# PAPER : IIT-JAM 2005
## BIOTECHNOLOGY-BT

**INSTRUCTIONS:**

(*i*) Each question has **4 choices** for its answer: (a), (b), (c) and (d). Only **ONE** of them is correct answer.

(*ii*) For each question, you will be awarded **3 (three)** marks, if you have darkened only one bubble corresponding to the correct answer.

(*iii*) In case you have not darkened any bubble for a question, you will be awarded **0 (zero)** mark for that question.

(*iv*) In all other cases, you will be awarded **–1 (minus one)** mark for the question.

1. In a chemical synapse, receptors for neurotransmitters are found on
   (a) presynaptic membranes
   (b) postsynaptic membranes
   (c) synaptic vesicles
   (d) myelin sheaths enveloping axons

2. During an allergic immune response, histamine is released from
   (a) B lymphocytes
   (b) T lymphocytes
   (c) mast cells
   (d) special Lymphocytes that also secrete IgE

3. Prostaglandins are biologically active molecules that are
   (a) monocyclic
   (b) bicyclic
   (c) tricyclic
   (d) polycyclic

4. When animal cells are placed in a hypotonic solution such as distilled water, they swell and burst due to
   (a) diffusion
   (b) osmosis
   (c) active transport
   (d) pinocytosis

5. Identify the hormone secreted by the pituitary gland that causes the smooth muscle of the uterus to contract during parturition in mammals
   (a) Vasopressin
   (b) Oxytocin
   (c) Prolactin
   (d) Gonadotropins

6. How many antigen-binding sites does a pentameric IgM molecule contain?
   (a) Two
   (b) Five
   (c) Ten
   (d) Fifteen

7. Identify the character that is lost by an animal cell when it gets transformed into a cancer cell
   (a) Differentiation
   (b) Contact inhibition
   (c) Regeneration
   (d) Totipotency

8. The correct match between **Group I** and **Group II** is

   | **Group I** | **Group II** |
   |---|---|
   | P. Nucleotide | 1. Ascorbic acid |
   | Q. Amino acid | 2. Adenosine triphosphate |
   | R. Fatty acid | 3. Aspartic acid |
   | S. Vitamin | 4. Gluconic acid |
   | | 5. Palmitic acid |
   | | 6. Uric acid |

   (a) P-6, Q-3, R-4, S-1
   (b) P-2, Q-3, R-5, S-4
   (c) P-2, Q-3, R-5, S-1
   (d) P-6, Q-4, R-3, S-1

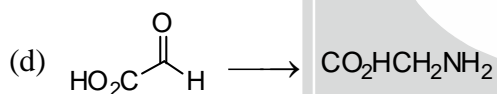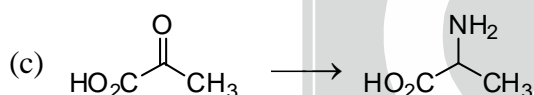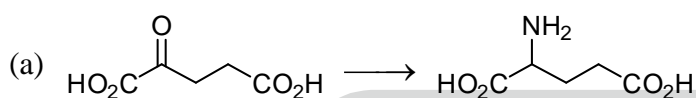9. The correct match between **Group I** and **Group II** is

   | **Group I** | **Group II** |
   |---|---|
   | P. Neurotransmitter | 1. Acetylcholine |
   | Q. Hormone | 2. Papain |
   | R. Second messenger | 3. Interferon |
   | S. Enzyme | 4. Streptomycin |

5. cAMP

6. Ecdysone

(a) P-1, Q-6, R-5, S-2                 (b) P-6, Q-5, R-3, S-2

(c) P-3, Q-6, R-1, S-4                 (d) P-1, Q-3, R-5, S-2

10. Enzymes catalyze chemical reactions by

(a) decreasing the activation energy

(b) increasing the activation energy

(c) providing a buffering effect

(d) regulating the concentration of substrates at optimal temperature and pH

11. In a typical ecosystem, biomagnification occurs at the highest level in

(a) primary producers                 (b) secondary producers

(c) primary consumers                 (d) secondary consumers

12. Western blot is used for the identification of

(a) monosaccharides                   (b) RNA

(c) DNA                               (d) proteins

13. Which of the following does **NOT** form the basis of an antigen-antibody binding?

(a) Hydrogen bond                     (b) Ionic interactions

(c) Covalent bond                     (d) Hydrophobic interactions

14. Myoglobin contains multiple distinct epitopes but only a single copy of each epitope. Identify the condition under which antigen-antibody precipitation reaction would occur.

