

Mod-II

Anomalies in relational database

- Insertion anomalies
(insert some info results in constraints)
- Deletion anomalies
(we delete some & cause deletion of other undesirable info)
- Update anomalies
(we try to update but lead to inconsistency)

Normalisation:-

Process by which that reduce data redundancy and eliminate anomalies from the database

- Decompose unsatisfactory large relation by breaking into smaller form
- It is a step by step process & each step is known as NORMAL FORM
- It is reversible process

1NF
2NF
3NF
BCNF

} Functional dependency

4NF $\Rightarrow$ Multivalued dependency

5NF $\Rightarrow$ Join dependency

① Functional dependency:-

In a relation X & Y are two subset of sets of attributes;

Y is functional dependent on X if a given value of X uniquely determines the value of Y

$$X \rightarrow Y$$

X	Y
a	1
b	22
c	65
a	1

$X \rightarrow Y$
if $t_1[X] = t_2[X]$
then $t_1[Y] = t_2[Y]$

X	Y
a	2
b	2
a	2
b	2
c	2

$$a \rightarrow 2$$

$$b \rightarrow 2$$

$$c \rightarrow 2$$

Yes

$$X \rightarrow Y$$

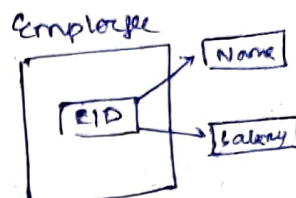
For same value of x , value of y must be same
 For diff value of x , value of y may be same

$$X(\text{EID}) \rightarrow Y(\text{Name, Salary})$$

mean:

$$X(\text{EID}) \rightarrow Y(\text{Name})$$

$$X(\text{EID}) \rightarrow Y(\text{Salary})$$



Classification of FD's :-

i) Trivial

$X \rightarrow Y$ is trivial if & only if $Y \subseteq X$.

also $X \rightarrow X$
 $Y \rightarrow Y$

$$AB \rightarrow B$$

$$B \subseteq AB$$

ii) Non-trivial

If at least one attribute in RHS that is not part of LHS

$$AB \rightarrow B \text{ (C)}$$

$$A \rightarrow BCD$$

$$A \rightarrow B \quad A \rightarrow C \quad A \rightarrow D \quad A \rightarrow A$$

(iii) Fully functional dependency:-

FD: $X \rightarrow Y$ Y is fully dep. on X if there is ~~no~~ Z where Z is proper subset of X such that $Z \rightarrow Y$

Ex:

FD $AB \rightarrow C$

$$A \rightarrow C \text{ (X)}$$

iv) Partial Dependency

$$F.D \rightarrow F$$

$$C.K \rightarrow R$$

$$R(ABCD)$$

$$CK \rightarrow AB$$

$$F.D = \{A \rightarrow C\}$$

Partial

v) Transitive Dependency

Dependency b/w non-prime key attribute

$$X \rightarrow Y, Y \rightarrow A \text{ then } X \rightarrow A$$

1NF

- Attribute of table cannot hold multiple values
- Should have atomic values

Roll No	Roll No
X	66
Y	77
	88

↓ 1NF

Roll No	Roll No
X	66
Y	77
Y	98

X	74A, Delhi
Y	64B, Odisha

↓ 1NF

X	74A	Delhi
Y	64B	Odisha

Composite attribute

	Date	WEP
X	2/10	3
Y	10/11	2

↓

X	21/10
Y	10/11

Derived attribute

Prime attribute:

For a given relation $R = \{A_1, \dots, A_n\}$ an attribute is prime attribute if it is part of candidate key.

Non-prime Attribute

An key that is not a part of candidate key

Closure set of FDs:

F^+ is set of all FDs that can be determined using given set of FD

Total no. of possible FDs in $R = 2^{2^n}$
(n attribute)

ex: $R(A, B)$ FDs
 $2^{2 \times 2} = 2^4 = 16$

Attribute Closure :-

① Finding keys of relation:

If X^+ contain all attributes then X is called superkey of R

$R(ABCDE)$

$\{ A \rightarrow BC$
 $CD \rightarrow E$
 $B \rightarrow D$
 $E \rightarrow A \}$

