapezoidal signal shown below:



6. How can you generate Fourier transform for discrete time periodic signals? Explain.

[3]

7. State and prove Parseval's relation for discrete time Fourier transforms.

[5]

8. Compute 4-point DFT of a signal $x[n] = \{2, 1+j, 1-j\}$ and plot its magnitude and phase spectrums.

[4+2]

9. State and prove sampling theorem for low pass signals.

[6]

10. The impulse responses of two LTI systems are given by $h_1(t) = e^{-\frac{1}{2}t}u(t)$ and $h_2(t) = u(t) - u(t-5)$. Determine the equivalent impulse response if these two systems are connected in cascade. Also sketch the graph of equivalent impulse response.

[8+2]

11. Derive the impulse response for ideal low pass filter with cutoff frequency ω_c .

[5]

12. Given a system $Y[n] = 0.5y[n-1] + x[n] + x[n+1]$. Find out its impulse response and frequency response.

[7]

13. What are the properties of LTI system? Show that the output of an LTI system is stable if the impulse response is absolutely summable.

[8]

Exam.	Regular	
Level	BE	Full Marks 80
Programme	BEL, BEX	Pass Marks 32
Year / Part	III / II	Time 3 hrs.

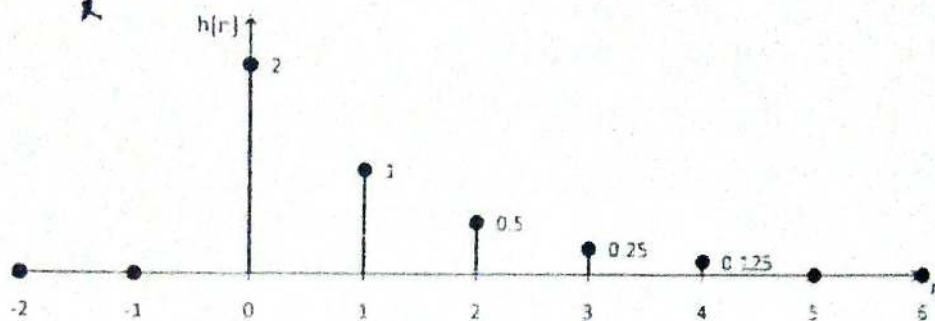
Subject - Signal Analysis (EX651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

- 3 ✓ 1. What do you understand by periodic and aperiodic signals? Explain with the help of examples. [4]
2. Determine whether the following signals are energy or power signals. [4]
- a) $f(t) = 3 \cos(2\pi t)$
- b) $x[n] = \cos\left(\frac{n}{6}\right)$
- 3 ✓ 3. What is the information provided by Fourier series coefficients of a signal? State and prove time shifting and conjugation properties of continuous time Fourier series representation. [1+6]
- 4 ✓ 4. Find out Fourier series coefficients of a periodic discrete time signal described over a period as [5+2]
- $$x[n] = \begin{cases} 2; & |n| \leq 1 \\ 0; & 1 < |n| \leq 1 \times 3 \end{cases}$$
- Using the Fourier series coefficients calculated above; find the Fourier series coefficients of the signal $e^{j\frac{4\pi}{7}n} x[n]$.
- 3 ✓ 5. Given the relationship $y(t) = x(t) * h(t)$ and $g(t) = x(3t) * h(3t)$ and given that $x(t)$ has the Fourier transform of $X(j\omega)$ and $h(t)$ has Fourier transform $H(j\omega)$, use Fourier transform properties to show that $g(t)$ has the form $g(t) = Ay(Bt)$. Determine the values of A and B. [8]
- 3 ✓ 6. Explain the linearity and time shifting properties of continuous time Fourier transform. [4]
- 5 ✓ 7. Find the Fourier transform of continuous time unit impulse and rectangular pulse. Discuss the result. [6]
- 7 ✓ 8. Find the Fourier transform of everlasting sinusoid $X(t) = \cos\omega_0 t$. [4]
- 6 ✓ 9. What do you mean by aliasing? Explain with the help of frequency domain analysis for impulse-train sampling. [1+5]
- 5 ✓ 10. What are the properties of systems? Determine whether the given system is time-variant or not: $y(t) = \sin[x(t)]$. [2+3]
- 5 ✓ 11. Let $x(t)$ be the input to an LTI system with unit impulse response $h(t)$, where, $x(t) = e^{-at} u(t)$, $a > 0$ and $h(t) = u(t)$. Verify commutative law of LTI system. [5]