(a) When monoclonal antibody is used   (b) When specific polyclonal antiserum is used

(c) When monovalent Fab fragments are used   (d) When any of the above conditions are fulfilled

15. According to the taxanomical classifications of humans,

(a) *Homo* refers to genus and *sapeins* the species

(b) *Homo* refers to family and *sapeins* the genus

(c) *Homo* refers to order and *sapeins* the family

(d) *Homo* refers to class and *sapeins* the sub-class

16. The optical rotation of a solution of D-glucose is +52.7º. Which of the following statements applies to this solution?

(a) It is a mixture of two forms of D-glucose and both forms exhibit the same specific optical rotation

(b) It has only one form of D-glucose and all molecules have the same specific optical rotation

(c) It is a mixture of two forms of D-glucose, each of which has different specific optical rotation

(d) It is a mixture of large number of D-glucose forms, each of which has different specific optical rotation

17. The decreasing order of the melting points of the following fatty acids is

P. Stearic acid, 18:0                 Q. *Cis*-oleic acid, 18:1

R. *Trans*-oleic acid, 18:1           S. Linolenic acid, 18:3

(a) P > Q > R > S                      (b) P > R > Q > S

(c) S > R > Q > P                      (d) S > Q > R > P

18. Consider the following four statements:

    P. The solubility of a protein is lowest at its isoelectric point

    Q. At low ionic strengths, solubility of a protein increases with increasing salt concentration

    R. Tyrosine, tryptophan and phenylalanine have aromatic side chains capable of forming hydrogen bonds

    S. Oxygen binding to hemoglobin decreases when pH is increased from 7.2 to 7.6

    Of these statements,

    (a) only P and Q are correct
    (b) P, Q and S are correct
    (c) all are correct
    (d) only Q is correct

19. For the enzyme catalyzed reaction $E + S \underset{k_{-1}}{\overset{k_1}{\rightleftharpoons}} ES \xrightarrow{k_2} P$

    $k_m$ is an indicator of the affinity of enzyme to the substrate

    (a) when $k_2 \ll k_{-1}$

    (b) when $k_2 \gg k_{-1}$

    (c) when $k_2 = k_{-1}$

    (d) irrespective of the mutual relationship of the rate constants

20. Which of the following statements is FALSE?

    (a) Nitrogen fixation by the nitrogenase complex requires eight electrons

    (b) Conversion of nitrogen to ammonia ($N_2 + 3H_2 \rightarrow 2NH_3$) is an endergonic process

    (c) Certain free living aerobic bacteria are also capable of nitrogen fixation

    (d) The nitrogen fixing nitrogenase complex is oxygen-labile

21. Which of the following is **NOT** an allosteric modulator of hemoglobin?

    (a) Carbon dioxide
    (b) $H^+$
    (c) 2, 3-Bisphosphoglycerate
    (d) Carbon monoxide

22. Relative to the inter-membrane space, the mitochondrial matrix is

    (a) alkaline and has negative membrane potential

    (b) acidic and has negative membrane potential

    (c) alkaline and has positive membrane potential

    (d) acidic and has positive membrane potential

23. Among the following, the strongest oxidant is

    (a) P680.Chl$^+$
    (b) $H_2O$
    (c) P680.Chl$^+$
    (d) P700

24. One of the carbon atoms of glucose is $^{14}$C-labeled. If none of the TCA cycle intermediates are $^{14}$C-labeled after glycolysis and one cycle of Krebs cycle, the carbon atom of glucose that was labeled is

    (a) C1
    (b) C6
    (c) C2
    (d) C3

25. Which of the following statements relating to microtubules is **NOT** correct?

    (a) The plus-end of microtubule is the fast-growing end

    (b) Addition of short fragments of microtubules enhances polymerization

    (c) A microtubule with GDP-cap enters the shrinkage phase (catastrophe)