$A^+ = \{ ABCDE \} \rightarrow C.K$

$B^+ = \{ BD \}$

$C^+ = \{ CEABD \}$

$D^+ = \{ DEABC \}$

$E^+ = \{ EABCD \}$

$BC^+ = \{ BCDEA \}$

$CD^+ = \{ CDEAB \}$

Additional FD's

$R(ABCD)$
 $\{ A \rightarrow BC$
 $B \rightarrow CD$
 $D \rightarrow AB \}$

$AD \rightarrow C$ is possible or not

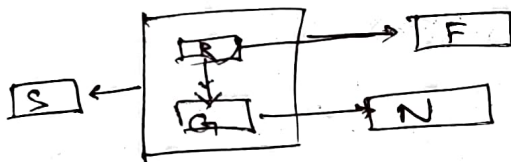
$$AD^+ = \{ A D B C \}$$

$AD \rightarrow C$ is possible

* Full functional Dependency

Let A be non prime key attribute then A completely dependent upon all prime key attribute

$$A \Rightarrow FFD$$



Prime: R, G
 Nonprime: S, N, F

S is F.F.D

$$R, G \rightarrow S$$

* Partial Dependency:-

If A non prime key attribute not dependent on all but some prime key attribute. It is called as partial dependency.

In above ex. F, N are partial de.

$$R \rightarrow F \quad G \rightarrow N$$

$ABCD \rightarrow E$ & $AB \rightarrow E$ } then it P.D.

$ABCD \rightarrow E$ } F.F.D

* 2NF

A relation is said to be in 2NF if

(i) 1NF

(ii) Non prime key attributes are fully functional dependent upon primary key (No partial F.D.)

Non-prime $\rightarrow$ non prime

$$R \rightarrow ABCDE$$

$$F: \left\{ \begin{array}{l} AB \rightarrow C \\ A \rightarrow D \\ B \rightarrow E \end{array} \right\}$$

$$(AB)^+ = \{ ABCDE \}$$

$$P.K = \{A, B\}$$

$$N.P.K = \{C, D, E\}$$

$$AB \rightarrow C \quad (FFD) \quad \nrightarrow \quad 2NF$$

$$A \rightarrow D \quad (P.D) \quad \times$$

$$B \rightarrow E \quad (P.D) \quad \times$$

$$R_1 = (AB \rightarrow C)$$

$$R_2 = (A \rightarrow D)$$

$$R_3 = (B \rightarrow E)$$

* Armstrong's axioms

1) Reflexivity: If $Y \subseteq X$ then $X \rightarrow Y$
which also implies $X \rightarrow X$

2) Augmentation:

If $X \rightarrow Y$ then $XZ \rightarrow YZ$ where Z is an set of attribute

3) Transitivity:

If $X \rightarrow Y$ and $Y \rightarrow Z$ then $X \rightarrow Z$ hold

Non prime key relationship

4) Union

If $X \rightarrow Y$ and $X \rightarrow Z$ then
 $X \rightarrow YZ$ holds

5) Decomposition:

If $X \rightarrow YZ$ holds then $X \rightarrow Y$ & $X \rightarrow Z$ holds

6) Pseudotransitivity:

If $X \rightarrow Y$ and $YZ \rightarrow W$ then
 $XZ \rightarrow W$ holds

$$R = \{A, B, C, D, E, F, G\}$$

$$FD = \{A \rightarrow B, BC \rightarrow DE, AEF \rightarrow G, E \rightarrow C, A \rightarrow E\}$$

Closure

LC की निम्नलिखित

$$A^+ = \{A, B, E, C, D\}$$

$$BC^+ = \{B, C, D, E\}$$

$$AEF^+ = \{A, E, F, G, C, B, D\}$$

$$E^+ = \{E, C\}$$



⊛ Candidate keys :-

It is minimal set of attributes whose attribute closure is set of all attributes called as candidate key.