12. What is distortionless transmission? Derive the expression for unit step response of ideal low pass filter. [5]

13. A discrete time LTI system has an impulse response as shown below. [6+2]



If the input to the given system is $x[n] = \{-0.25, 0.5, 1, -0.5, 0, 0.25\}$, calculate and plot the output of the system.

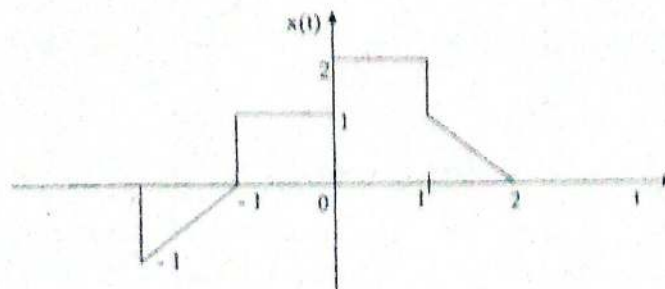
14. Define systems with memory and memory-less systems with examples. Explain the causality property of discrete time LTI systems. [3+4]

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Subject: - Signal Analysis (EX651)

- ✓ Candidates are required to give their answers in their own words as far as practicable.
- ✓ Attempt All questions.
- ✓ The figures in the margin indicate Full Marks.
- ✓ Assume suitable data if necessary.

1. Define energy and power type signal with suitable examples. Sketch and label the signal $y(t) = \{x(t) + x(-t)\}u(t)$ for given signal $x(t)$ depicted below. [3+5]



2. Derive the expression for Fourier series representation of a signal $x(t)$ periodic with period T . [8]
3. Find the Fourier series representation of the signal $x[n] = \sum_{l=-\infty}^{\infty} \delta[n - lN]$. [6]
4. State and prove Parseval's theorem for continuous time aperiodic signal. [4]
5. ALTI system has input $x(t) = e^{-t}u(t)$ and impulse response $h(t) = e^t u(-t)$. Find output $y(t)$ of the system using Fourier transform of $x(t)$ and $h(t)$. [8]
6. Compute discrete time Fourier transform of the discrete time signal $x[n] = \left(\frac{1}{2}\right)^n u[-n-1]$. [5]
7. Find circular convolution of the signal $x[n] = \{1, 0, 0, 1\}$ and $y[n] = \{2, 0, 2\}$. [5]
8. What is sampling. How are spectrum of continuous time signal and its sampled version related? Illustrate with diagram. [6]
9. Write about the following properties of continuous time system: (a) Linearity (b) Causality (c) Memory (d) Stability (e) Time invariance. [5]
10. Derive the expression for impulse response and step response of first order continuous time system described by the differential equation $\tau \frac{dy(t)}{dt} + y(t) = x(t)$. [5]
11. If the impulse response of continuous time linear time invariant system is $h(t) = u(t) - u(t-3)$ and input to the system is $x(t) = u(t+4) - u(t)$, determine the output $y(t)$ of the system. [5]
12. Find output of a LTI system using convolution sum, if the input signal is $x[n] = \delta[n] + 2\delta[n-1] - \delta[n-3]$ and impulse response of the system is $h[n] = 2\delta[n+1] + 2\delta[n-1]$. [7]
13. For a system characterized by Linear constant coefficient difference equation $y[n] = 0.5y[n-1] + x[n]$, find the frequency response $H(e^{j\omega})$ and impulse response $h[n]$. Also plot the frequency response magnitude $|H(e^{j\omega})|$. [8]