    (d) Critical concentration for polymerization is same for both plus-and minus-ends

26. Treadmilling of actin filaments refers to
    (a) net assembly at both plus-and minus-ends
    (b) net assembly at plus-end and net disassembly at minus-end
    (c) net disassembly at plus-end and net assembly at plus-end
    (d) net disassembly at both-and minus-ends

27. Which of the following vitamins becomes part of a high-energy metabolite in the cell?
    (a) Thiamine        (b) Riboflavin        (c) Pantothenate    (d) Folate

28. Which of the following four is involved in cell cycle control?
    (a) Proteolysis of cyclins             (b) Phosphorylation of cyclins
    (c) Proteolysis of cyclin-dependent kinases     (d) Dephosphorylation of cyclins

29. Which of the following is the key reaction linking carbon and nitrogen cycles?

    (a) $HO_2C-CO-CH_2-CH_2-CO_2H \longrightarrow HO_2C-CH(NH_2)-CH_2-CH_2-CO_2H$

    (b) $HO_2C-CO-CH_2-CO_2H \longrightarrow HO_2C-CH(NH_2)-CH_2-CO_2H$

    (c) $HO_2C-CO-CH_3 \longrightarrow HO_2C-CH(NH_2)-CH_3$

    (d) $HO_2C-CHO \longrightarrow CO_2HCH_2NH_2$

30. The most effective enzyme-catalyzed reaction is the one in which
    (a) $k_{cat} = 1.4 \times 10^4 \ sec^{-1}$ and $k_m = 9 \times 10^{-5}$
    (b) $k_{cat} = 1.4 \times 10^5 \ sec^{-1}$ and $k_m = 9 \times 10^{-5}$
    (c) $k_{cat} = 1.4 \times 10^3 \ sec^{-1}$ and $k_m = 9 \times 10^{-5}$
    (d) $k_{cat} = 1.4 \times 10^4 \ sec^{-1}$ and $k_m = 9 \times 10^{-4}$

31. The deoxyribonucleotides in a DNA strand are linked together covalently through
    (a) 5'-hydroxyl group of one sugar and 5'-phosphate group of the next
    (b) 2'-hydroxyl group of one sugar and 3'-hydroxyl group of the next
    (c) 3'-hydroxyl group of one sugar and 5'-phosphate group of the next
    (d) 5'-hydroxyl group of one sugar and 3'-hydroxyl group of the next

32. sno-RNAs
    (a) process and chemically modify ribosomal RNAs
    (b) are involved in telomere synthesis
    (c) are involved in splicing pre-mRNA
    (d) form the basic structure of ribosome

33. How many bands would you expect if a pentameric sample of IgM containing $\beta$-mercaptoethanol is subjected to SDS-PAGE?
    (a) 2        (b) 3        (c) 5        (d) 6

34. In DNA-gel retardation assay, which of the following complexes that are formed is analyzed?
    (a) DNA-RNA complex
    (b) DNA-DNA complex
    (c) RNA-protein complex
    (d) DNA-protein complex

35. The TATA$^A/_T$A$^A/_T$ sequence, present in the eukaryotic promoter, is recognized and initially bound by which of the following transcription factors?
    (a) TFIIA
    (b) TFIIB
    (c) TFIID
    (d) TFIIH

36. The backbone of peptidoglycan present in the bacterial cell wall is a polysaccharide consisting of repeating units of
    (a) N-acetylgalactosamine – N-acetylmuramic acid
    (b) N-acetylgalactosamine – N-acetylneuraminic acid
    (c) N-acetylglucosamine – N-acetylmuramic acid
    (d) N-acetylglucosamine – N-acetylneuraminic acid

37. Which of the following statements is true with respect to the influenza virus?
    (a) Hemagglutinin present in the virus envelope is involved in attachment of the virus to sialic acid residues of the host cell surface
    (b) Hemagglutinin present in the virus envelope is involved in the attachment of the virus to N-acetylglucosamine residues of the host cell surface
    (c) Hemagglutinin proteins form tetramers that project out from viral surface
    (d) Hemagglutinin is not a glycoprotein