$$R = \{A, B, C, D, E\}$$

$$FD = AB \rightarrow C, CD \rightarrow E, DE \rightarrow B$$



$$ADC^+ = \{A, D, C, E, B\}$$

$$ABD^+ = \{A, B, D, C, E\}$$

$$ADE^+ = \{A, D, E, B, C\}$$

$$C.K = \{ADC^+, ABD^+, ADE^+\}$$

$$R = \{A, B, C, D, E, F\}$$

$$AB \rightarrow C$$

$$C \rightarrow D$$

$$D \rightarrow BE$$

$$E \rightarrow F$$

$$F \rightarrow A$$

$$A^+ = \{A\}$$

$$B^+ = \{B\}$$

$$C^+ = \{C, D, B, E, F, A\} \text{ck}$$

$$D^+ = \{D, B, E, F, A, C\} \text{ck}$$

$$E^+ = \{E, F, A\}$$

$$F^+ = \{F, A\}$$

$$AB^+ = \{A, B, C, D, E, F\} \text{ck}$$

$$AE^+ = \{A, E, F\}$$

$$AF^+ = \{A, F\}$$

$$BE^+ = \{B, E, F, A, C, D\} \text{ck}$$

$$BF^+ = \{B, F, A, C, D, E\} \text{ck}$$

$$EF^+ = \{E, F, A\}$$

$$AEF^+ = \{A, E, F\}$$

$$CK = \{C, D, AB, BE, BF\}$$

Convert relation to 2NF

Q1

$$R = \{A, B, C, D\}$$

$$AB \rightarrow D \quad \{A, B\} \text{ ck}$$

$$B \rightarrow C \quad \{C, D\} \text{ N.P. attr.}$$

$$AB \rightarrow D \quad 2NF \checkmark$$

$$B \rightarrow C \times$$

$$\{A, B\}^+ = \{A, B, D, C\}$$

Decomposition

$$R_1 (A, B, D) \quad AB \rightarrow D$$

$$R_2 (B, C) \quad B \rightarrow C$$

Q2

$$R = \{A, B, C, D, E\}$$

$$AB \rightarrow C$$

$$B \rightarrow DE$$

$$A \rightarrow D$$

$AB \Rightarrow$ Primary key

$C, D, E \Rightarrow$ N.P. attr.

$$AB \rightarrow C \times$$

$$A \rightarrow D \times$$

$$B \rightarrow DE \times$$

$$R_1 (A, B, C)$$

$$R_2 (A, D)$$

$$R_3 (B, D, E)$$

3NF

A relation is said to be 3NF if

(i) Satisfies 2NF

(ii) Non primary key attribute must be non transitive dependence

To convert into 3NF

① General ② (Non prime) wala

Q3 $R \{A, B, C, D, E\}$

$$F.D \Rightarrow AB \rightarrow C$$

$$B \rightarrow D$$

$$D \rightarrow E$$

$$(AB)_{ck}$$

$$B \rightarrow D$$

$$D \rightarrow E$$

$$B \rightarrow E$$

$$AB \rightarrow C$$

$$\text{3NF} \checkmark$$

No trans.

$$B \rightarrow D$$

$\times$ 2NF P.F.D

$$D \rightarrow E$$

Non P.F.D

$R_1(A, B, C)$ 2NF
 $R_2(B, DE)$ 2NF

$R_1(A, B, C)$ 3NF
 $R_2(B, DE)$
 $R_3(D, E)$ 2NF 3NF
 $R_4(B, D)$ 2NF 3NF

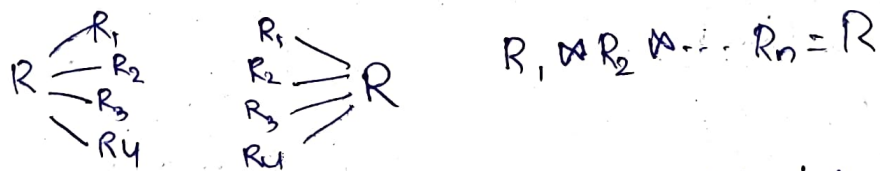
Property of Normalisation:-

Two additional prop. also must hold on the decomposition of relation:-

- (i) Lossless Join
- (ii) Dependency preservation

① Lossless Join:

It ensures that no data will be lost after decomposition that means we will recover the original relation from the decomposition relation



→ It contains equal or less no of tuples without losing data

Lossy Join

(Extra tuples)

$$R_1 \bowtie R_2 \supset R \quad (\text{Natural Join})$$

Lossless Join is a compulsory in Norm.

② Dependency Preservation Property:

It ensures function dependency keep alive after decomposition also

$$R \xrightarrow{(F)} R_1(F_1) \bowtie R_2(F_2) \Rightarrow (F_1 \cup F_2)^+ = F^+$$

Lossless Join Property!

x	y	z
A	6	7
B	3	4
C	8	4

$R_1(xyz)$

x	z
A	7
B	4
C	4

$R_2(xz)$

z	y
7	6
4	3
4	8

$R_3(zy)$

x	y	z
A	6	7
B	3	4
B	8	4
C	3	4
C	8	4

Lossy Join

x	y	z
A	6	7
B	3	4
C	8	4

$R_1(xyz)$

x	y
A	6
B	3
C	8

$R_2(xy)$

y	z
6	7
3	4
8	4

$R_3(yz)$

x	y	z
A	6	7
B	3	4
C	8	4

$R(xyz)$

$$R_1(xyz) \Rightarrow R_2(xy) \cup R_3(yz) \Rightarrow R(xyz)$$

Lossless

Condition to Check :-

$R \Rightarrow R_1 \& R_2$
For Lossless Join

(i) Union of R_1 & R_2 must contain all the attribute of R

(ii) Must be common attribute
 $R_1 \cap R_2 \neq \emptyset$

(iii) Intersection of R_1 & R_2 must be superkey of R_1 or R_2 or Both

Q) $R(ABCD)$ $R_1(AB)$ & $R_2(CD)$ is Lossless or Lossy?

