

[6403]-36

**T.E. (Computer Engineering)**  
**THEORY OF COMPUTATION**  
**(2019 Pattern) (Semester - V) (310242)**

Time : 2½ Hours]

[Max. Marks : 70]

## Instructions to the candidates:

- 1) Answer Q.1 or Q.2, Q.3 or Q.4, Q.5 or Q.6, Q.7 or Q.8.
- 2) Neat diagrams must be drawn wherever necessary.
- 3) Figures to the right side indicate full marks.
- 4) Assume suitable data if necessary.

**Q1) a)** Give Context Free Grammars for the following languages and show the derivation for given string. [12]

- i)  $L = \{ w \in \{a,b\}^* \mid w \text{ is string of starting with 'a' and ending with 'b'} \}$   
 show the derivation for "ababab"
- ii)  $L = a^n b^{2n}$  where  $n \geq 1$ . Show the derivation for "aabbba"
- iii)  $RE = (0+1)^*$  Show the derivation for "0110"

**b)** Reduce the following grammar to Greibach Normal form. [6]

$$S \rightarrow AA \mid 0$$

$$A \rightarrow SS \mid 1$$

OR

**Q2) a)** Convert the following grammar to CNF. [8]

$$S \rightarrow aSa \mid bSb \mid A \mid \epsilon$$

$$A \rightarrow a \mid b \mid \epsilon$$

**b)** In the grammar, convert the given production rule into GNF form. If any production rule in the grammar is not in GNF form, convert it. [10]

$$S \rightarrow XB \mid AA$$

$$A \rightarrow a \mid SA$$

$$B \rightarrow b$$

$$X \rightarrow a$$

**Q3) a) i)** Construct PDA for the given CFG, and test whether  $010^4$  is acceptable by this PDA. [10]

$$S \rightarrow 0BB$$

$$B \rightarrow 0S \mid 1S \mid 0$$

**ii)** Construct PDA for the given CFG, and test whether 'aaabb' is acceptable by this PDA.

$$S \rightarrow aSb$$

$$S \rightarrow a \mid b \mid \epsilon$$

**b)** Construct PDA to accept  $L = \{ a^n b^n \mid n \geq 1 \}$  through empty stack. [4]

**c)** Convert the given PDA to CFG  $S \rightarrow 0S1 \mid 00 \mid 11$  [4]

OR

**Q4)** a) Construct Pushdown automata for  $L = \{0^n 1^m 2^{(n+m)} \mid m, n \geq 0\}$  [6]  
 b) NPDA for accepting the language  $L = \{a^{2m} b^{3m} \mid m \geq 1\}$  [6]  
 c) NPDA for accepting the language  $L = \{a^i b^j c^k d^l \mid i=k \text{ or } j=i, j>=1, l>=1\}$  [6]

**Q5)** a) Write short notes on with suitable diagrams. [12]  
 i) Reducibility  
 ii) Multi-tape Turing Machine  
 iii) Multi-head Turing Machine  
 iv) Two-way infinite Tape Turing Machine:  
 v) Multi-tape Multi-head Turing Machine  
 b) Construct a TM for subtraction of two unary numbers  $f(a-b) = c$  where a is always greater than b. Explain the logic of building this Turing machine. [5]

OR

**Q6)** a) Draw a Turing Machine to increment a binary number by 1 and demonstrate with any example. [6]  
 b) Obtain a Turing Machine to accept the language containing strings of a's and b's that do not end with abb. [7]  
 c) Construct a TM for the language  $L = \{0^n 1^n 2^n \mid n \geq 1\}$  [4]

**Q7)** a) What Minimum spanning tree problem? Prove that finding MST by using Kruskal's algorithm is in class P. [5]  
 b) What is post correspondence problem? Why is post correspondence problem undecidable? Explain PCP with following instance of the set of the strings A and B. [12]

	A	B
1.	1	111
2.	10111	10
3.	10	0

OR

**Q8)** a) Define and Compare Class P and Class NP Problem with suitable diagram. [8]  
 b) State and explain with suitable example. [9]  
 i) Decidable Problem  
 ii) Undecidable Problem  
 iii) Church-Turing Thesis

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