38. Which one of the following causes pneumonia?
    (a) *Helicobacter pylori*
    (b) *Hemophilus influenzae*
    (c) *Vibrio fisheri*
    (d) *Naegleria fowleri*

39. Choose the right combination from the following statements with respect to proof reading activity during DNA replication.
    P. DNA polymerase activity is involved
    Q. DNA topoisomerase I activity is involved
    R. $3' \rightarrow 5'$-exonuclease activity is involved
    S. $5' \rightarrow 3'$-exonuclease activity is involved
    (a) PQ
    (b) PR
    (c) PS
    (d) QR

40. Which one of the following movements of phospholipids is catalyzed by the phospholipid translocators in the eukaryotic cell membrane?
    (a) Lateral
    (b) Flexion
    (c) Flip-flop
    (d) Rotation

41. Baculovirus vectors are used to transfer genes into
    (a) mammalian cells
    (b) plant cells
    (c) insect cells
    (d) bacterial cells

42. Choose the right combination from the following statements with respect to the amino acid activation during protein biosynthesis.
    P. A single aminoacyl-tRNA synthetase can catalyze the coupling of all amino acids to appropriate tRNAs
    Q. The energy during the activation step is provided through GTP hydrolysis
    R. The energy during the activation step is provided through ATP hydrolysis
    S. The aminoacyl-tRNA synthetase catalyzed reaction attached amino acid to the 3'-end of the tRNA.
    (a) PR
    (b) PS
    (c) QS
    (d) RS

43. The correct match between **Group-I** and **Group-II** is

    | **Group-I** | **Group-II** |
    |---|---|
    | P. DNA ligase | 1. Unwinds dsDNA into ssDNA |
    | Q. DNA primase | 2. Synthesizes small DNA fragments as primers |
    | R. DNA topoisomerase I | 3. Joins 3'-OH and 5'-phosphate ends of DNA |
    | S. DNA helicase | 4. Produces a transient single strand break in the phosphodiester backbone of DNA |
    | | 5. Synthesizes RNA primers |
    | | 6. Converts ssDNA into dsDNA |

    (a) P-3, Q-2, R-6, S-1        (b) P-3, Q-5, R-4, S-1

    (c) P-5, Q-2, R-1, S-3        (d) P-4, Q-2, R-3, S-6

44. Which of the following statements is **NOT** correct with respect to elongation step of prokaryotic protein biosynthesis?

    (a) fMet-tRNA$_f$ is recognized by EF-Tu-GTP

    (b) Binary complex of EF-Tu-GTP binds aminoacyl-tRNA to form a ternary complex

    (c) Binary complex EF-Tu-GDP is inactive

    (d) Kirromycin is an antibiotic that inhibits the function of EF-Tu

45. If the ionization energy of H is 13.59 eV, then the ionization energy of He$^+$ will be

    (a) 13.59 eV     (b) 27.18 eV     (c) $(13.59)^2$ eV     (d) 54.36 eV

46. In a $CO_2$ molecule the number of translational, rotational and vibrational degrees of freedom, respectively, is

    (a) 3, 2, 4     (b) 3, 4, 2     (c) 3, 3, 3     (d) 4, 3, 2

47. The molecule which is IR inactive and Raman active is

    (a) HCl     (b) $N_2$     (c) $SO_2$     (d) $CO_2$

48. Which of the following axis of symmetry does the tetragonal crystal possess?

    (a) Two fold     (b) Three fold     (c) Six fold     (d) Four fold

49. For which of the following reactions $\Delta H = \Delta U$

    (a) $N_2 + O_2 \rightarrow 2NO$        (b) $C + \frac{1}{2}O_2 \rightarrow CO$

    (c) $C + O_2 \rightarrow CO_2$        (d) $N_2O_4 + \frac{1}{2}O_2 \rightarrow N_2O_5$

50. Assuming that $\Delta H_{vap}$ is 540 kcal g$^{-1}$, what would be the $\Delta S$ accompanying the evaporation of one mole of water at 100°C?