$R_1(AB) \cup R_2(CD) = R(ABCD)$ ✓

$R_1 \cap R_2 = \emptyset$ Fail

Hence it is Lossy Join

1) R (ABCDEF)

R₁ (ABC) A → CD

R₂ (AFD) B → C

R₃ (EF) F → DE

F → A

Lossless or Lossy?

2)

R (ABCDEF)

R₁ (ABC)

R₂ (AFD)

R₃ (EF)

R₄ (AEFD)

(i) R₁ (ABC) ∪ R₄ (AEFD) = R (ABCEFD)

(ii) R₁ (ABC) ∩ R₄ (AEFD) = A ≠ ∅

(iii) R₁ (ABC) B → C

AB⁺ = {ABC} _{ck}

R₂ (AEFD)

F → DE

F → A

F⁺ = {FDEA} _{ck}

AB⁺ F⁺
(A)

Not super key ⇒

"Either R₁ or R₂ mein sirf 'A' data graphir dono mein bhi ok hai"

Lossy Join

Dependency Preservation Property:-

1) R (ABC) F = {A → B, B → C, C → A}

R₁ (AB)

R₂ (BC)

{R₁ ∪ R₂}⁺ = F

A → B
B → C
C → A

A⁺ = {ABC} _{ck}
B⁺ = {BCA} _{ck}
C⁺ = {ABC} _{ck}

F⁺

R₁ (AB)

F₁ {A → B, B → A} (transitivity)

R₂ (BC)

F₂ {B → C, C → B} (transitivity)

(F₁ ∪ F₂)⁺ = {A → B, B → A, B → C, C → B, A → C} _{A → C} = F⁺

A⁺ = {ABC} _{ck}
B⁺ = {ACB} _{ck}
C⁺ = {ABC} _{ck}

BCNF (Boyce Code Normal Form)

→ Strict format of BCNF

→ A relation is said to be in BCNF if

(i) It is in 3NF

(ii) All determinants are ~~candidate~~ keys
(LHS)

$R(ABC)$ $A \rightarrow B, B \rightarrow C$

$A \& B \Rightarrow \text{deter.} \Rightarrow \text{Cand.}$

Every BCNF is also 3NF but Vice versa is not true.

Ex:

$R(ABC)$

$A \rightarrow B \rightarrow B$

$A \rightarrow C$

$A \& B$ are candidate keys

$A \rightarrow BC$

$B \rightarrow B$

$A^+ = \{ABC\}_{ck}$

$B^+ = \{BC\} \times$

Lossless or
BCNF

$R_1(ABC), R_2(BC)$

$R_1 \cup R_2 = R$

$R_1 \cap R_2 = C$

$R_1(AC)$

$A \rightarrow C$

$A^+ = \{AC\}_{ck}$

(A)

$R_2(BC)$

$B \rightarrow B$

$B^+ = \{BC\}_{ck}$

(B)

(C) Super key

Lossless Join

BCNF

Multivalued Functional Dependency

For $R(ABC)$, there is multivalued dependency of B on attribute A if and only if the set of B values associated a given value of A and is independent of the C values.

$A \twoheadrightarrow B$ (A multideternines B values)

If $A \twoheadrightarrow B$ then $A \twoheadrightarrow C$

$B \twoheadrightarrow C$ ✓

$C \twoheadrightarrow B$ Not possible

If any two tuples t_1 & t_2 has same A value, then there must exist two other tuples t_3 & t_4 obey the rule

(i) t_3 & t_4 has same A values of t_1 & t_2

(ii) $t_3 = t_1 = B$

(iii) $t_4 = t_2 = B$

(iv) The dependency $A \twoheadrightarrow B$ is called multivalued

If $B \subseteq A$ or $A \cup B = R$

YNF:

$A \rightarrow t_1 = t_2 = t_3 = t_4 = \text{Deepak}$

$B \rightarrow t_1 = t_3 = P_1$

- Redundant

$B \rightarrow t_2 = t_4 = P_2$

Prog	Proj
Kapil	P_3
Deepak	P_1
Sanjay	P_6
Deepak	P_2
Rahul	P_1
Sonia	P_9

$A \twoheadrightarrow B$

($A \& B$) Superkey

Proj	Mod
P_3	M01
P_1	M31
P_6	M91
P_2	M61
P_1	M91
P_1	M71
P_2	M75
P_9	M01

$B \twoheadrightarrow C$

($B \& C$) Superkey

5NF !

