

Helical Staircase Assembly

Structural Verification Report

Code Compliance Check against Dubai Building Code, ASCE 7-16 and Eurocode 1

Project:

Element: Helical Staircase — One Flight (27 treads)

Software: SOLIDWORKS Simulation 2021

Material: S275JR (1.0044)

Report date: 25 May 2026

1. Introduction

This report documents the structural verification of one full flight of the helical staircase at . The objective is to demonstrate compliance with the requirements of the Dubai Building Code (DBC) Part K (Villas), ASCE/SEI 7-16 (referenced by DBC for all loading definitions) and Eurocode 1 (EN 1991-1-1) used as an international cross-check.

The staircase consists of two parallel helical strings (inner and outer) connecting two adjacent slabs over 27 treads. The strings are supported at three locations: a central steel column (CHS 610 × 14.3 mm), the upper slab landing, and the lower slab landing. Welded steel brackets transfer the load from each string to the central column. The treads are clad with French oak boards (~30 mm thick) and the railings are glass with a wooden top rail.

Five static finite element analyses and one frequency (modal) analysis were performed to verify strength, serviceability and vibration performance against the applicable codes.

1.1 Scope and Applied Loads

The following load scenarios were evaluated:

- Study Static 1 — dead load only on the COMPLETE assembly (all three flights): steel self-weight plus remote masses of the French oak treads, the laminated glass balustrade and the structural sealant. No live load.
- Study Static 2 — uniform live load 3000 N/m² applied over all treads of the COMPLETE assembly (all three flights), plus dead load, oak cladding, glass balustrade and structural sealant. Solved at three mesh densities (rough/middle/fine) to demonstrate convergence and to identify the governing flight. This is the governing strength load case.
- Study Static 3 — concentrated load 3000 N applied at the edge of step (position 1).
- Study Static 4 — concentrated load 3000 N applied at the edge of step (position 2).
- Study Static 5 — concentrated load 3000 N applied at the edge of step (position 3).
- Study Frequency 1 — modal analysis with dead load and remote masses (no external forces) to identify the natural frequencies of the structure.

Important: horizontal load on the railing (DBC + ASCE 7-16, ~0.75 kN/m) was NOT analysed in this report because the railing is full-height glass. The horizontal action on the railing is carried directly by the glass to the outer string and to the slab landings, and does not transfer torsional moment to the central column or to the bracket assembly evaluated here.

1.2 Boundary Conditions and Modelling Assumptions

- Fixed support: the lower slab and the upper slab interfaces are taken as fully rigid (zero deformation) and fully fixed against displacement and rotation in all six degrees of freedom. This represents the embedment of the staircase landings into the reinforced concrete villa floor slabs.
- The central vertical column is also fully fixed at its top and bottom anchorage rings (visible as green arrow groups on each simulation image).
- A single material — S275JR (1.0044) — is assigned to the entire steel assembly. The oak treads and the glass railing are not modelled geometrically; their masses are applied as remote distributed masses on the tread top faces and on the string contact faces respectively.
- All welds are modelled as bonded contacts. Bolted connections in the brackets are modelled with bolt-connector elements.
- All four staircase support brackets (one at each tread group + one at each landing) are identical and share the same model from the previous "stair_support_bracket" study.

2. Material and Code Requirements

2.1 Material

| Property | Value | Note |
|------------------------|--------------------------|--|
| Designation | S275JR (1.0044) | EN 10025-2 |
| Yield strength f_y | 275 MPa | Used in von Mises failure criterion |
| Tensile strength f_u | 410 MPa | Ultimate strength |
| Elastic modulus E | 210 GPa | Standard for structural steel |
| Poisson's ratio ν | 0.28 | — |
| Mass density ρ | 7,800 kg/m ³ | — |
| Model type | Linear elastic isotropic | Plasticity not modelled (design stays elastic) |

2.2 Applicable Codes and Load Requirements

Dubai Building Code Part K (Villas) section K.8.4.5 explicitly refers to ASCE/SEI 7-16, Chapter 4, for minimum live loads. Eurocode 1 (EN 1991-1-1) is used as an additional cross-check. The following table summarises the load requirements for a residential single-family staircase:

| Load type | DBC + ASCE 7-16 | Eurocode 1 (Cat. A) | Applied in this study |
|-------------------------------|---|--|---|
| Self-weight (dead load, G) | Per $\rho \times V$ | $\gamma_G = 1.35$ (ULS) | Yes — gravity 9.81 m/s ² |
| Remote masses (oak + glass) | Per actual weight | Per actual weight | Yes — 320 kg + 2 × 1300 kg |
| Uniform live load (Q) | 1.92 kN/m ² × $\gamma = 3.0$ kN/m ² | 2.0 kN/m ² × $\gamma_Q 1.5 = 3.0$ kN/m ² | Yes — Static 2 (3000 N/m ²) |
| Concentrated load on tread | 1.33 kN × $\gamma \approx 2.1$ kN | 2.0 kN × $\gamma_Q 1.5 = 3.0$ kN | Yes — 3000 N (Static 3-5) |
| Horizontal load on handrail | 0.73 kN/m | 0.5 kN/m | N/A — glass railing, see §1.1 |
| Natural frequency | > 8 Hz (vibration) | > 5 Hz residential | Yes — Frequency 1 study |
| Allowable stress (ULS) | $f_y / 1.0 = 275$ MPa | $f_y / \gamma_{M0} 1.0 = 275$ MPa | Check $\sigma < 275$ MPa |
| Allowable deflection (SLS) | $L / 360$ for stairs | $L / 300$ spans, $L / 250$ cantilevers | Check $\delta < L / 300$ |

Both code systems converge on the same effective design loads: approximately 3.0 kN/m² uniform live load and 2.0–3.0 kN concentrated live load on a 100 × 100 mm contact patch. The 3000 N concentrated value used in Studies 3, 4 and 5 covers both code requirements with a small additional margin.

3. Results — Summary

| Study | Load case | σ max (MPa) | δ max (mm) | Min FoS | Status |
|--------------------|---|--------------------|---------------------------------|-------------|---------------|
| Static 1 | Dead load only, full assembly (3 flights) | 43.04 | 0.94 | 6.39 | PASS ✓ |
| Static 2 | Uniform 3000 N/m ² , full assembly (3 flights) | 122.29 | 1.82 | 2.25 | PASS ✓ |
| Static 3 | DL + 3000 N at edge, step v1 | 67.16 | 0.64 | 4.09 | PASS ✓ |
| Static 4 | DL + 3000 N at edge, step v2 | 68.74 | 0.83 | 4.00 | PASS ✓ |
| Static 5 | DL + 3000 N at edge, step v3 | 53.81 | 0.56 | 5.11 | PASS ✓ |
| Frequency 1 | Modal analysis with DL | — | f₁ = 10.08 Hz | — | PASS ✓ |

Allowable stress limit: 275 MPa ($f_y / \gamma M_0$). All values are well below this threshold. Allowable deflection: $L / 300 \approx 13$ mm assuming span $L \approx 4$ m. Allowable natural frequency: > 8 Hz per DBC vibration recommendations.

4. Detailed Results

4.1 Static 1 — Dead Load Only (Full Assembly, All Three Flights)

This study models the complete staircase assembly (all three flights) under permanent (dead) loads only, with no live load applied. The applied loads comprise the steel self-weight (gravity) plus remote masses representing all cladding and finish materials: the French oak tread boards, the laminated glass balustrade and the structural sealant (Arbokol or equivalent), distributed across all three flights. This study establishes the baseline stress state of the full structure under permanent loads.

Von Mises Stress

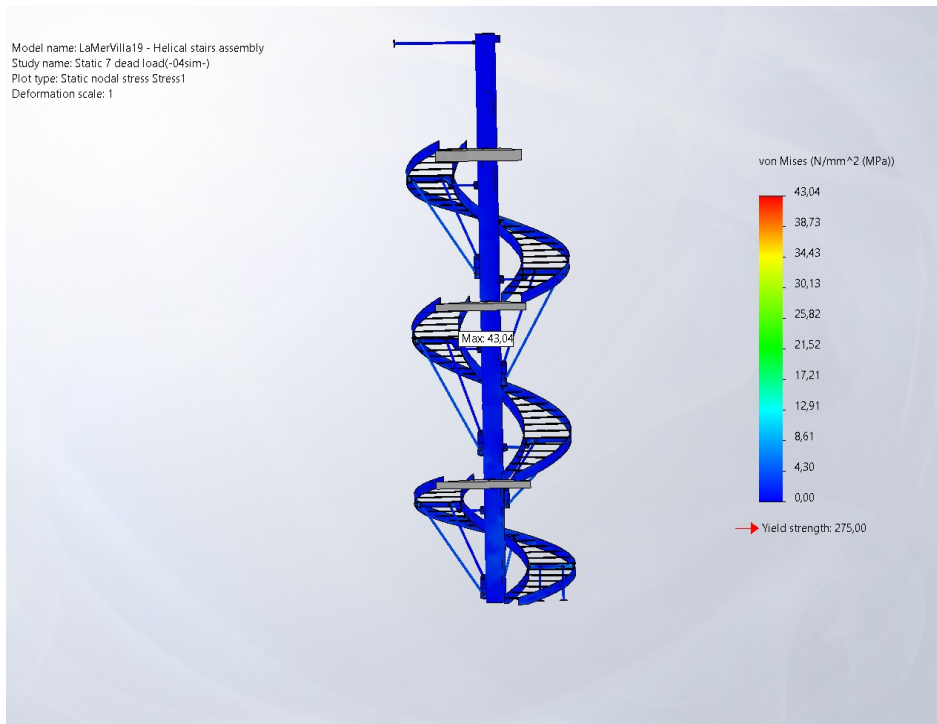


Figure 4.1.1 — Static 1 (full assembly): stress overview, peak sigma = 43.04 MPa.

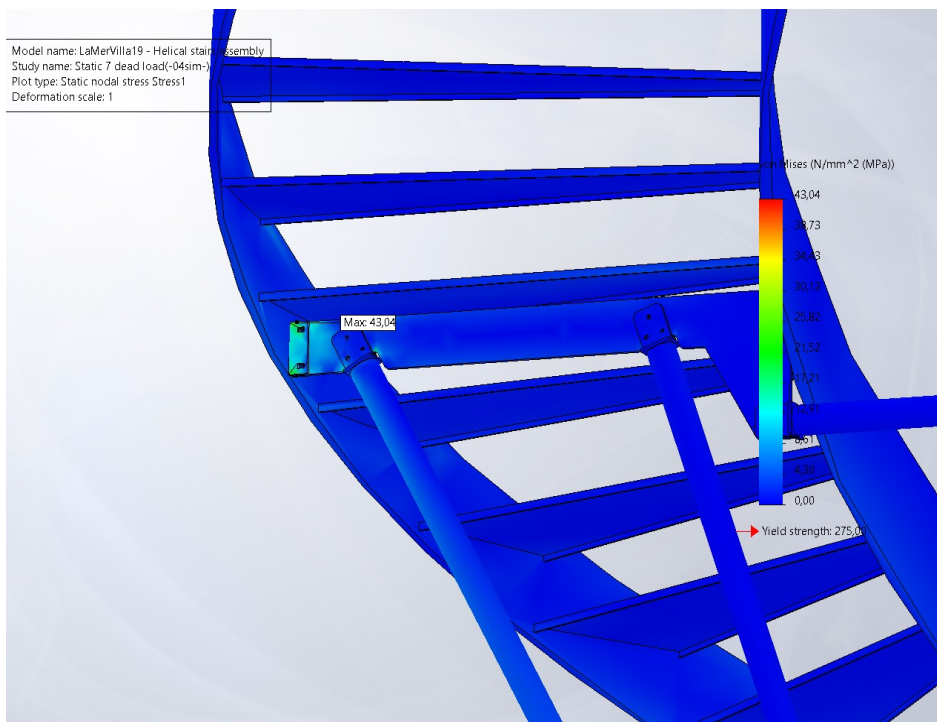


Figure 4.1.2 — Static 1: stress detail at the critical bracket.

