

# **Economics for Engineers**

**DEPARTMENT OF HUMANITIES  
VSSUT BURLA**

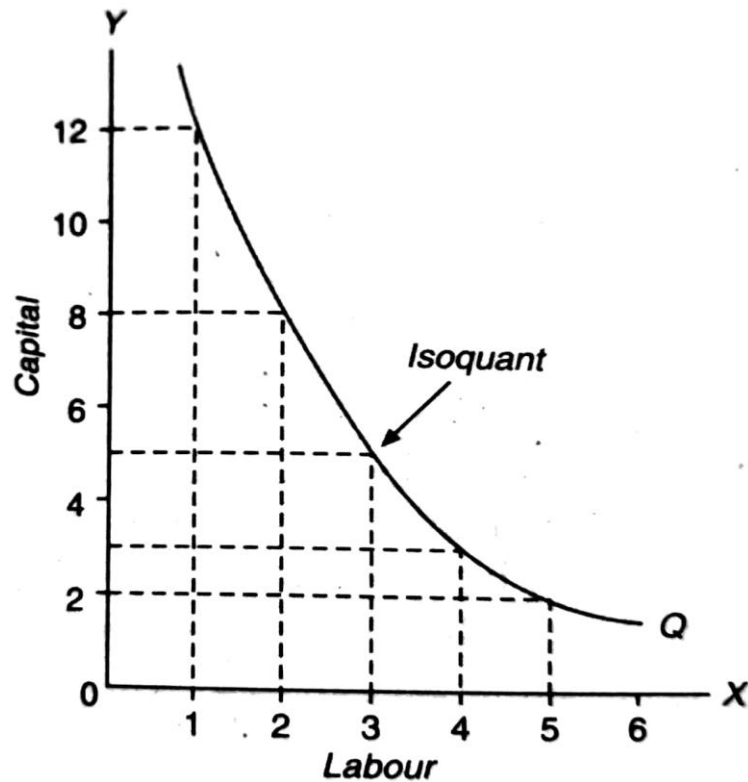
# Long-Run Production

- All Factors are variables
- Use of Isoquants or equal product curve
- Isoquant: Locus of the different combinations of two factor inputs producing same level of output
- Marginal Rate of Technical Substitutions (MRTS):  
The slope of Isoquant
- $MRS = MU_x / MU_y$
- $MRTS = MPL / MPK$
- $MPL = dq/dl = dq/dk$

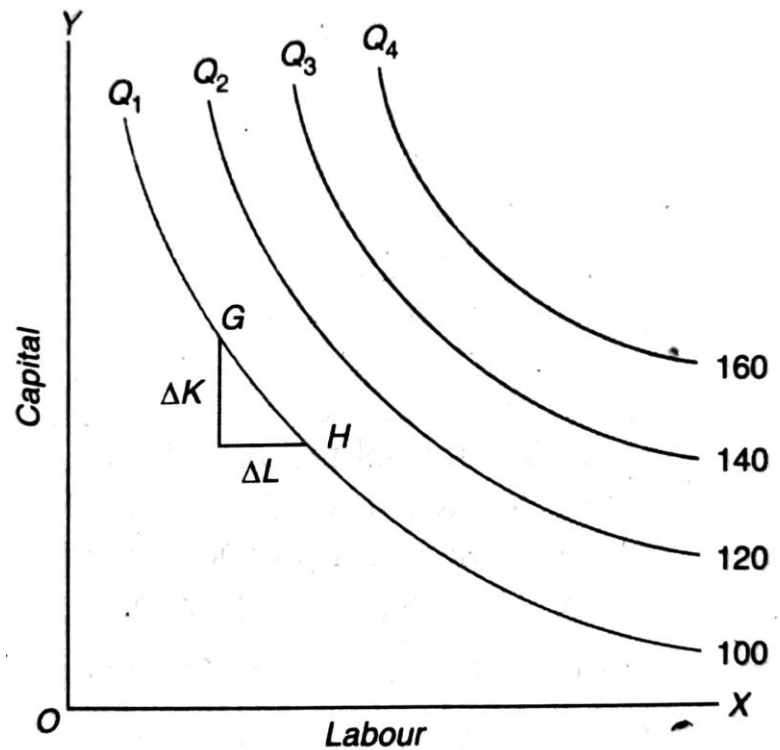
- $U = F(X, Y) \dots IC$
  - $I = P_X \cdot X + P_Y \cdot Y \dots \text{Budget Line}$
  - SLOPE OF IC = SLOPE OF BL
  - $MUX/MUY = P_X/P_Y \dots \text{CONSUMER EQUIL}$
- 
- $Q = F(L, K) \dots IQ$
  - $C = WL + RK \dots \text{ISO COST LINE}$
  - SLOPE OF IQ = SLOPE OF Iso COST
  - $MPL/MPK = W/R$