    (a) 540 cal g$^{-1}$        (b) 25 cal K$^{-1}$ mol$^{-1}$

    (c) 1.45 cal K$^{-1}$ mol$^{-1}$        (d) 26.06 cal K$^{-1}$ mol$^{-1}$

51. For a reaction $2A + B \rightarrow P$, by doubling the initial concentration of both the reactants the rate increases by a factor of 8, whereas by doubling the concentration of B alone the rate increases two times. The rate law for the reaction is

    (a) $\dfrac{d[P]}{dt} = k[A][B]^2$        (b) $\dfrac{d[P]}{dt} = k[A][B]$

    (c) $\dfrac{d[P]}{dt} = k[A]^2[B]$        (d) $\dfrac{d[P]}{dt} = k[A]^2[B]^0$

52.    For the Zn-Cu cell, $E^o = 1.10V$. If the reduction potential of the $Cu^{2+}$ (aq)/Cu(s) couple is 0.34V, then that of the $Zn^{2+}$ (aq)/Zn(s) couple is

(a)  –0.76V              (b)  0.76V              (c)  1.44V              (d)  1.10V

53.    The geometry of the complex $[Ni(CN)_4]^{2-}$ is

(a)  Tetrahedral        (b)  Square planar      (c)  Octahedral         (d)  Distorted tetragonal

54.    The increasing order of stability of $O_2^{2-}$, $O_2^-$, $O_2$, $O_2^+$ species is

(a)  $O_2^+$, $O_2^-$, $O_2^{2-}$, $O_2$                           (b)  $O_2^{2-}$, $O_2^-$, $O_2$, $O_2^+$

(c)  $O_2^-$, $O_2^{2-}$, $O_2$, $O_2^+$                           (d)  $O_2^+$, $O_2^{2-}$, $O_2^-$, $O_2$

55.    The average distance of an electron from the nucleus in the ground state of hydrogen atom (in units of Bohr radius $a_0$) is

(a)  1                   (b)  2                  (c)  3/2                (d)  1/2

56.    Phthalimide on treatment with base will undergo Hoffman rearrangement to give

(a)  aniline                                    (b)  benzylamine

(c)  2-aminobenzoic acid                        (d)  3-aminobenzoic acid

57.    Which one of the following compounds is *antiaromatic*?

(a)  Cyclopentadiene                            (b)  Cyclobutadiene

(c)  Azulene                                    (d)  Cycloheptatrienyl cation

58.    Choose the correct absolute configuration for the following compound
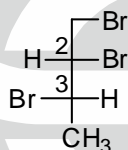


(a)  2*R*, 3*R*          (b)  2*S*, 3*R*         (c)  2*S*, 3*S*         (d)  2*R*, 3*S*

59.    Nylon-6, 6 is made from

(a)  caprolactam                               (b)  adipic acid and hexamethylenetetramine

(c)  phenol and formaldehyde                    (d)  terephthalic acid and ethylene glycol

60.    Which one of the following is not a heterocyclic amino acid?

(a)  Proline            (b)  Tyrosine           (c)  Histidine          (d)  Tryptophan

61.    Carbylamine test is usually carried out to confirm the presence of

(a)  nitro group                               (b)  primary amine

(c)  secondary amine                           (d)  tertiary amine

62.    The following reduction is best achieved by
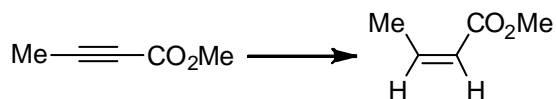


(a)  $H_2$/Pd-C                                 (b)  $H_2$/Lindlar catalyst

(c)  $LiAlH_4$                                  (d)  Na/liq. $NH_3$

63.    Which is the strongest base among the following compounds?
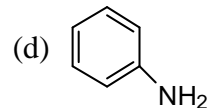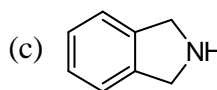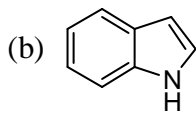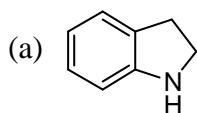
64. The correct match between **Group-I** and **Group-II** is