Peak stress of 43.04 MPa occurs at a welded stringer-to-column bracket. This is only about 16% of the S275JR yield strength of 275 MPa. The structure is very lightly stressed under dead load alone, confirming that the limiting cases are the live-load scenarios analysed in the subsequent sections.

Resultant Displacement

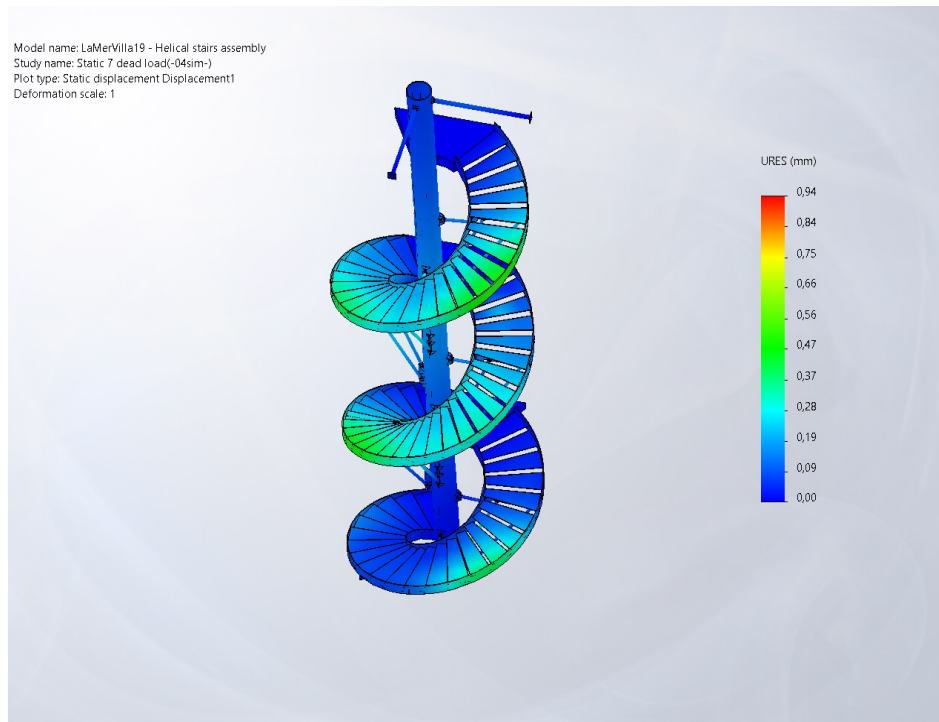


Figure 4.1.3 — Static 1: resultant displacement, peak delta = 0.94 mm.

Peak displacement of 0.94 mm is well below the $L / 300 \approx 13$ mm serviceability limit. The complete staircase is very rigid under permanent loads.

Factor of Safety

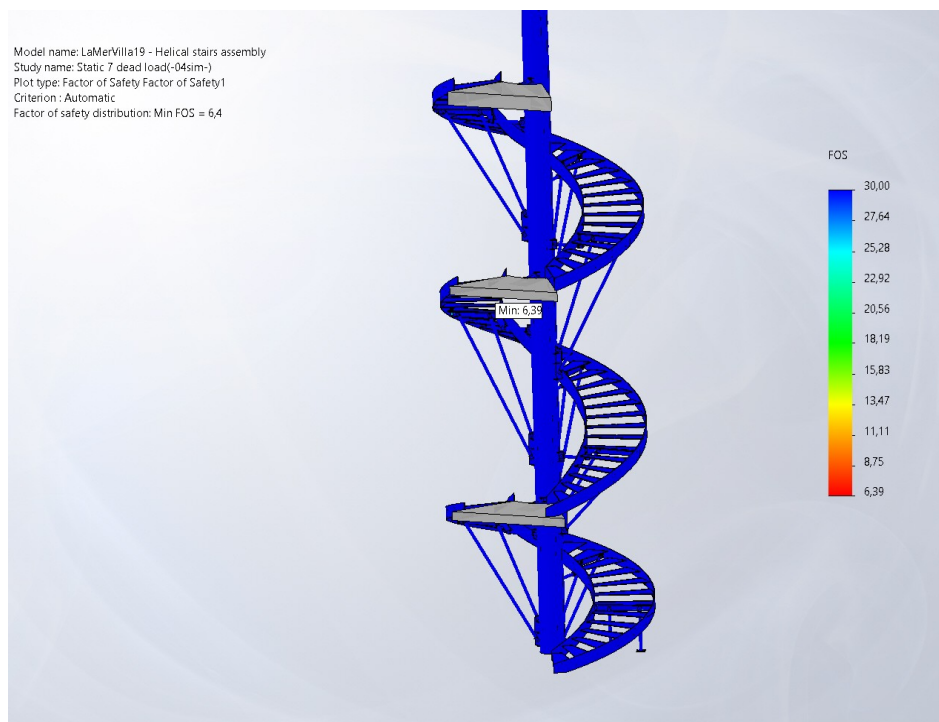


Figure 4.1.4 — Static 1: factor of safety overview, Min FoS = 6.39.

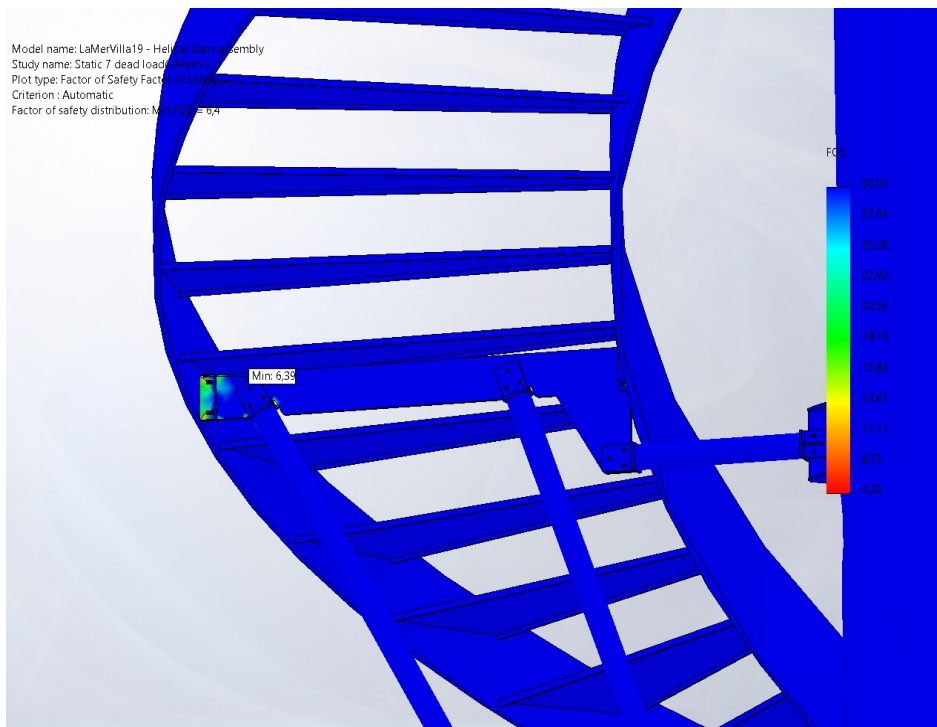


Figure 4.1.5 — Static 1: factor of safety detail at the critical bracket.

Minimum factor of safety of 6.39 indicates a very large reserve capacity under dead load only — as expected for a structure that must also carry significant live loads. The total vertical support reaction under dead load is approximately 118.6 kN (compared with 196.5 kN under full dead-plus-live loading in Static 2).

4.2 Static 2 — Uniform Live Load 3000 N/m² (Full Assembly, All Three Flights)

This study applies a uniform pressure of 3000 N/m² (= 3.0 kN/m², the ULS-factored residential live load per DBC + ASCE 7-16 Chapter 4) over the top faces of all treads across the entire staircase — all three flights (floors) simultaneously. In contrast to the other studies in this report (which analyse a single flight), this analysis models the complete assembly to capture the global load distribution and to identify which flight is the most critical.

The applied loads include, in addition to the uniform live load: the steel self-weight (gravity), the French oak tread cladding, the laminated glass balustrade and the structural sealant (Arbokol or equivalent). The full set of applied masses is reflected in the support reactions reported below.

Because the peak stress location depends on mesh density at the critical welded bracket detail, this load case was solved at three mesh densities (rough, middle and fine) to demonstrate convergence. This satisfies the mesh-convergence requirement of the pre-submission checklist.

4.2.1 Mesh Parameters and Convergence

Three mesh densities were evaluated for the full-assembly model, all using blended curvature-based second-order tetrahedral elements:

| Mesh density | Max element | Total nodes | Total elements |
|---------------|-------------|-------------|----------------|
| Rough | 772.7 mm | 216,930 | 103,438 |
| Middle | 492.4 mm | 337,949 | 162,543 |
| Fine | 333.3 mm | 426,661 | 206,363 |

The corresponding results at each mesh density are summarised below:

| Mesh density | Peak sigma (MPa) | Max delta (mm) | Min FoS |
|------------------------|------------------|----------------|-------------|
| Rough (773 mm) | 91.64 | 1.06 | 3.00 |
| Middle (492 mm) | 108.85 | 2.26 | 2.53 |
| Fine (333 mm) | 122.29 | 1.82 | 2.25 |

As the mesh is refined, the peak stress rises from 91.6 to 122.3 MPa and the minimum factor of safety settles at 2.25 (fine mesh). The change between the middle and fine meshes (108.9 to 122.3 MPa) is moderate and the FoS remains well above 2.0, indicating an adequately converged result. The fine-mesh values are used as the governing result.

4.2.2 Support Reactions

The total support reactions from the fine-mesh solution (sum across both slab landings and the central column base) confirm overall equilibrium under the applied loads:

| Direction | Reaction force (N) | Note |
|---------------------------|--------------------|--------------------------------|
| Sum X (horizontal) | -12,375 | Lateral equilibrium |
| Sum Y (vertical) | 196,549 | Total vertical load ≈ 196.5 kN |
| Sum Z (horizontal) | 5,221 | Lateral equilibrium |
| Resultant | 197,007 | ≈ 197 kN total |

The vertical reaction of 196.5 kN represents the combined dead load (steel, oak, glass, sealant) plus the full 3 kN/m² live load across all three flights. This value is used as the basis for the column buckling check (Section 4.7) and for the base-plate/anchor design.