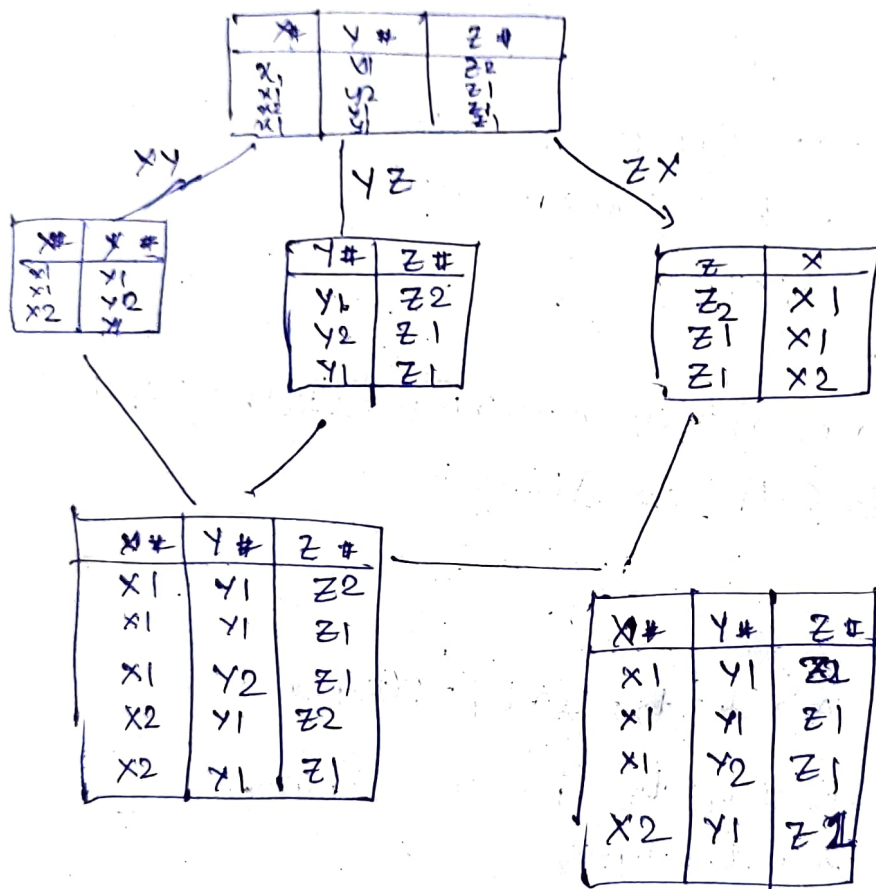
A relation R is in 4NF & it decomposed into $R_1, R_2, \dots, R_n$ then R satisfies the Join dependency

$$\pi(R_1, R_2, R_3 \dots R_n) = R$$

If & only If Joining of

$$R_1 \text{ to } R_n = R$$

$$R_1 \bowtie R_2 \bowtie \dots \bowtie R_n = R$$



(b)

Equivalence functional dependency:

$$F: \begin{array}{l} A \rightarrow B \\ B \rightarrow C \\ C \rightarrow A \end{array} \quad G: \begin{array}{l} A \rightarrow BC \\ B \rightarrow A \\ C \rightarrow A \end{array}$$

$$A^+ = \{ABC\}$$

$$B^+ = \{BAC\}$$

$$C^+ = \{ABC\}$$

$$F \subseteq G$$

$$A^+ = \{ABC\}$$

$$B^+ = \{BCA\}$$

$$C^+ = \{CAB\}$$

$$G \subseteq F$$

$$\text{So } F = G$$

$$\left. \begin{array}{l} AB \rightarrow C \\ A \rightarrow C \\ B \rightarrow C \end{array} \right\} \text{X (wrong) but } \begin{array}{l} A \rightarrow BC \\ A \rightarrow B \\ A \rightarrow C \end{array}$$

Canonical form: Redundancy

$$R(W, X, Y, Z)$$

$$X \rightarrow W$$

$$WZ \rightarrow XY$$

$$Y \rightarrow WXZ$$

Convert into single one/decom.

