

[6003]-347

**T.E. (Computer Engineering)**  
**THEORY OF COMPUTATION**  
**(2019 Pattern) (Semester-I) (310242)**

Time : 2½ Hours]

[Max. Marks : 70

Instructions to the candidates:

- 1) Answer Q.1 or Q.2, Q.3 or Q.4, Q.5 or Q.6, Q.7 or Q.8.
- 2) Neat diagrams must be drawn wherever necessary.
- 3) Figures to the right side indicate marks.
- 4) Assume suitable data, if necessary.

**Q1) a)** Give a Context Free Grammar for the following language. [9]

- i)  $L1 = \{a^i b^j c^k \mid i = j + k\}$  such that  $i, j, k > 0$
- ii)  $L2 = \{a^i b^j c^k \mid j = i + k\}$  such that  $i, j, k > 0$

b) Reduce the following grammar to Greibach Normal form. [9]  
 $S \rightarrow SS, S \rightarrow 0S1 \ 01$

OR

**Q2) a)** Show that the following grammar is ambiguous. [6]

 $S \rightarrow iCtS$ 
 $S \rightarrow iCtSeS$ 
 $S \rightarrow a$ 
 $C \rightarrow b$ 

b) Convert the following grammar to Chomsky Normal Form (CNF). [6]

 $G = (\{S\}, \{a, b\}, P, S)$ 
 $P = \{S \rightarrow aSa \mid bSb \mid a \mid b \mid aa \mid bb\}$ 

c) Consider the following grammar. [6]

 $E \rightarrow E + E \mid E - E \mid id$ 
Derive the string  $id-id*id$  using

- i) Leftmost derivation
- ii) Rightmost derivation

**Q3) a)** Find the transition rules of PDA for accepting a language  $L = \{w \mid w \in \{a, b\}^* \mid w \text{ is of the } a^n b^n \text{ with } n \geq 1\}$  through both empty stack and final state and demonstrates the stack operation for the string  $aaabbb$ . [9]

P.T.O.

- b) Design a push down automation to recognize the language generated by the following grammar :  
 $S \rightarrow S + S \mid S \square S \mid 4 \mid 2$   
 Show the acceptance of the input string  $2+2*4$  by this PDA. [8]
- OR
- Q4)** a) What is NPDA? Construct a NPDA for the set of all strings over  $\{a,b\}$  with odd length palindrome. [9]  
 b) Design a push down automation to recognize the language generated by the following. [8]  
 $S \rightarrow S + S \mid S \square S \mid 4 \mid 2$   
 Show the acceptance of the input string  $2+2*4$  by this PDA.
- Q5)** a) Design a Turing Machine for the following language by considering transition table and diagram. [9]  
 i) TM that erases all non blank symbols on the tape where the sequence of non blank symbols does not contain any blank symbol B in between.  
 ii) TM that find 2's complement of a binary machine.  
 b) What is TM? Design TM to check well formedness of parenthesis. Expand the transition for  $(())()$  [9]
- OR
- Q6)** a) How turing machine can be use to compute the functions? Design turing machine for multiplication of two numbers. [9]  
 b) Elaborate the following terms. [9]  
 i) Universal Turing Machine (UTM)  
 ii) Recursively Enumerable Languages  
 iii) Halting problem of Turing Machine
- Q7)** a) Define and Compare Class P and Class NP Problem with suitable diagram. [9]  
 b) What do you mean by polynomial time reduction? Explain with suitable example. [8]
- OR
- Q8)** a) Explain Satisfiability Problem and SAT Problem and comment on NP Completeness of the SAT Problem. [9]  
 b) What makes a problem NP-Complete? How do we prove a problem is NP-complete? Are all decision problems NP-complete? [8]