4.2.3 Von Mises Stress

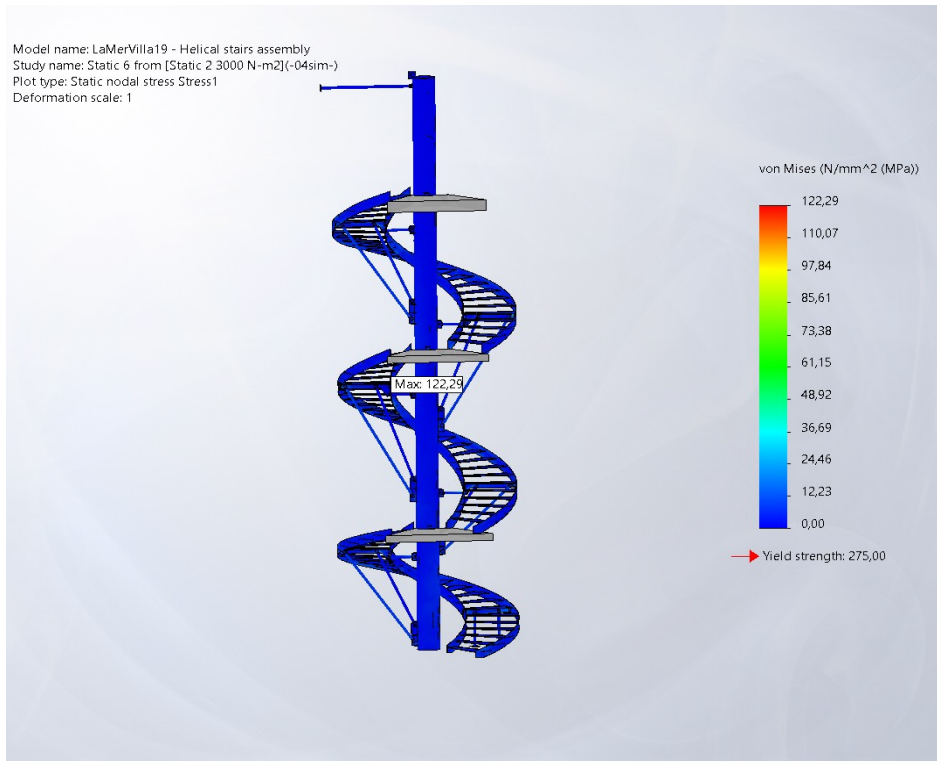


Figure 4.2.1 — Static 2 (fine mesh): stress overview of the complete three-flight assembly, peak sigma = 122.29 MPa located on the MIDDLE flight (2nd floor).

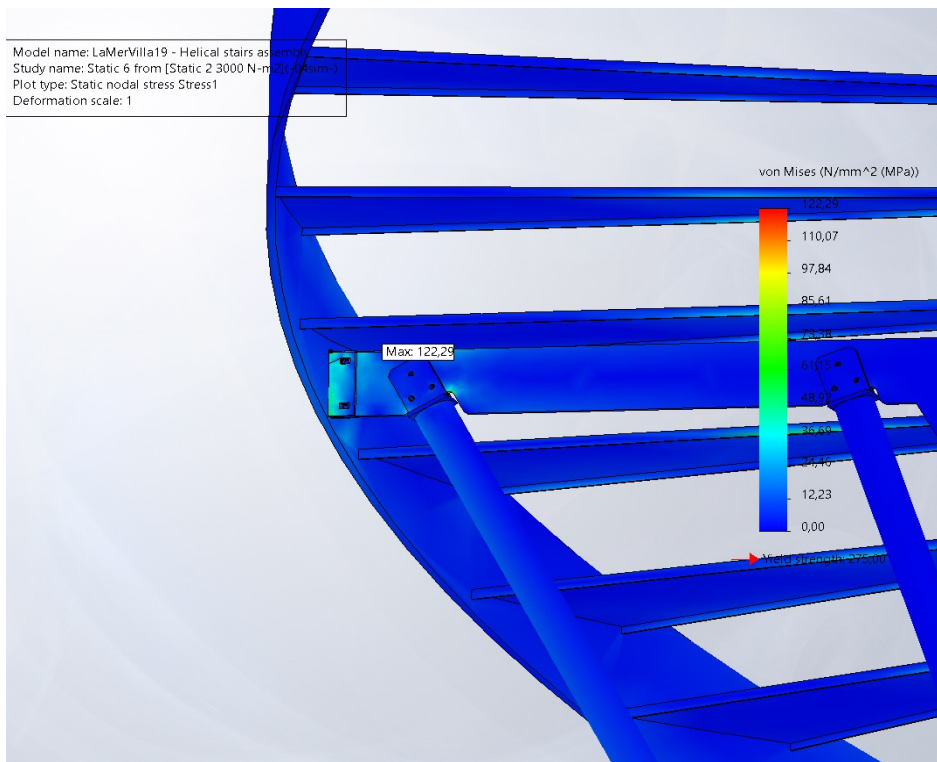


Figure 4.2.2 — Static 2 (fine mesh): stress detail at the critical welded bracket on the middle flight.

The peak stress of 122.29 MPa is located on the MIDDLE flight (second floor) at a welded stringer-to-column bracket. This is approximately 44% of the S275JR yield strength of 275 MPa. The other two flights show lower stresses, confirming that the middle flight is the most heavily loaded — it carries load from above while spanning between the supports without the benefit of direct slab proximity at both ends.

This finding is the key result of the full-assembly analysis: it identifies the middle flight as the governing (most critical) flight. For this reason, all the remaining detailed studies in this report (Static 1, 3, 4, 5 and the modal analysis) are performed on the middle flight, which represents the worst case for the whole staircase.

4.2.4 Resultant Displacement

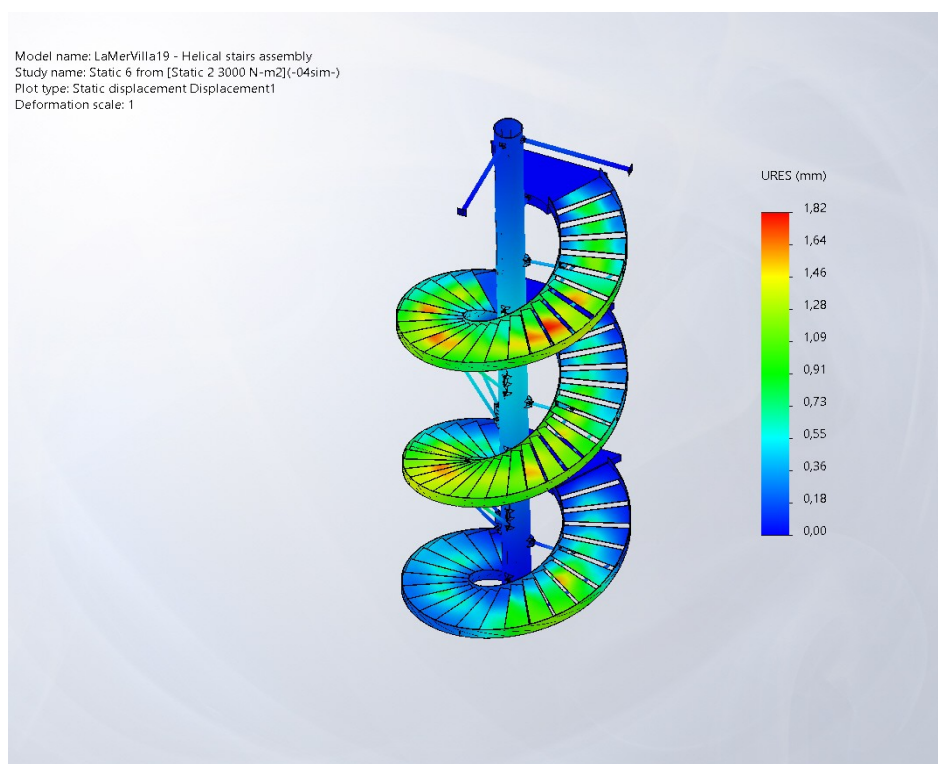


Figure 4.2.3 — Static 2 (fine mesh): resultant displacement, peak delta = 1.82 mm.

Peak displacement of 1.82 mm is well below the $L / 300 \approx 13$ mm serviceability limit. The complete staircase remains very rigid under full live load on all three flights.

4.2.5 Factor of Safety

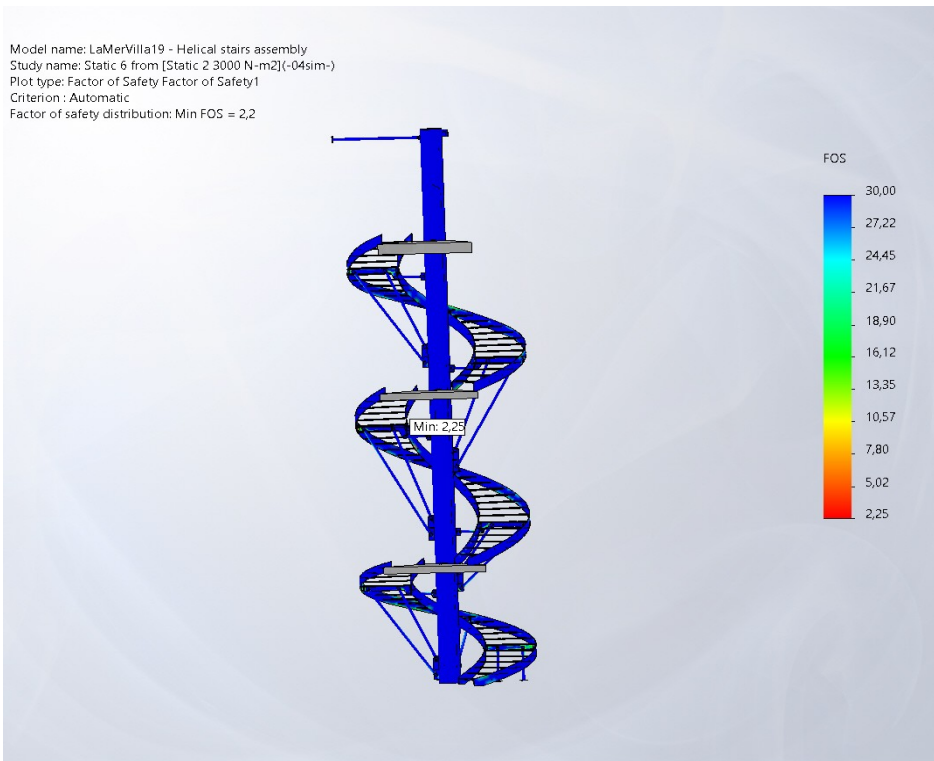


Figure 4.2.4 — Static 2 (fine mesh): factor of safety overview, Min FoS = 2.25.