Contd...  $u = f(x, y)$ ... IC  
 $Q = F(L, K)$ ....

Isoquant



Isoquant Map



# Properties of Isoquants

1. Isoquants slope downward to the right
2. Isoquants are convex to the origin
3. Never intersect each other
4. Higher Isoquants represents higher level of output

# Return to Scale

- ✓ Scaling Up or Scaling Down
- ✓ Looking into Output by changing all input in the same proportion

$$Q=f(L, K)$$

$$hQ=f(hL, hK)$$

Now, If  $h=\$$ : Output increases in same proportion to input (Constant return to Scale)

# Contd...

If  $h > 1$ : Output increases more than proportionately to input changes (Increasing return to Scale)

If  $h < 1$ : Output increases less than proportionately to input changes (Decreasing return to Scale)

Cobb-Douglas Production function:

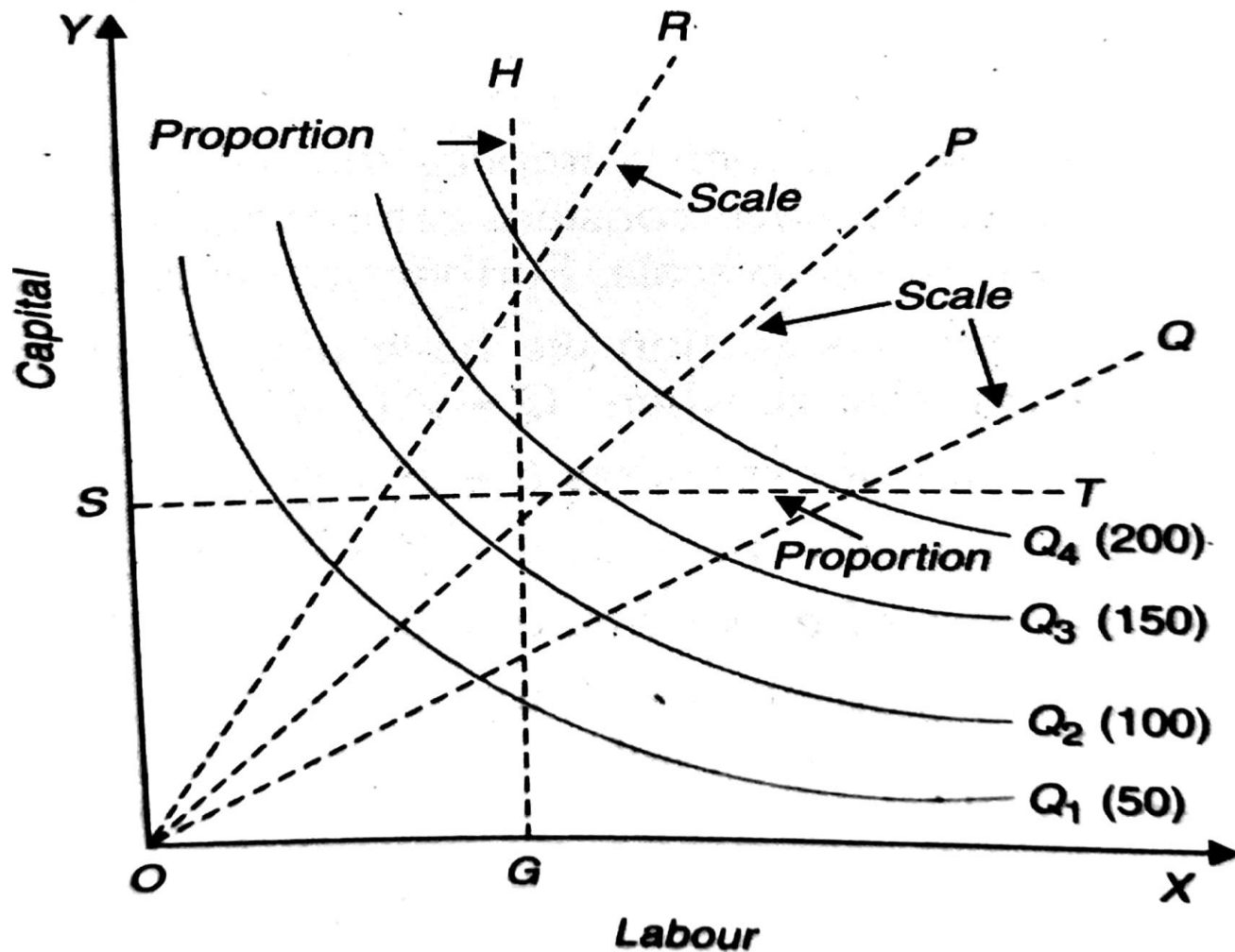
$$Q = AL^\alpha K^\beta$$

$$\alpha + \beta = 1 \text{ (CRS)}$$

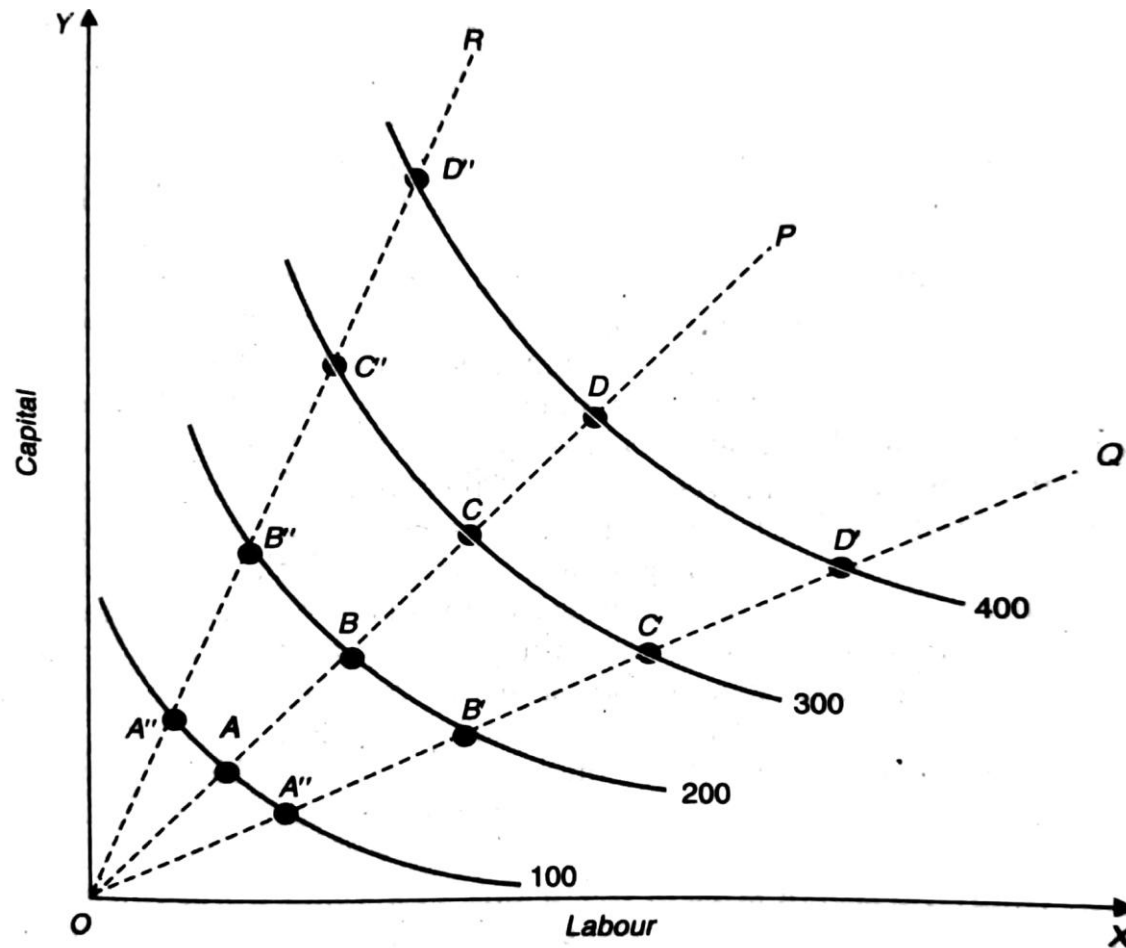
$$\alpha + \beta < 1 \text{ (DRS)}$$

$$\alpha + \beta > 1 \text{ (IRS)}$$