   **Group-I**                           **Group-II**
   P.  $AlCl_3$                           1.  Cope rearrangement
   Q.  Salicylaldehyde                    2.  $S_{N2}$ reaction
   R.  2-Allylvinylether                  3.  Friedal-Crafts reaction
   S.  2-bromobutane                      4.  Reimer-Teiman reaction
                                          5.  Claisen rearrangement
                                          6.  Kolbe reaction

   (a) P-3, Q-5, R-1, S-2                 (b) P-2, Q-4, R-5, S-6
   (c) P-3, Q-4, R-1, S-2                 (d) P-3, Q-4, R-5, S-2

65. Three lines $y = 0$, $y = x$ and $x = -4$ constitute a triangle. Its area is
   (a) 8 sq. units                        (b) 16 sq. units
   (c) −8 sq. units                       (d) −16 sq. units

66. The order and degree of the differential equation $k = \dfrac{\left\{1+\left(\dfrac{dy}{dx}\right)^2\right\}^{2/3}}{\dfrac{d^2y}{dx^2}}$ are, respectively

   (a) 2, 2            (b) 2, 3            (c) 3, 2            (d) 2, 4

67. For what value of $p$, the vectors $2i - j + k$, $i + 2j - 3k$ and $3i + pj + 5k$ are coplanar?
   (a) 4              (b) 0               (c) 22/5            (d) −4

68. If $f(x) = 3$, when $-3 \le x \le -1$

   $= -6x - 3$, when $-1 \le x \le 0$

   $= 3x - 3$, when $0 \le x \le 1$,

   then the values of $x$ for which $2f(x) + 3 = 0$ are
   (a) 1/4, 1/2                           (b) −1/4, 1/2
   (c) 1/4, −1/2                          (d) −1/4, −1/2

69. The values of $x$ in the following equation are $[x \ \ 1]\begin{bmatrix} 1 & 0 \\ -4 & -3 \end{bmatrix}\begin{bmatrix} x \\ 5 \end{bmatrix} = 6$

   (a) 7, −3          (b) −7, 3           (c) −7, −3          (d) 7, 3

70. $A$, $B$, and $C$ toss a coin in succession on the understanding that the first one to throw a head wins. The probability that $C$ wins is
   (a) 1/7            (b) 2/7             (c) 4/7             (d) 1/8

71. If $x^y = e^{x-y}$, then $\dfrac{dy}{dx}$ is

   (a) $\dfrac{\log x}{[\log(ex)]^2}$   (b) $\dfrac{\log x}{[\log(ex)]}$   (c) $\dfrac{x\log x}{[\log(ex)]^2}$   (d) $\dfrac{x\log x}{[\log(ex)]}$

72. The shortest distance between the lines $\dfrac{x-1}{2}=\dfrac{y-2}{3}=\dfrac{z-3}{4}$ and $\dfrac{x-2}{3}=\dfrac{y-4}{4}=\dfrac{z-5}{5}$ is

   (a) $1/\sqrt{6}$      (b) $5/\sqrt{6}$      (c) $11/\sqrt{6}$      (d) $15/\sqrt{6}$

73. The curves $2x^2+3y^2=1$ and $px^2+6y^2=1$ intersect orthogonally if $p$ is

   (a) 1/3      (b) 3      (c) 4      (d) 2/3

74. If the profit function $p(x)=41-24x-18x^2$, then the maximum profit that a company can make is

   (a) 49      (b) 65      (c) 33      (d) 17

75. A particle is in equilibrium under the action of three forces $P$, $Q$ and $R$. If the angle between $P$ and $Q$ is 120º and that between $Q$ and $R$ is 135º, then the ratio of their magnitudes $P : Q : R$ is

   (a) $2:\sqrt{3}+1:\sqrt{6}$      (b) $2:\sqrt{3}+1:\sqrt{2}$      (c) $\sqrt{6}:\sqrt{3}+1:2$    (d) $2:\sqrt{6}:\sqrt{3}+1$