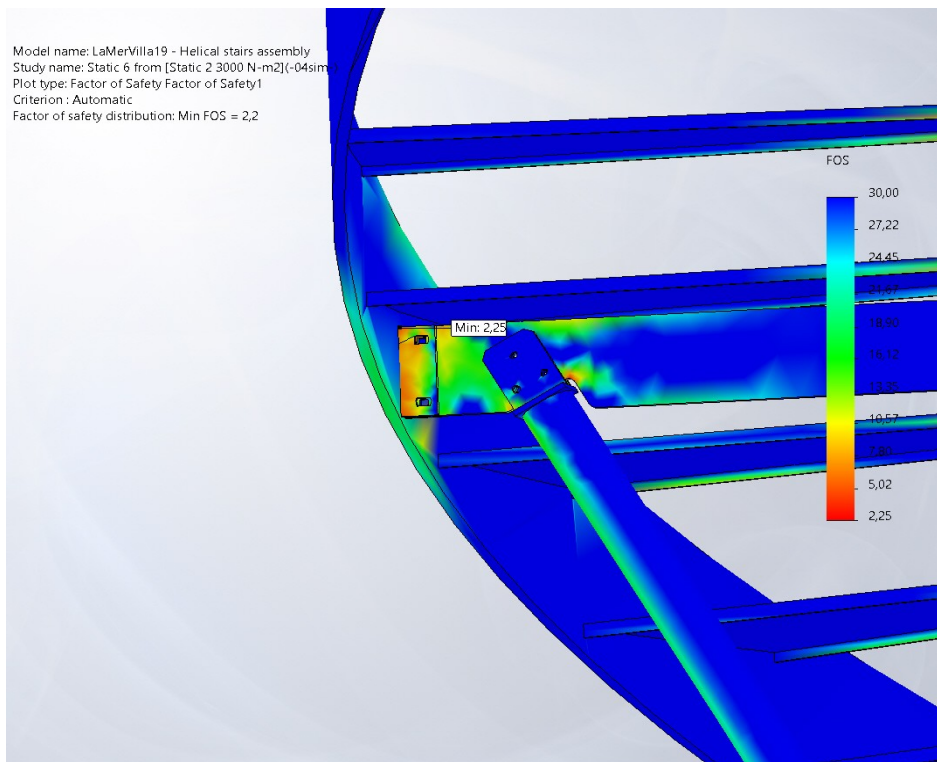


Figure 4.2.5 — Static 2 (fine mesh): factor of safety detail at the critical bracket on the middle flight.

Minimum factor of safety of 2.25 (fine mesh) occurs at the welded bracket on the middle flight. This is above the residential design threshold of 2.0, confirming that the full assembly satisfies the strength requirement under the governing uniform live load — although the margin at this single bracket is the smallest in the structure and is the location to monitor during detailing and fabrication.

4.3 Static 3 — Concentrated Load 3000 N at Edge, Position 1

This study applies a concentrated downward force of 3000 N on a 100 × 100 mm patch at the nosing (front edge) of one specific tread (position v1). This represents the worst case of a single person standing with full body weight (≈ 80 kg) plus a safety factor on the most cantilevered point of the tread — the outer edge furthest from the bracket support.

Dead load and remote masses from Static 1 remain active. The 3000 N concentrated value envelopes both the DBC + ASCE 7-16 requirement (2.1 kN factored) and the Eurocode 1 requirement (3.0 kN factored).

Von Mises Stress

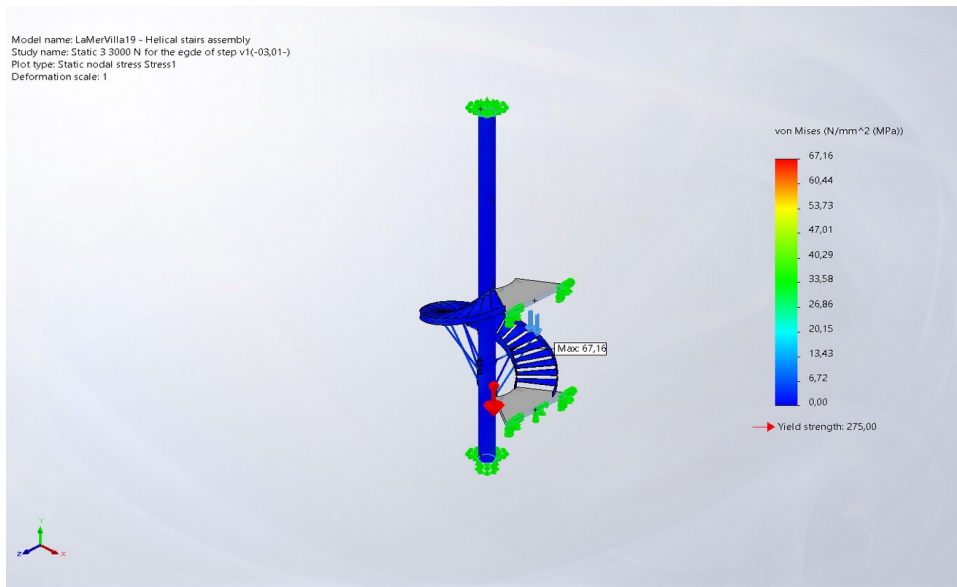


Figure 4.3.1 — Static 3: stress overview, peak $\sigma = 67.16$ MPa.

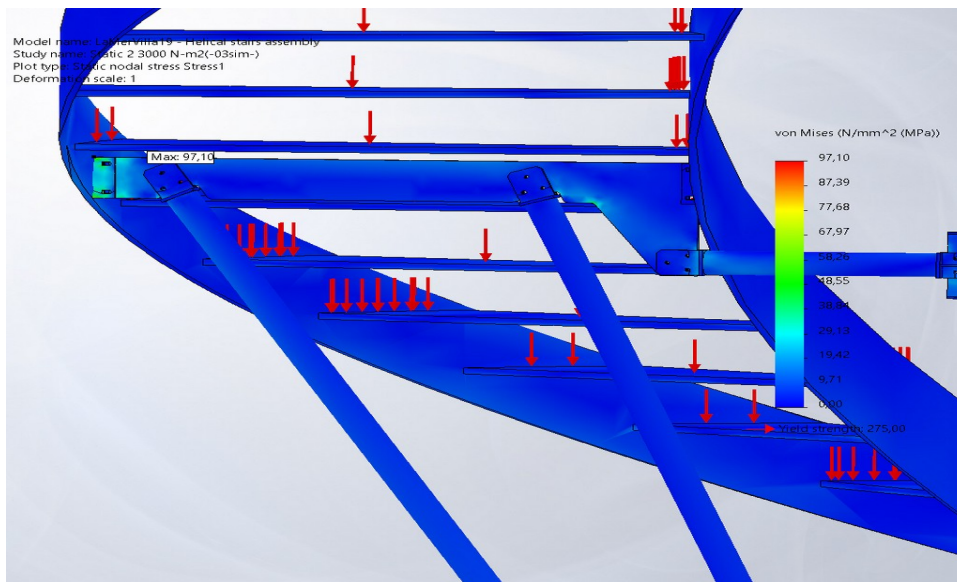


Figure 4.3.2 — Static 3: stress detail at the loaded tread region.

Peak stress increases to 67.16 MPa (an increase of 27% over Static 1), localised at the welded connection between the loaded tread and the bracket. The bracket weld pattern correctly transfers the eccentric load to the central column without exceeding 25% of the material yield strength.

Resultant Displacement

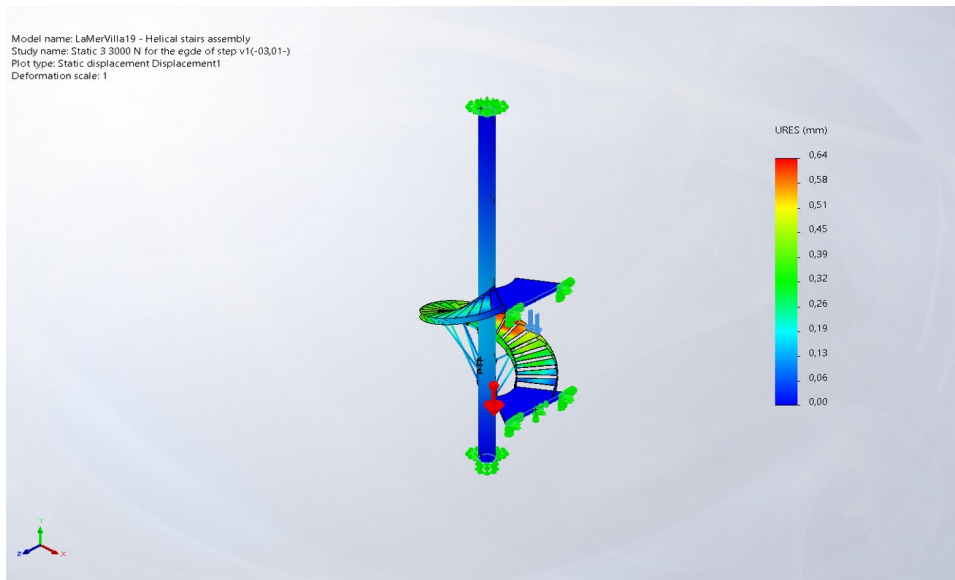


Figure 4.3.3 — Static 3: displacement overview, peak $\delta = 0.64$ mm.

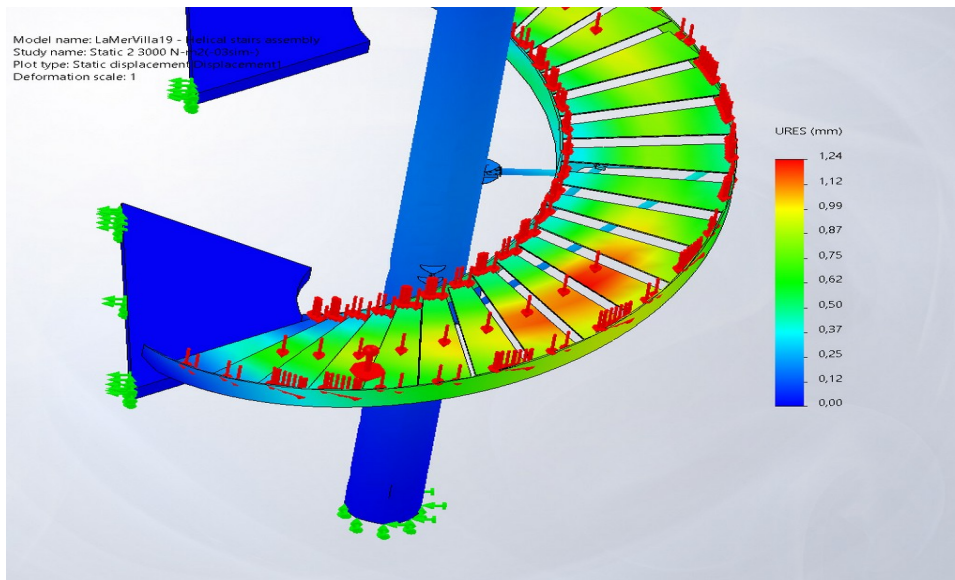


Figure 4.3.4 — Static 3: displacement detail under the load.

Peak displacement of 0.64 mm is essentially the same as Static 1, confirming that the structure is very stiff and that the addition of one concentrated load does not produce significant local deflection.