$$X \rightarrow W \quad \checkmark$$

$$\cancel{WZ \rightarrow X}$$

$$WZ \rightarrow Y \quad \checkmark$$

$$\cancel{X \rightarrow WXZ}$$

$$Y \rightarrow X \quad \checkmark$$

$$Y \rightarrow Z \quad \checkmark$$

$$X^+ = \{W\}$$

$$X^+ = \{X\}$$

Dependency as dec.

$$WZ^+ = \{WZ, XY\}$$

$$WZ^+ = \{X, Y, WZ\}$$

$$WZ^+ = WZ, XY$$

$$WZ^+ = \{WZ\}$$

$$Y^+ = \{WXZ\}$$

$$Y^+ = \{X, Z, W\}$$

$$Y^+ = \{Y, X, Z\}$$

$$Y^+ = \{Y, Z\}$$

$$Y^+ = \{Y, X, W\} \quad \checkmark$$

(with Z)

$$\text{So, } X \rightarrow W$$

$$WZ \rightarrow Y$$

$$Y \rightarrow X$$

$$Y \rightarrow Z$$

$$WZ^+ = \{WZ, Y, Z\}$$

$$W^+ = \{W\}$$

$$Z^+ = \{Z\}$$

Final (Ans)

$$X \rightarrow W$$

$$XZ \rightarrow Y$$

$$Y \rightarrow XZ$$

Min

$R(ABCD)$

$A \rightarrow B$
 $C \rightarrow B$
 $D \rightarrow ABC$
 $AC \rightarrow D$

$A \rightarrow B$ ✓
 $C \rightarrow B$ ✓
 $D \rightarrow A$ ✓
 ~~$D \rightarrow B$~~
 $D \rightarrow C$ ✓
 $AC \rightarrow D$ ✓

Minimal cover

Set of functional dependencies that is reduced version of given set of FDs

$A \rightarrow B$
 $A^+ = \{AB\}$
 $A^+ = \{A\}$ } $\downarrow$ ac

$C \rightarrow B$
 $C^+ = \{CB\}$
 $C^+ = \{C\}$ } $\downarrow$

$D \rightarrow A$
 $D^+ = \{DABC\}$
 $D^+ = \{DBC\}$ } $\downarrow$ dep

$D \rightarrow B$
 $D^+ = \{DABC\}$
 $D^+ = \{ACBD\}$ } $\downarrow$

$D \rightarrow C$
 $D^+ = \{DACB\}$
 $D^+ = \{DAB\}$ } $\downarrow$

$AC \rightarrow D$
 $AC^+ = \{ACDB\}$
 $AC^+ = \{ACB\}$ } $\downarrow$

$A \rightarrow B$
 $C \rightarrow B$
 $D \rightarrow A$
 $D \rightarrow C$
 $AC \rightarrow D$

$AC \rightarrow D$
 $AC^+ = \{ACDB\}$
 $AC^+ = \{ACB\}$ } $\downarrow$ in
 $A^+ = \{AB\}$
 $C^+ = \{CB\}$ } $\downarrow$ Both are req

Q) $R(VWX.YZ)$

$V \rightarrow W$
 $VW \rightarrow X$
 $Y \rightarrow VXZ$

$V \rightarrow W$ ✓
 $VW \rightarrow X$ ✓
 $Y \rightarrow V$ ✓
 ~~$Y \rightarrow X$~~
 $Y \rightarrow Z$ ✓

$V \rightarrow W$
 $V^+ = \{VWX\}$
 $V^+ = \{V\}$ } $\downarrow$

$VW \rightarrow X$
 $VW^+ = \{VWX\}$
 $VW^+ = \{VW\}$ } $\downarrow$

$Y \rightarrow V$
 $Y^+ = \{YVXZWX\}$
 $Y^+ = \{YXZ\}$ } $\downarrow$

$Y \rightarrow X$
 $Y^+ = \{YXZWX\}$
 $Y^+ = \{VXZWX\}$

$Y \rightarrow Z$
 $Y^+ = \{YZVWX\}$
 $Y^+ = \{YVWX\}$ } $\downarrow$

$$VW \rightarrow X$$

$$VW^+ = \{VWX\}$$

$$V^+ = \{VWX\}$$

$$W^+ = \{W\}$$

$$V \rightarrow W$$

$$W \rightarrow X$$

$$Y \rightarrow V$$

$$Y \rightarrow Z$$

$$V \rightarrow X$$

Final answer:

$$V \rightarrow W$$

$$V \rightarrow X$$

$$Y \rightarrow V$$

$$Y \rightarrow Z$$

$$V \rightarrow WX^*$$

$$Y \rightarrow VZ$$

Key

$$(Key)^+ = R$$

(Whole relation)