76. A man can throw a stone to a maximum distance of 50 m. The time in seconds for which the stone remains in the air is

   (a) $\sqrt{(10/g)}$      (b) $5/\sqrt{g}$      (c) $10/\sqrt{g}$      (d) $5/\left(2\sqrt{g}\right)$

77. If $A+B=\pi/4$, then $(1+\tan A)(1+\tan B)$ is equal to

   (a) 1      (b) 2      (c) $\sqrt{3}$      (d) 0

78. If $1, \omega, \omega^2$ are the cube roots of unity, then the value of $(1+\omega)^3-(1+\omega^2)^3$ is

   (a) $2\omega$      (b) 2      (c) –2      (d) 0

79. If the arithmetic mean of the roots of a quadratic in $x$ is 8 and geometric mean is 5, then the quadratic is

   (a) $x^2-8x+25=0$      (b) $x^2-16x+5=0$

   (c) $x^2-16x+25=0$      (d) $x^2-8x+5=0$

80. The sum of the binomial coefficients of the odd terms in the expansion of $(1+x)^{50}$ is

   (a) $2^{51}$      (b) $2^{50}$      (c) $2^{49}$      (d) 0

81. If $x=3+\dfrac{2^2}{2!}+\dfrac{2^3}{3!}+\dfrac{2^4}{4!}+...\infty,$ then $1/x$ is equal to

   (a) $e^{-2}$      (b) $e^2$      (c) $e^{1/2}$      (d) $e^{-1/2}$

82. If $\dfrac{^{n+2}C_8}{^{n-2}P_4}=\dfrac{1}{48},$ then the value of $n$ is

   (a) 7      (b) 6      (c) 5      (d) 4

83. The displacement $x$ of a particle as a function of time $t$ is given in the figure. The acceleration of the particle is

    (a) always positive
    (b) always negative
    (c) always zero
    (d) positive during time 0 to $t$ and negative during $t$ to T
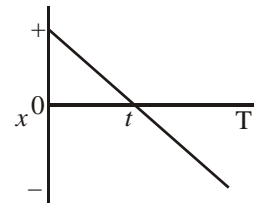
84. A ball is dropped from a height of 20m. After its impact with the ground, it rebounds with a velocity half of its velocity just before the impact. The maximum height reached after impact is
    (a) 20m        (b) 15m        (c) 10m        (d) 5m

85. The electric potential at a distance $r$, far off from an electric dipole of moment $p$, is

    (a) $\dfrac{1}{4\pi\varepsilon_0}\left(\dfrac{\vec{p}\cdot\vec{r}}{|\vec{r}|}\right)$
    (b) $\dfrac{1}{4\pi\varepsilon_0}\left(\dfrac{\vec{p}\cdot\vec{r}}{|\vec{r}|^2}\right)$
    (c) $\dfrac{1}{4\pi\varepsilon_0}\left(\dfrac{\vec{p}\cdot\vec{r}}{|\vec{r}|^3}\right)$
    (d) $\dfrac{1}{4\pi\varepsilon_0}\left(\dfrac{\vec{p}\times\vec{r}}{|\vec{r}|^3}\right)$

86. An ideal heat engine operating between a source and an intermediate sink has 50% efficiency. Another ideal heat engine operating between this intermediate sink and a final sink has 40% efficiency. The efficiency of an ideal engine operating between the same source and same final sink is
    (a) 90%        (b) 70%        (c) 45%        (d) 10%

87. A current of 20A flows through a copper rod of diameter 2cm. The magnetic field at a distance 5mm from the axis of the rod is

    (a) $\dfrac{\mu_0}{2\pi}\times10^3\,\text{T}$
    (b) $\dfrac{2\mu_0}{2\pi}\times10^3\,\text{T}$
    (c) $\dfrac{4\mu_0}{2\pi}\times10^3\,\text{T}$
    (d) $\dfrac{10\mu_0}{2\pi}\,\text{T}$

88. A thin convex lens is placed between a mirror and an object in such a way that the image of the object falls on to itself. The separation between the object and the lens is 20cm. Now, if another thin lens is placed between mirror and convex lens in contact with the convex lens, the object is to be moved by 10cm away from convex lens in order that the image of the object falls on to itself. The new lens is a concave lens of focal length
    (a) 10 cm        (b) 30 cm        (c) 40 cm        (d) 60 cm