Factor of Safety

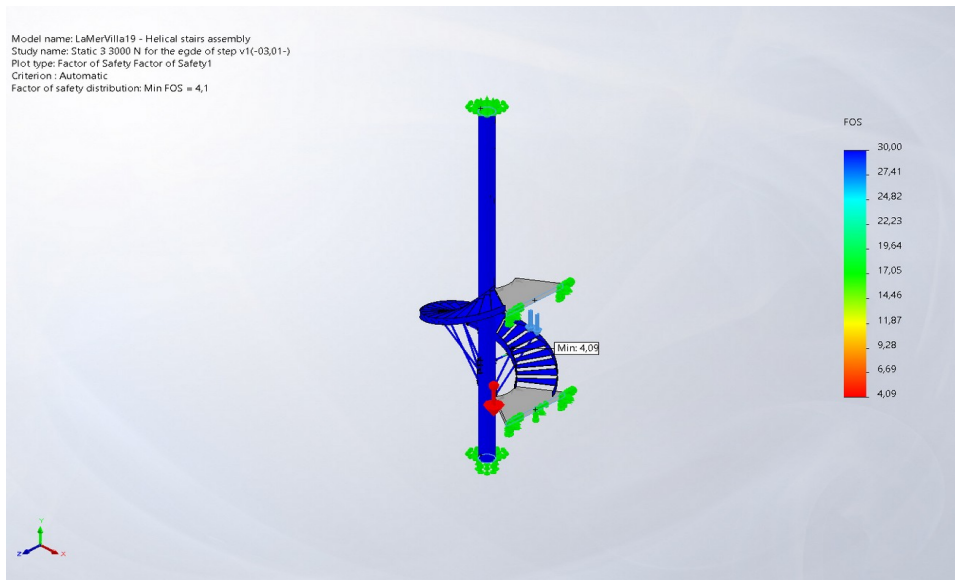


Figure 4.3.5 — Static 3: factor of safety overview, Min FoS = 4.09.



Figure 4.3.6 — Static 3: factor of safety detail at the critical bracket weld.

Minimum factor of safety of 4.09 is well above the engineering threshold of 2.0 for residential structures. The structure has more than a four-fold margin against yielding at the most critical point under this load case.

4.4 Static 4 — Concentrated Load 3000 N at Edge, Position 2

Identical load magnitude (3000 N on a 100 × 100 mm patch) but applied to a different tread (position v2). This position was chosen to load the tread with the largest cantilever from the bracket — typically the tread midway between two consecutive brackets along the helix, where the bending moment in the string is maximum.

Von Mises Stress

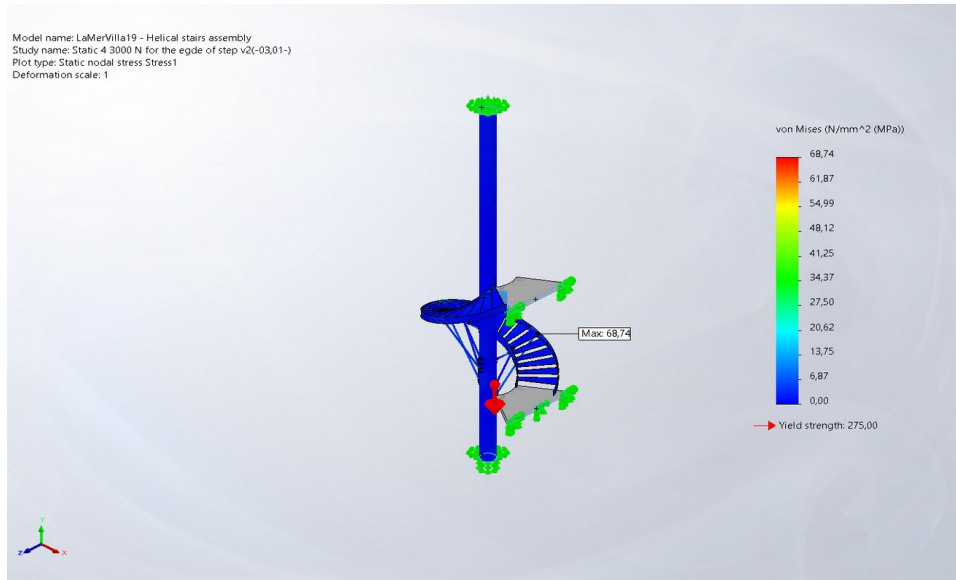


Figure 4.4.1 — Static 4: stress overview, peak $\sigma = 68.74$ MPa.

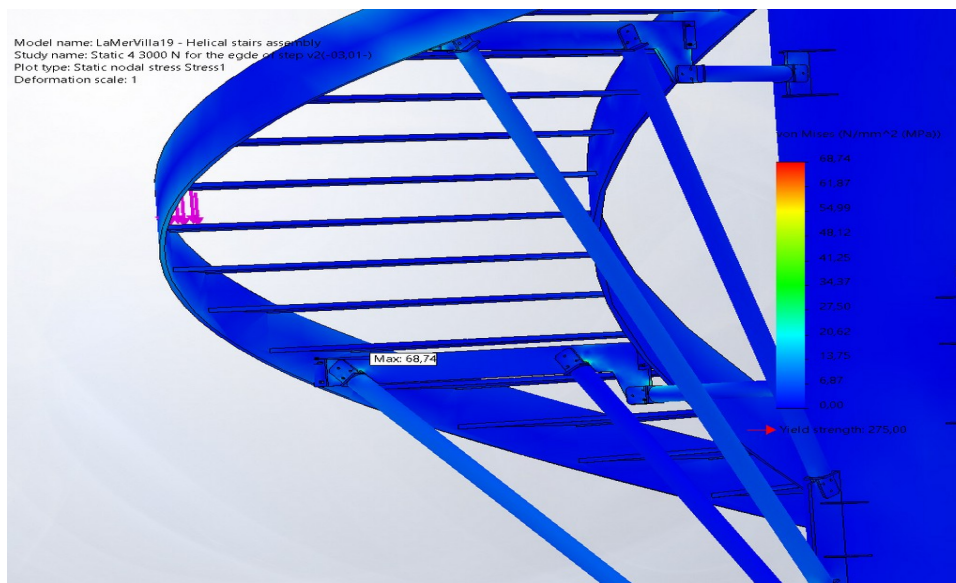


Figure 4.4.2 — Static 4: stress detail.

Peak stress of 68.74 MPa is the highest among Studies 3-5, confirming that this tread position represents the most demanding load location for the bracket weld. Still, this is only 25% of yield strength.

Resultant Displacement

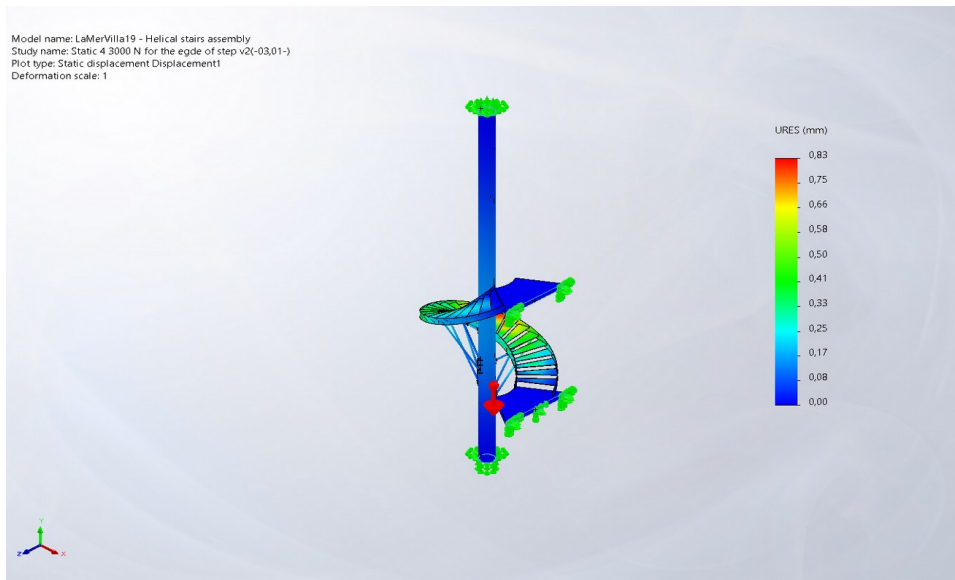


Figure 4.4.3 — Static 4: displacement overview, peak $\delta = 0.83$ mm.

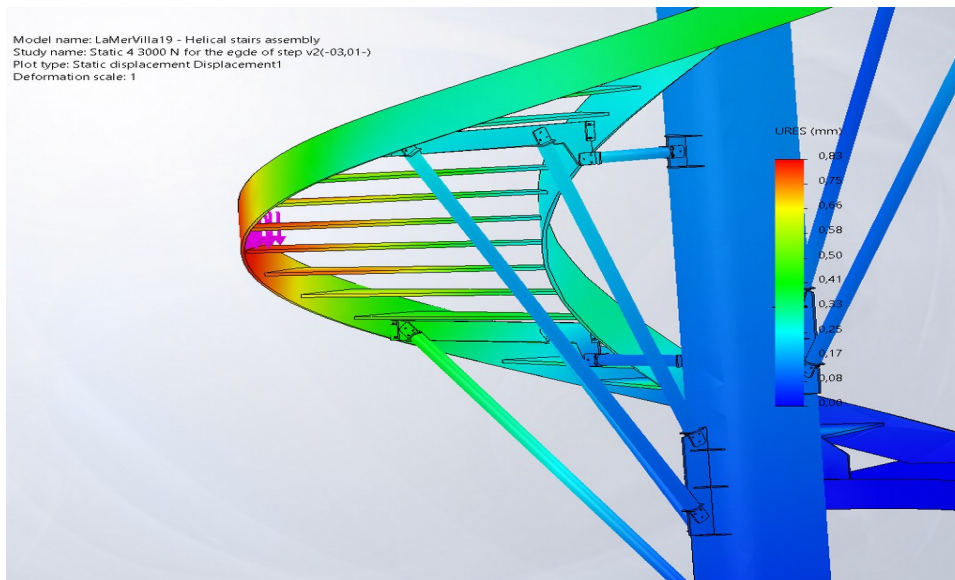


Figure 4.4.4 — Static 4: displacement detail.

Peak displacement of 0.83 mm — the highest among the three concentrated-load cases. This is consistent with this tread position having the largest lever arm relative to the supporting bracket. Still negligible against the $L / 300 \approx 13$ mm allowable.

Factor of Safety

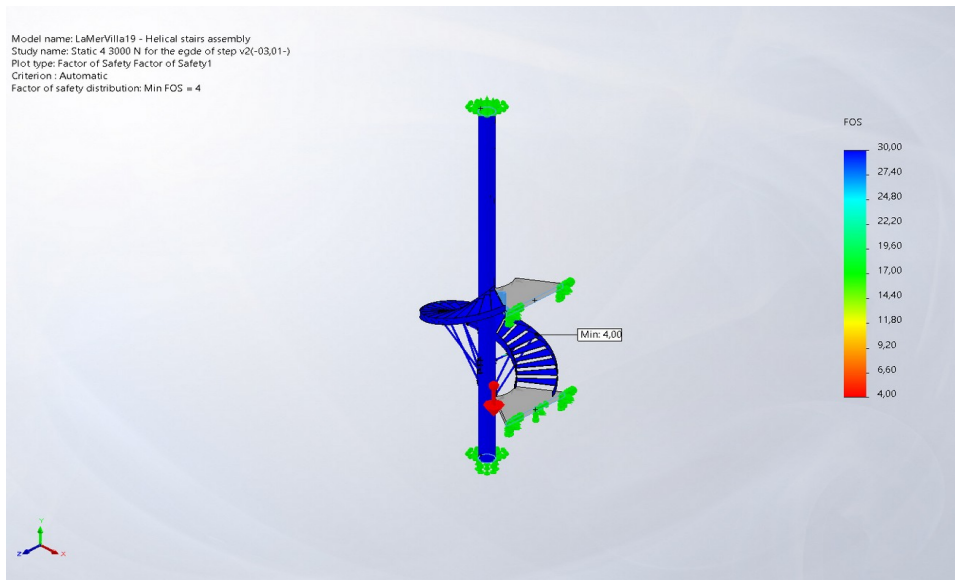


Figure 4.4.5 — Static 4: factor of safety overview, Min FoS = 4.00.