Unique value

Set of attributes which can uniquely identify a set of tuples/rows in a table

$$R(ABCD)$$

$$A \rightarrow BC$$

$$A^+ = \{ABC\}$$

A set of attributes which can uniquely identify a set of tuples/rows in a table. So A is not a key

$$AD^+ = \{ADBC\}$$

AD is a key

$$ABC \rightarrow D$$

$$AB \rightarrow CD$$

$$A^+ \rightarrow BCD$$

$$ABC \checkmark$$

$$AB \checkmark$$

$$A \checkmark$$

} all are superkeys

A^+ } Candidate key

(Efficient/minimal version)

whose proper subset is not a superkey.

Super key
all keys

$$B \rightarrow ACD$$

$$ACD \rightarrow B$$

$$B^+ = \{ACD\}$$

$$ACD^+ = \{ACDB\}$$

} Both are candidate key

Primary Key: Amongst key one is chosen as primary by data administrator to identify tuples

R(ABCD)

$AB \rightarrow C$

$C \rightarrow BD$

$D \rightarrow A$

$AB^+ = \{ABCD\}$

$C^+ = \{CBDA\}$

$D^+ = \{DA\}$

CK

To find Candidate Key :-

1) R(ABCD)

$A \rightarrow B$

$B \rightarrow C$

$C \rightarrow A$

'D' essential attribute

$AD^+ \rightarrow ABCD$

$BD^+ \rightarrow BDCA$

$CD^+ \rightarrow CDAB$

$\Rightarrow$ Minimal C.K

2) $AB \rightarrow CD$

$D \rightarrow A$

$AB^+ = ABCD$

$D = ADX$

$DB^+ = BDAC$

B is essential attribute

(AB, BD) CK

3) R(ABCDEF)

$AB \rightarrow C$

$C \rightarrow D$

$B \rightarrow AE$

B, F are essential attribute

$BF = \{BFAEC\}$ CK

~~ABF~~

No need to check further

4) R(ABCD)

$AB \rightarrow CD$

$C \rightarrow A$

$D \rightarrow B$

$A^+ = A$

$B^+ = B$

$C^+ = CA$

$D^+ = DB$

$AB^+ = \{ABCD\}$ CK

$AC^+ = \{AC\}$

$AD^+ = \{ADBC\}$ CK

$BC^+ = \{BCAD\}$ CK

$BD^+ = \{BD\}$

$CD^+ = \{CDAB\}$ CK

$\begin{pmatrix} B \\ C \end{pmatrix}$

$\{AC^+, AD^+, CD^+, BC^+\}$

5) R(ABCDE)

AB → CD

D → A

BC → DE

C.K

GAB, BC, BD

B is essential attribute

$AB^+ = \{ABCD E\}_{ck}$

$BC^+ = \{BCDE A\}_{ck}$

$BD^+ = \{BDACE\}_{ck}$

$BE^+ = \{BE\}_x$

6) R(WXYZ)

Z → W

Y → XZ

XW → Y

$X^+ = \{X\}$

$Y^+ = \{YXZ W\}_{ck}$

$Z^+ = \{Z W\}$

$W^+ = \{W\}$

$\begin{matrix} X \\ | \\ Z \\ | \\ W \end{matrix}$

$XZ^+ = \{XZ W. Y\}_{ck}$

$XW^+ = \{XW YZ\}_{ck}$

$ZW^+ = \{ZW\}_x$

CK = Y^+, XZ, XW

7) R(ABCDEF)

AB → C

DC → AE

E → F

B & D are essential attribute

$BD^+ = \{BD\}_x$

$ABD^+ = \{ABDCEF\}_{ck}$

$CBD^+ = \{CBDAE\}_{ck}$

$EBD^+ = \{EBDF\}$

$FBD^+ = \{FBD\}_x$

$EFBD^+ = \{EFBD\}_x$

C.K = ABD, CBD

8) R(ABCDEFGHIT)

AB → C

AD → GH

BD → EF

A → I

H → T

A, B, D are essen

$ABD^+ = \{ABDCGH T I E\}$

ABD is CK

9) R(ABCDE)

BC → ADE

D → B

C is essential

$AC^+ = \{AC\}$

$BC^+ = \{BCADE\}_{ck}$

$CD^+ = \{CDBADE\}_{ck}$

$EC^+ = \{EC\}$

$AEC = \{AEC\}_x$

C.K BC, (C)

10) R(A B C D E F)

$AB \rightarrow C$
 $C \rightarrow D$
 $D \rightarrow BE$
 $E \rightarrow F$
 $F \rightarrow A$