# Change in Scale and Factor Proportion



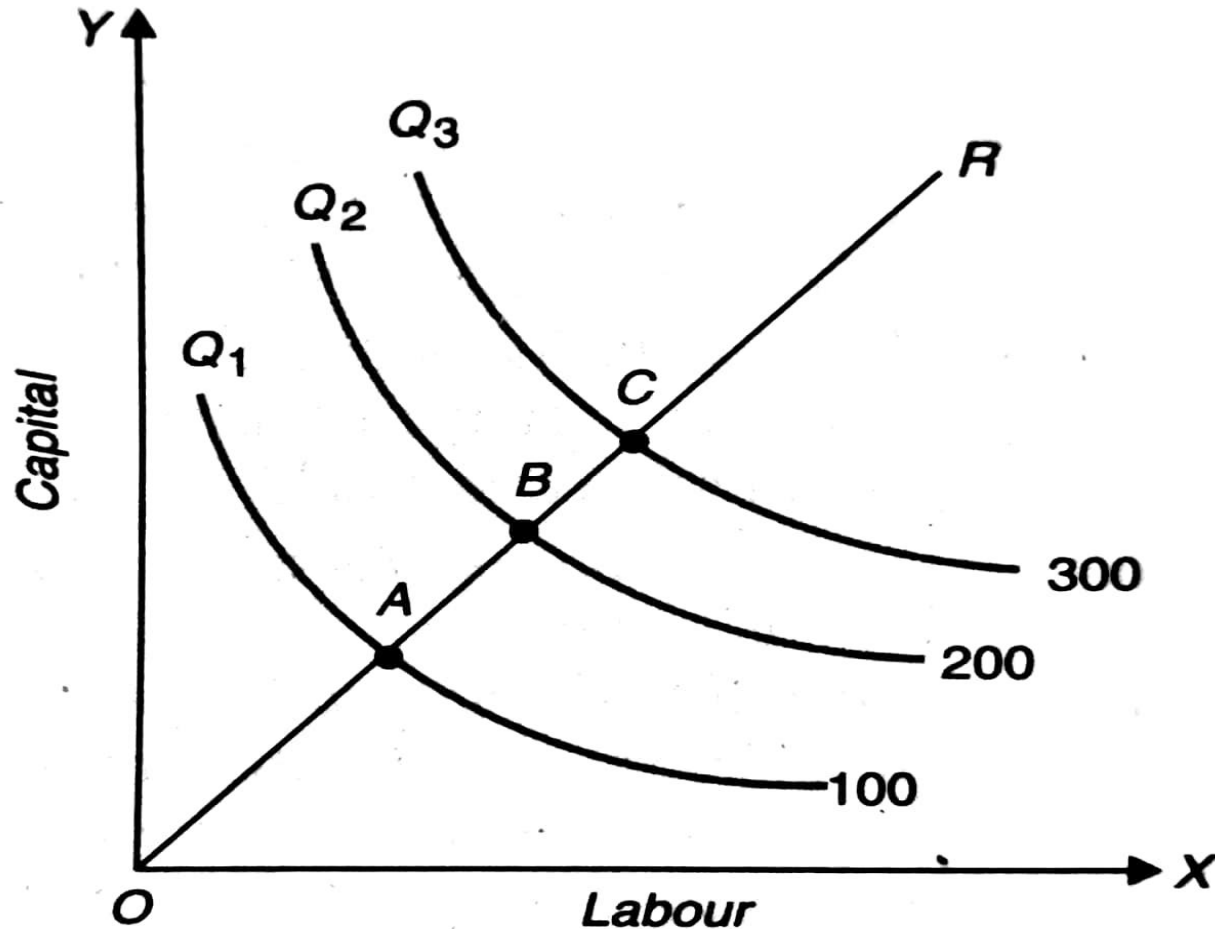
# Constant Return to Scale



Increasing Return to Scale...  $OA >$

$AB > BC$

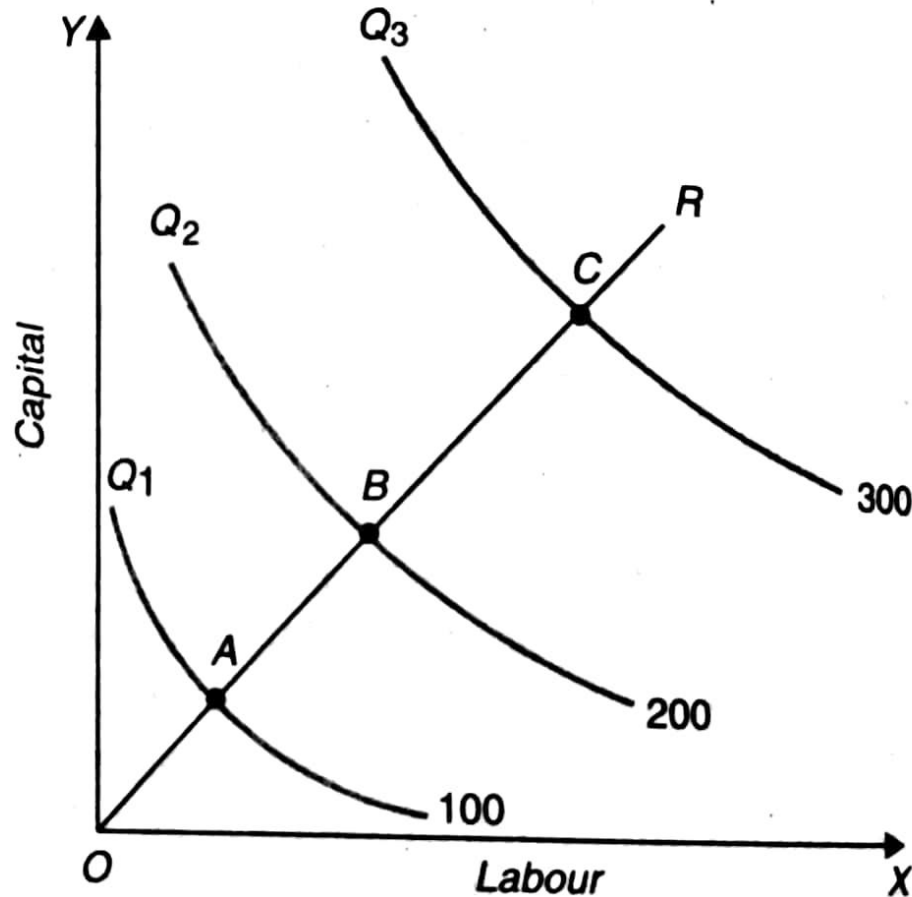
$OA < AB < BC \dots OA = AB = BC$



# Contd...

- Indivisibility of the factors
- Greater possibility of specialisation
- Dimensional Economies