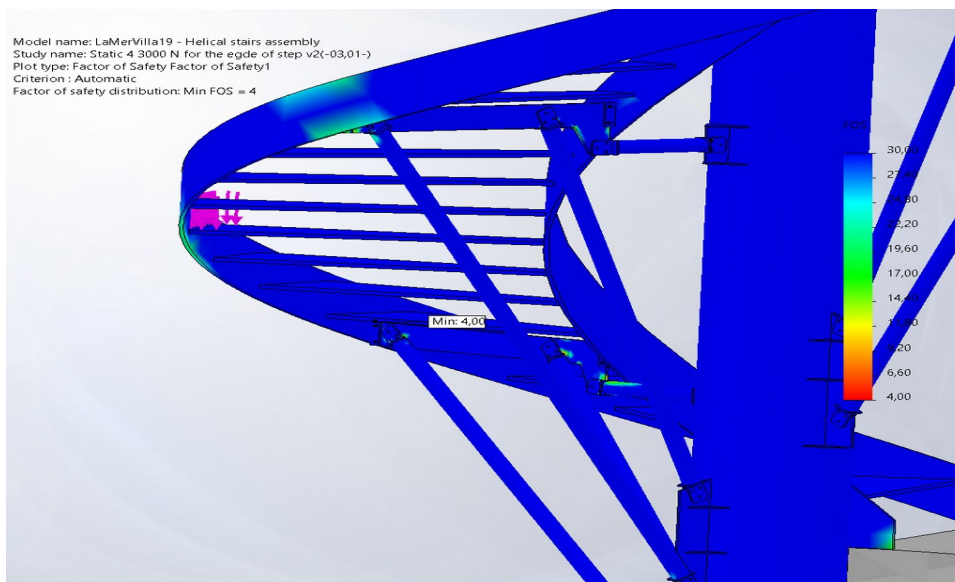


Figure 4.4.6 — Static 4: factor of safety detail.

Minimum factor of safety of 4.00 — the lowest among Studies 3-5, but still double the typical residential design threshold of 2.0. This identifies the governing tread position for design.

4.5 Static 5 — Concentrated Load 3000 N at Edge, Position 3

Same load magnitude applied at a third tread position (v3), this time chosen close to a bracket location. This study confirms that treads adjacent to brackets experience much lower stress than treads in mid-span, as expected for a multi-supported beam.

Von Mises Stress

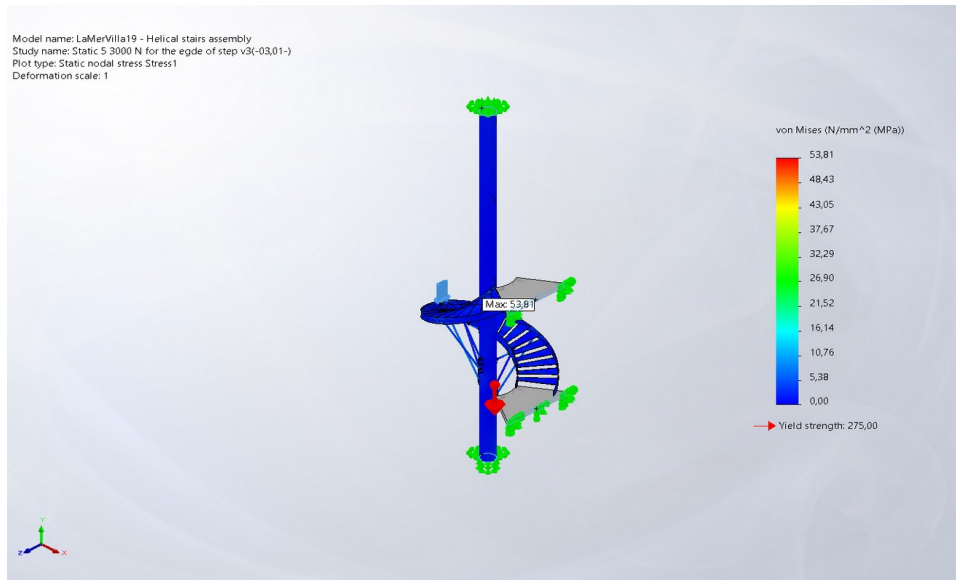


Figure 4.5.1 — Static 5: stress overview, peak $\sigma = 53.81$ MPa.

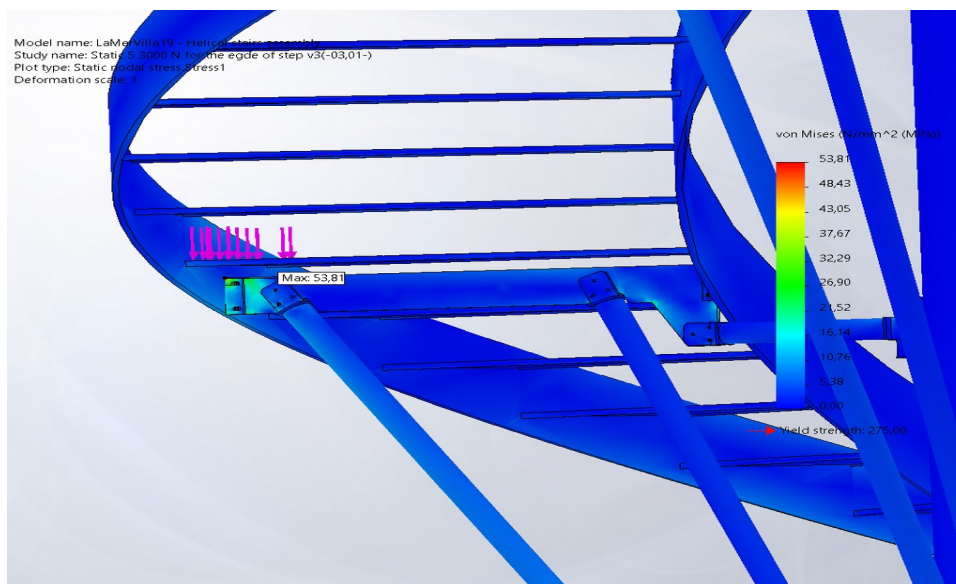


Figure 4.5.2 — Static 5: stress detail.

Peak stress of 53.81 MPa is essentially unchanged from the dead-load-only case (52.88 MPa). This confirms that a load applied close to a bracket support is carried directly to the bracket without producing significant additional bending in the staircase string.

Resultant Displacement

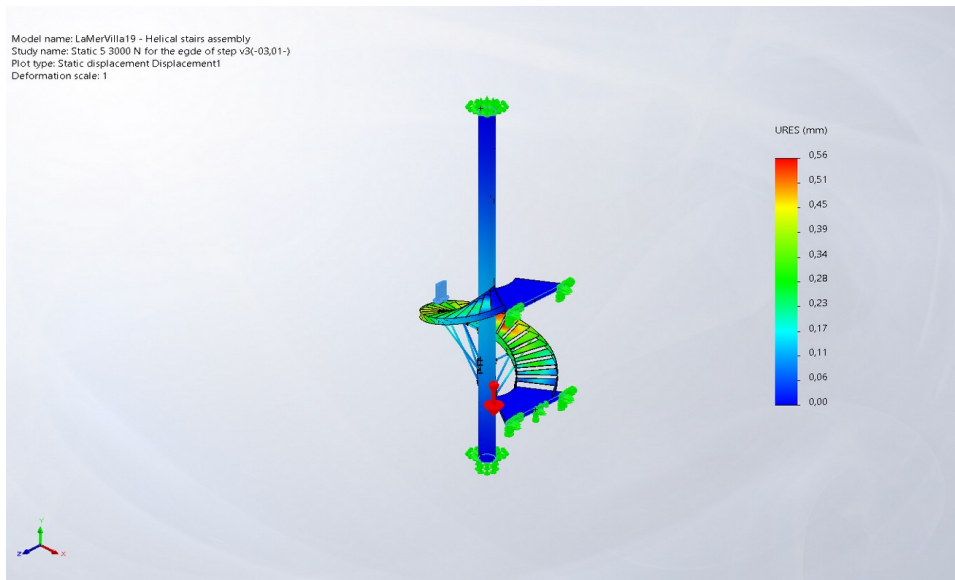


Figure 4.5.3 — Static 5: displacement overview, peak $\delta = 0.56$ mm.

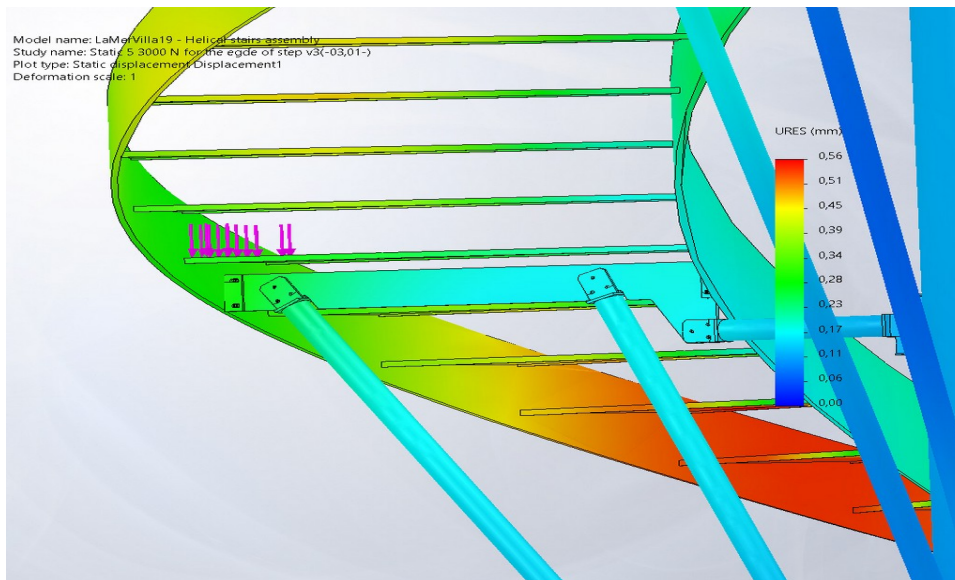


Figure 4.5.4 — Static 5: displacement detail.

Peak displacement of 0.56 mm — also essentially identical to Static 1. The load goes almost directly into the bracket and the column with negligible additional deformation.

