

Types of FA (Finite Automaton) :-

There are two types of FA -

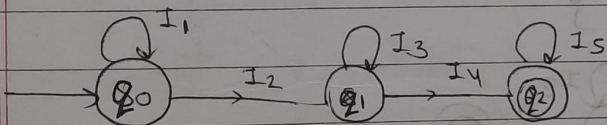
- (i) DFA : Deterministic finite Automata
- (ii) NFA or NFA : Non-deterministic FA.

DFA :- It is a special case of FSM, where from each state there will be unique transition for any input symbol.

Technical Representation of DFA :-

$$\delta(Q \times \Sigma) \rightarrow Q$$

For deterministic automaton (DFA), the outcome is a state, i.e. an element of Q ;



Transition Table :-

δ	I_1	I_2	I_3	I_4	I_5
$\rightarrow Q_0$	Q_0	Q_1	ϕ	ϕ	ϕ ← Phi
Q_1	ϕ	ϕ	Q_1	Q_2	ϕ
Q_2	ϕ	ϕ	ϕ	ϕ	Q_2

NDFA / NFA: It is a special case of FSM, where exist some state form which two or more transition are possible for some input symbol, which is called as NFA / NDFA.

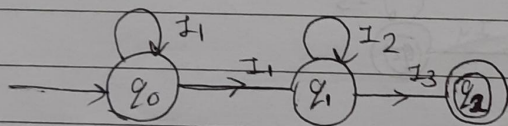
Technical Representation of NDFA:-

$$S(Q \times \Sigma) \rightarrow 2^Q$$

2^Q which is the power set of Q , the set of all subsets of Q ;

$$Q = \{q_0, q_1, q_2\}$$

$$2^Q = \{ \{ \emptyset \}, \{q_0\}, \{q_1\}, \{q_2\}, \{q_0, q_1\}, \{q_1, q_2\}, \{q_2, q_0\}, \{q_0, q_1, q_2\} \}$$



Transition Table:-

S	I ₁	I ₂	I ₃
→ q ₀	q ₀ q ₁	∅	∅
q ₁	∅	q ₁	q ₂
q ₂	∅	∅	∅

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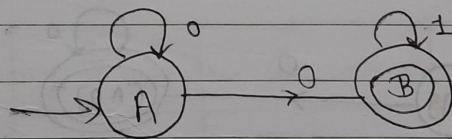
Equivalence of DFA and NFA :-

NFA TO DFA CONVERSION :-

Rules :-

- (1) Copy initial state transition as it is into new DFA table.
- (2) All multiple states are written in square bracket [].
- (3) All newly generated o/p states must be considered for making new transition once.
- (4) Repeat step (3) till all newly generated o/p states are diverted into transition column.
- (5) For final state we always check possible combination of available final state.
- (6) If any state does not give any o/p then we mark a dash (-) in o/p.
- (7) Define the DFA & draw transition diagram.

1. Q :-

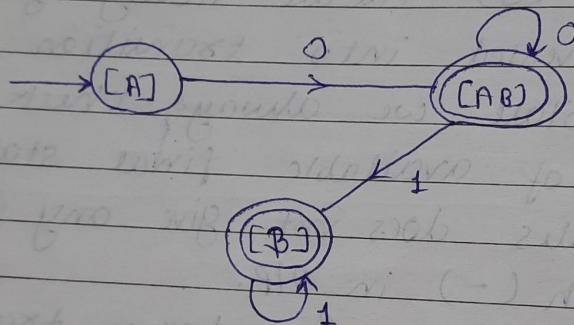


Sol :- Transition Table of NFA :-

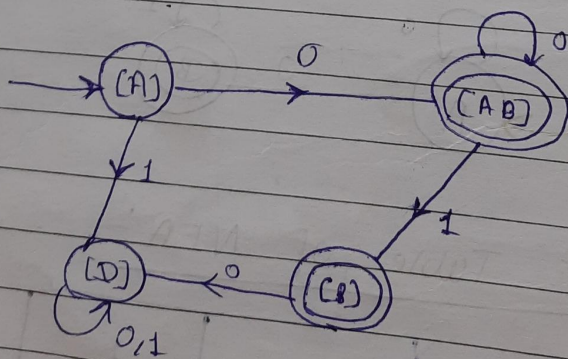
S	0	1
→ A	AB	∅
B	∅	B

Transition Table of DFA :-

S	0	1
$\rightarrow [A]$	$[AB]$	-
$[AB]$	$[AB]$	$[B]$
$[B]$	-	$[B]$



This is required DFA.



Here, D is dummy state.

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