89. The half life of two elements A and B is 5 and 15 yrs, respectively. If equal numbers of atoms of A and B are present in an alloy initially, then the time when the number of B atoms is twice that of A atoms is
    (a) 2.5 yrs        (b) 7.5 yrs        (c) 10 yrs        (d) 20 yrs

90. An optical fibre has a core of diameter 20 $\mu$m and refractive index 1.5. If the fibre has maximum entrance angle of $\pm60°$, the refractive index of the cladding is
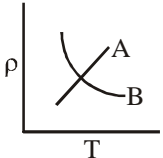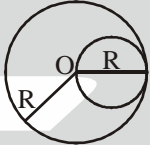    (a) $\sqrt{2}/2$        (b) $\sqrt{3}/2$        (c) $\sqrt{6}/2$        (d) $\sqrt{9}/2$

91. The SI unit of the permittivity of free space $\varepsilon_0$ is
    (a) $m^{-3}\,kg^{-1}\,s^4\,A^2$                    (b) $m^{-2}\,kg^{-1}\,s^4\,A^2$
    (c) $m^{-3}\,kg^{-1}\,s^4\,A^{-2}$                 (d) $m^{-2}\,kg^{-1}\,s^4\,A^{-2}$

92. A meter bridge is used for the measurement of
    (a) length        (b) potential        (c) resistance        (d) current

93. The role of graphite in a nuclear reactor is
    (a) to increase the energy of neutrons          (b) to decrease the energy of neutrons
    (c) to act as a catalyst in uranium fission      (d) to act as a source of neutron

94. In a PNP transistor, base is at a
    (a) lower potential than emitter                 (b)          higher potential than emitter
    (c) lower potential than collector               (d) higher potential than both collector and emitter

95. The variation of resistivity $\rho$ as a function of temperature $T$ is shown in the figure.
    (a) Curve $A$ is for metal and $B$ for a semiconductor
    (b) Curve $A$ is for semiconductor and $B$ for metal
    (c) Curve $A$ is for undoped semiconductor and $B$ for doped semiconductor
    (d) Curve $A$ is for doped semiconductor and $B$ for undoped semiconductor

96. A disk of mass $m$ and radius $R/2$ is attached to a disk of mass $M$ and radius $R$ as shown in the figure. The moment of inertia of the system about an axis passing through centre of the bigger disk and perpendicular to the disk is

    (a) $\frac{1}{2}MR^2 + \frac{3}{2}m(R/2)^2$     (b) $\frac{1}{2}MR^2 + \frac{1}{2}m(R/2)^2$

    (c) $\frac{1}{2}(M+m)R^2$                        (d) $(M+m)R^2$

97. A series LCR circuit is driven with a constant voltage ac source of variable frequency $\omega$. The power P dissipated in the circuit is graphically represented by

    (a) ![graph a]   (b) ![graph b]   (c) ![graph c]   (d) ![graph d]

98. A series combination of two capacitors $C_1$ and $C_2$ is charged by a voltage sources, $C_1$ is then discharged through an electrolytic cell liberating $m_1 g$ of a metal. Now, the parallel combination of $C_1$ and $C_2$ is charged by the same source and $C_1$ is discharged through the same cell liberating $m_2 g$ of the metal. The ratio $m_1/m_2$ is

    (a) $(C_1+C_2)/C_1$      (b) $(C_1+C_2)/C_2$      (c) $C_1/(C_1+C_2)$   (d) $C_2/(C_1+C_2)$

99. The intensity at the mid point on the line connecting two light sources has a maximum value of 36 units. At a point $x$ distance (from the mid point) towards either source, it has a minimum value of 4 units. The intensity at a distance $x/2$ is
    (a) 25 units          (b) 20 units          (c) 12 units          (d) 6 units

100. Two electric bulbs rated 120W and 80W are connected in series to mains (240 V) supply. The net power consumed is closest to
    (a) 200 W             (b) 80 W              (c) 50 W             (d) 40 W