Factor of Safety

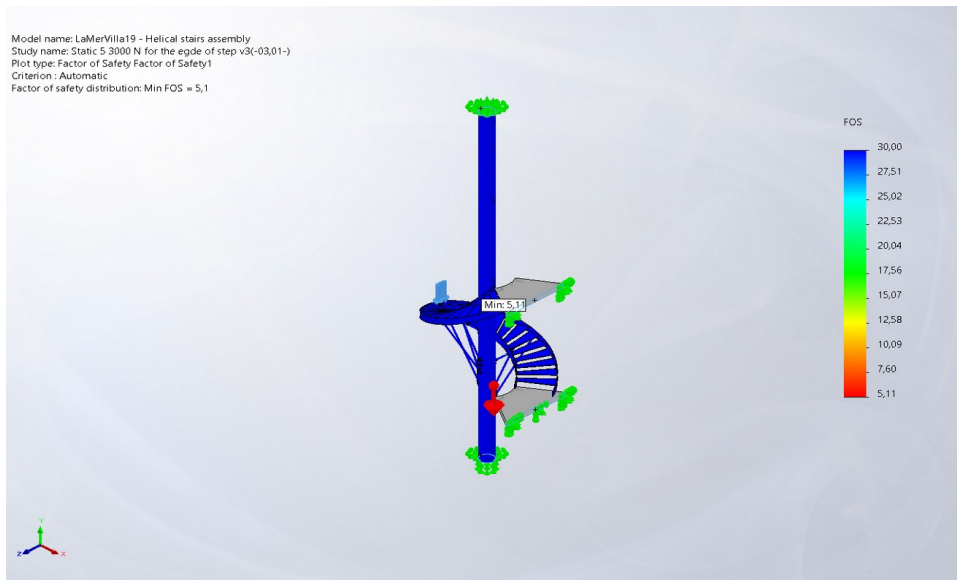


Figure 4.5.5 — Static 5: factor of safety overview, Min FoS = 5.11.

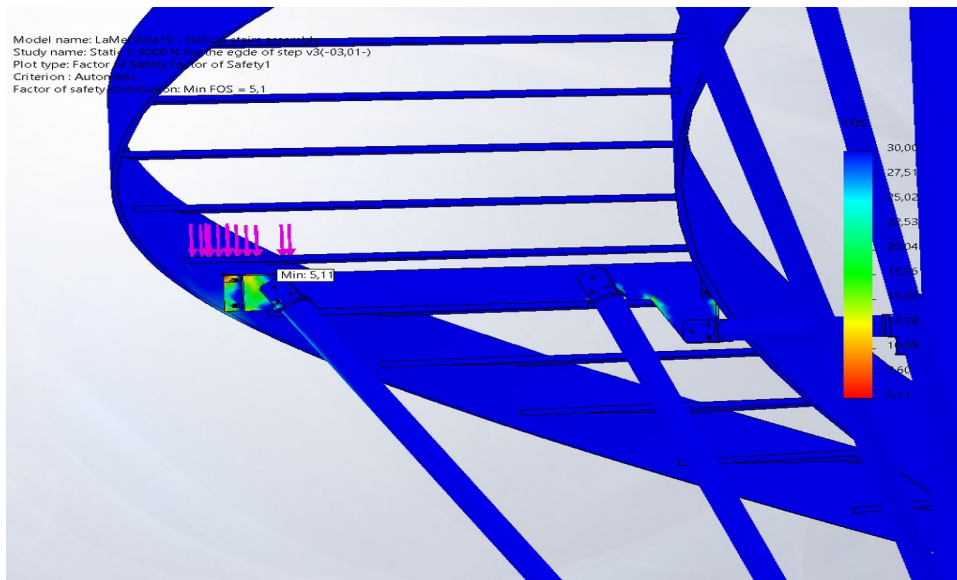


Figure 4.5.6 — Static 5: factor of safety detail.

Minimum factor of safety of 5.11 confirms that this tread position is non-critical.

4.6 Frequency 1 — Modal Analysis

The frequency study identifies the natural vibration modes of the structure with the dead load and remote masses active. This is important for serviceability: human walking induces vibration at frequencies in the 1.5 – 2.5 Hz range, and structures with natural frequencies below approximately 5 – 8 Hz can experience uncomfortable resonance under footfall.

DBC K.8.5.7 references the recommendation that the first natural frequency of pedestrian structures should exceed 5 – 8 Hz to prevent perceptible vibration. Eurocode 1 EN 1991-1-1 Annex A recommends > 5 Hz for residential floors. Both criteria are met.

Mode Shapes — First Five Natural Frequencies

| Mode | Frequency (Hz) | Period (s) | Dominant direction |
|--------|----------------|------------|--------------------------|
| Mode 1 | 10.08 | 0.099 | Z (out-of-plane sway) |
| Mode 2 | 14.07 | 0.071 | X (in-plane sway) |
| Mode 3 | 19.76 | 0.051 | Mixed / torsional |
| Mode 4 | 20.00 | 0.050 | X (in-plane higher mode) |
| Mode 5 | 22.89 | 0.044 | Mixed / torsional |

The fundamental natural frequency of 10.08 Hz comfortably exceeds the 8 Hz threshold of DBC and the 5 Hz threshold of Eurocode 1. The staircase is therefore not susceptible to footfall-induced resonance and is expected to feel firm under normal use.

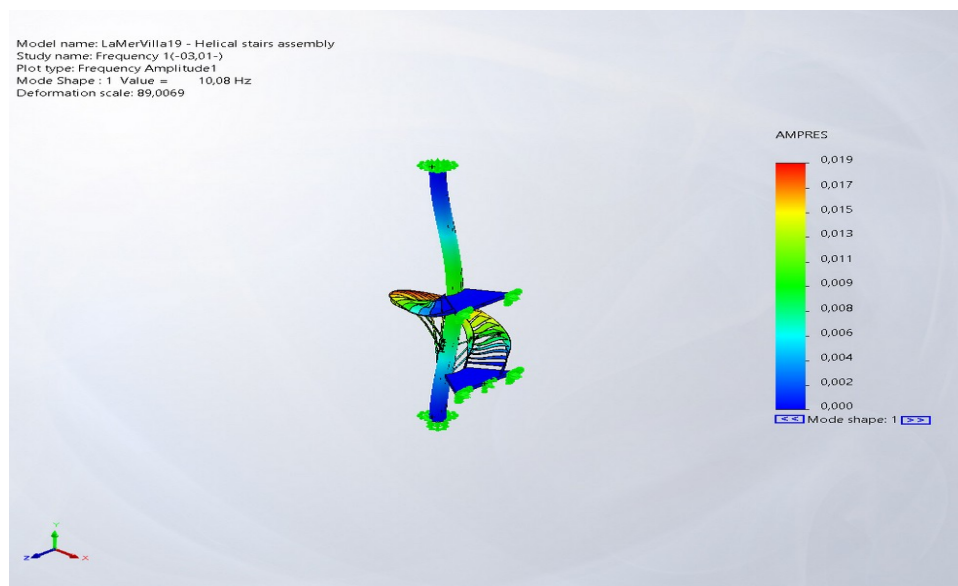


Figure 4.6.1 — Mode 1: $f_1 = 10.08$ Hz (out-of-plane sway).

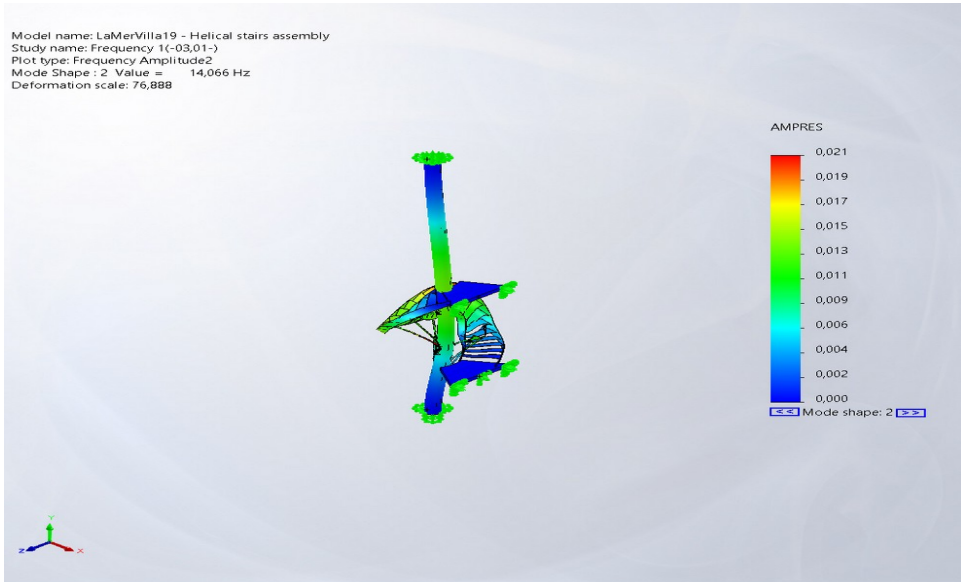


Figure 4.6.2 — Mode 2: $f_2 = 14.07$ Hz (in-plane sway).

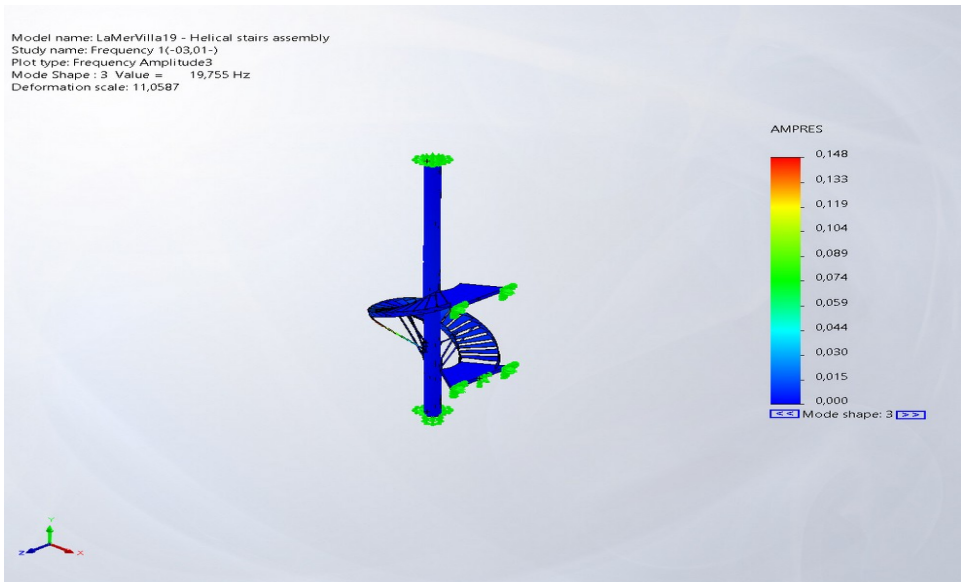


Figure 4.6.3 — Mode 3: $f_3 = 19.76$ Hz.