# Decreasing Return to Scale $OA < AB < BC$



$$TC = TFC + TVC \dots$$

$$TAC = TC / Q$$

$$AFC = TFC / Q$$

$$AVC = TVC / Q$$

$$TAC = AFC + AVC$$

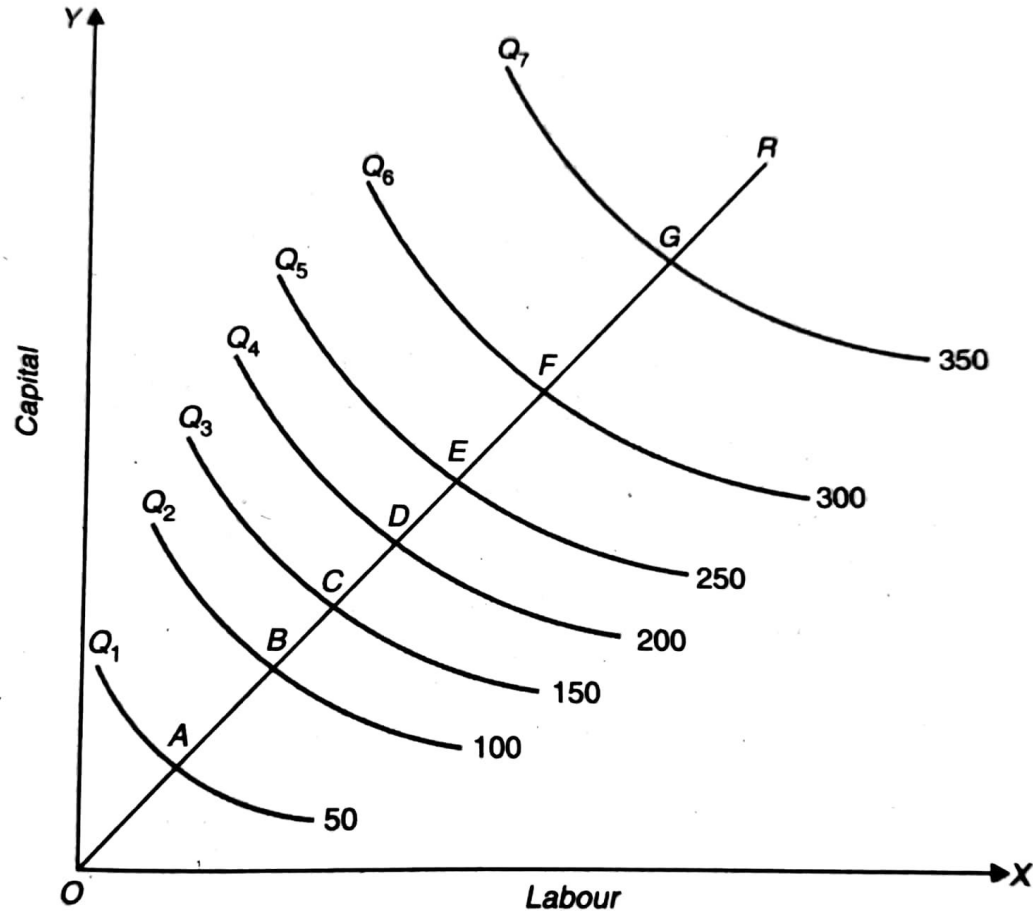
MC

$$TC = TVC$$

$$TAC = AVC$$

MC

# Varying Return to Scale



Thank  
you!!