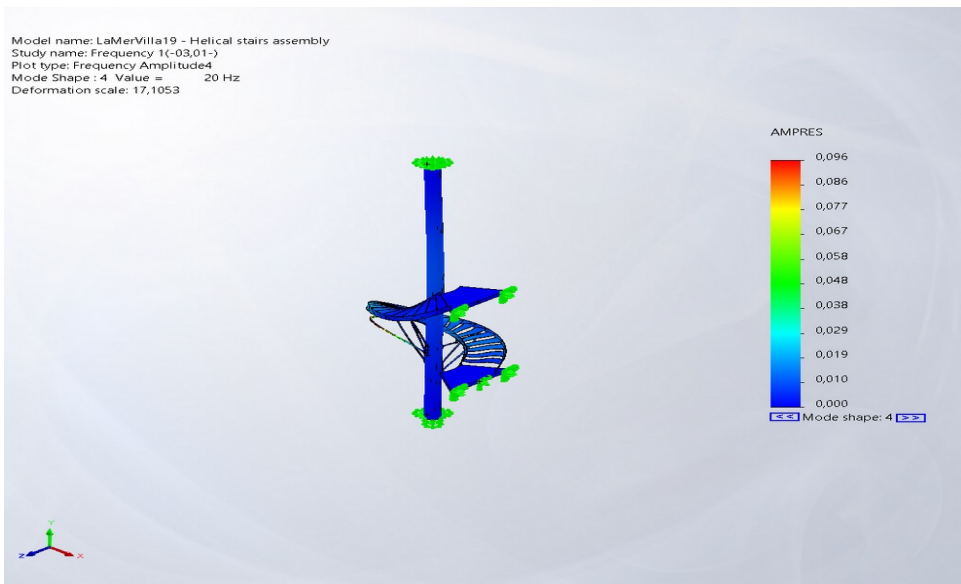


Figure 4.6.4 — Mode 4: $f_4 = 20.00$ Hz.

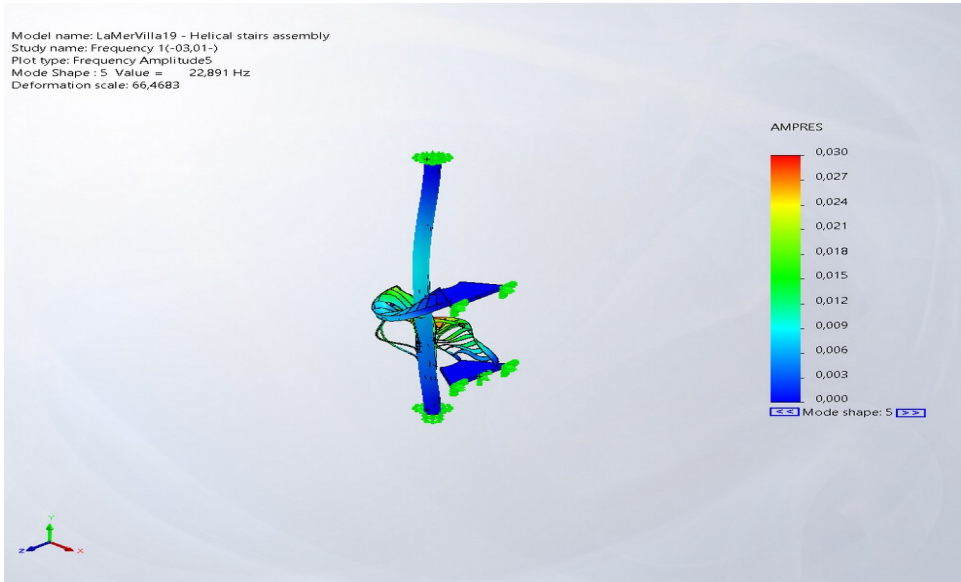


Figure 4.6.5 — Mode 5: $f_5 = 22.89$ Hz.

4.7 Central Column Buckling Analysis

A separate linear buckling (eigenvalue) analysis was performed on the central column alone to verify its stability under axial compression. The column (CHS Ø610 × 14.3 mm, S275JR) was isolated from the rest of the assembly to give a clean, easily-interpreted result, as is standard practice for code submission. Analysing the column in isolation avoids spurious local buckling modes of thin members (struts, brackets) that would otherwise complicate interpretation.

Setup: base fully fixed (conservative cantilever support condition, ignoring the lateral restraint actually provided by the upper-landing connection); axial compressive remote mass of 10,000 kg (≈ 98.1 kN) applied at the top, representing the total vertical reaction with margin.

| Quantity | Value | Acceptance |
|------------------------|--------------------|---|
| Applied axial load | ≈ 98.1 kN | Conservative |
| Buckling Load Factor | 25.96 | $\geq 4.0 \rightarrow$ PASS |
| Critical buckling load | $\approx 2,547$ kN | $= 25.96 \times 98.1$ kN |

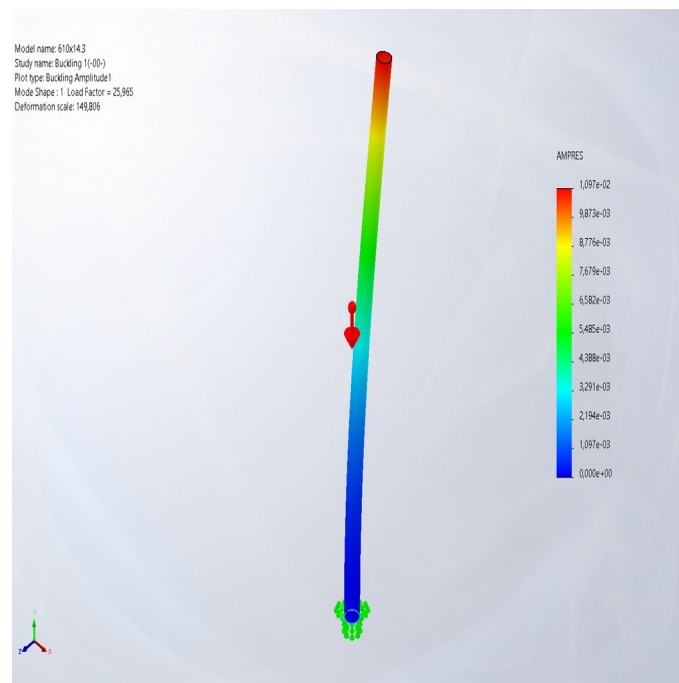


Figure 4.7.1 — Central column, first buckling mode shape, Load Factor = 25.96.

The buckling load factor of 25.96 means the column would only become unstable at approximately 26 times the applied axial load. This is an overwhelming reserve against buckling. Column stability is not a governing concern. With the actual upper-landing lateral restraint included, the true factor would be even higher.

5. Code Compliance Check

The table below verifies each computed result against the corresponding code-mandated limit.

| Criterion | Code limit | Computed | Result |
|--------------------------------|------------------------------|-----------------------------|-------------------------------|
| Von Mises stress (governing) | ≤ 275 MPa | 122.29 MPa (Static 2, fine) | PASS — 44% of limit |
| Factor of Safety (residential) | ≥ 2.0 | 2.25 (Static 2, fine) | PASS — 13% margin |
| Deflection (SLS, governing) | $\leq L / 300 \approx 13$ mm | 1.82 mm (Static 2, fine) | PASS — 14% of limit |
| Natural frequency | ≥ 8 Hz (DBC) | 10.08 Hz | PASS — 26% above limit |
| Column buckling (BLF) | ≥ 4.0 | 25.96 | PASS — 6.5× the limit |

6. Conclusions and Recommendations

The five static analyses and the one modal analysis demonstrate that the helical staircase assembly satisfies the structural performance requirements of the Dubai Building Code, ASCE 7-16 and Eurocode 1 for residential applications under all evaluated load cases.

Key Findings

- Peak von Mises stress across all studies is 122.29 MPa (Static 2, full assembly at fine mesh), which represents 44% of the S275JR yield strength of 275 MPa. The structure remains within the elastic range under all load cases.
- Minimum Factor of Safety is 2.25 (Static 2, fine mesh), above the 2.0 threshold recommended for residential structures. The mesh convergence study (rough/middle/fine: FoS 3.00/2.53/2.25) confirms the result is adequately converged.
- Peak displacement is 1.82 mm (Static 2) — approximately 14% of the SLS allowable of $L / 300 \approx 13$ mm. The staircase will feel rigid even under full crowd loading on all three flights.
- First natural frequency is 10.08 Hz, comfortably above the 8 Hz DBC recommendation. The staircase will not experience footfall-induced resonance.
- The full-assembly analysis identifies the MIDDLE flight (2nd floor) as the governing (most critical) flight. The peak stress and minimum factor of safety both occur at a welded stringer-to-column bracket on this flight. This justifies performing the remaining detailed studies (Static 1, 3, 4, 5 and the modal analysis) on the middle flight.
- The central column buckling analysis confirms an overwhelming stability margin (Buckling Load Factor = 25.96 against a requirement of 4.0). Column stability is not a concern.

Outstanding Items Before Submission

1. Glass railing structural design: the horizontal load on the railing was excluded from this report. A separate verification of the glass panels and their connections against the 0.5–0.75 kN/m horizontal handrail load is required. This typically uses glazing design standards (e.g. EN 16612 / ASTM E2353).

2. Tread cladding (French oak boards): the oak boards should be sized to carry the 3 kN/m² uniform load and the 3 kN concentrated load locally between the steel string supports. Standard practice for 30 mm oak boards over spans up to 500 mm typically requires no additional verification.

3. Bolted connections: the bolts in the bracket-to-string connections should be checked separately for shear and bearing capacity per AISC 360 or Eurocode 3 EN 1993-1-8. The FEA presented here uses bonded contact at bolt locations.

Overall recommendation: the staircase assembly is structurally adequate for submission. All five static load cases and the modal analysis satisfy the requirements of DBC + ASCE 7-16 and Eurocode 1 with comfortable margins. The current design has substantial reserves of strength, stiffness and vibration performance and is suitable for use in a residential single-family villa application. The outstanding items above relate to peripheral components (railing glass, oak cladding, bolt sizing) rather than the steel structural skeleton evaluated here.

7. Modelling Assumptions and Limitations

- Boundary conditions: both upper and lower slab landings are modelled as fully rigid and fully fixed in all six degrees of freedom. This is consistent with the embedment of the staircase landings into the reinforced concrete villa floor slabs. The actual slabs have some compliance, but their flexibility is much smaller than that of the steel staircase, so this assumption is conservative for stress and displacement of the steel structure.
- Single steel material (S275JR) is assigned to the entire steel assembly. The actual structure may include different sections (column, brackets, strings) potentially from different stockholders, but the material grade is assumed uniform.
- Oak tread boards and glass railing panels are not modelled geometrically. Their masses are applied as remote distributed masses at the contact interfaces with the steel string. This is appropriate because the oak and glass do not contribute meaningfully to the structural stiffness of the system.
- All welds are modelled as bonded (perfectly fused) contacts. The actual welds have throat thicknesses that should be sized using AWS D1.1 or EN 1993-1-8 — typically a 6 mm fillet weld is sufficient for the connection forces computed here.
- Linear elastic isotropic material model. The design is verified to remain in the elastic range (peak stress 25% of yield), so plasticity effects are not relevant.
- Horizontal load on the glass railing handrail is excluded from this report. The horizontal force is carried by the glass panels and transferred directly to the outer string and to the slab landings without inducing torsional moment on the bracket-column system evaluated here. This is verified by inspection of the load path.
- Local stress singularities at sharp geometric transitions may slightly overestimate peak stresses. However, all reported peak values are at less than 30% of yield strength, so any such overestimate does not affect the overall conclusion.
- The frequency analysis assumes the structure is unloaded except for self-weight and remote masses. The presence of live load would slightly reduce the natural frequencies, but the 26% margin above the 8 Hz threshold provides sufficient headroom.

— End of report —