$A^+ = \{A\}$
 $B^+ = \{B\}$
 $C^+ = \{C D B E F A\}_{ck}$
 $D^+ = \{D B E F A C\}_{ck}$
 $E^+ = \{E F A\}$
 $F^+ = \{F E F A B\}$

A
B
C
D
E
F

$AB^+ = \{A B C D E F\}_{ck}$

$AF^+ = \{A F\}$

$BF^+ = \{B F A C D E\}_{ck}$

$AE^+ = \{A E F\}$

$BE^+ = \{B E F A C D\}_{ck}$

$FE^+ = \{F E F A\}_x$

$AEF^+ = \{A E F\}_x$

$ck, \{C, D, AB, BF, BE\}$

11) R(A B C D E F G H)

$CH \rightarrow G$
 $A \rightarrow BC$
 $B \rightarrow CFH$
 $E \rightarrow A$
 $F \rightarrow EG$

D is essential

$AD = \{A D B C F H E G\}_{ck}$

$BD = \{B D\}$

12) R(A B C)

F: $A \rightarrow BC$
 $B \rightarrow C$
 $A \rightarrow C$
 $AB \rightarrow C$

A is essential attribute

$A^+ = \{A B C\}_{ck}$

So minimal cover is $\{A\}$

$A \rightarrow B$ ✓
 ~~$A \rightarrow C$~~
 $B \rightarrow C$ ✓
 ~~$A \rightarrow B$~~
 ~~$A \rightarrow C$~~
 ~~$AB \rightarrow C$~~

$A \rightarrow B$
 $A^+ = \{A B C\}$
 $A^+ = \{A C\}_x$

$A \rightarrow C$
 $A^+ = \{A B C\}$
 $A^+ = \{A B C\}$

$AB^+ = \{A B C\}$

$AB^+ = \{A B C\}$

$B \rightarrow C$
 $B^+ = \{B C\}$
 $B = \{B\}$

$\left[\begin{array}{l} A \rightarrow B \\ B \rightarrow C \end{array} \right]$

$A \rightarrow C$
 $A^+ = \{A B C\}$
 $A^+ = \{A B C\}$

~~$A \rightarrow C$~~

2NF:

R(ABCD)

$AB \rightarrow D$

$B \rightarrow C$

$AB^+ = \{ABCD\}$

$CK = \{AB\}$

* A & B are prime attribute

* C & D are non-prime attribute

$AB \rightarrow D \Rightarrow$ Fully F.D.

$B \rightarrow C \Rightarrow$ Partial F.D

↗ If B becomes null then we can't compute D as a result the prop. of prime attribute is violated

2NF: 1NF & No Partial F.D

R(ABCD)

$R_1(ABD)$

$R_2(BC)$

R(ABC)

$B \rightarrow C$

AB is the candidate key

A, B are Prime Attr.

C is N.P. Attr.

$AB^+ = \{ABC\}$

there is partial dependency

$R_1(AB)$

$R_2(BC)$

Convert to 2NF

(i) R(ABCDE)

$AB \rightarrow C$

$D \rightarrow E$

$ABD^+ = \{ABDCE\}_{CK}$

A, B, D are prime

C, E are N.P.

$AB \rightarrow C$ (Partial F.D)

$D \rightarrow E$ (Partial)

$R_1(ABC)$

$R_2(DE)$

$R_3(ABD)$

ii) R(ABCDE)

$A \rightarrow B$

$B \rightarrow E$

$C \rightarrow D$

$AC^+ = \{ACBED\}_{CK}$

A, C are prime

B, D, E are N.P.

$A \rightarrow B$ (P.D)

$B \rightarrow E$ (F.F.D)

$C \rightarrow D$ (P.D)

↗ $R_1(ABE)$

$R_2(CD)$

$R_3(AC)$

3) $R(ABCDEFGHIJ)$

$AB \rightarrow C$
 $AD \rightarrow GH$
 $BD \rightarrow EF$
 $A \rightarrow I$
 $H \rightarrow J$

$ABD^+ = \{ABCDGHEFIJ\}_{ck}$

A, B, D are prime attr.
 C, E, F, G, H, I, J are non-prime attr.

$AB \rightarrow C$ (P.D)
 $AD \rightarrow GH$ (P.D)
 $AD \rightarrow G$ $AD \rightarrow H$

$BD \rightarrow EF$ (P.D) $H \rightarrow J$ (F.D)
 $A \rightarrow I$ (P.D)

$R_1(ABC)$ $R_3(BDEF)$ $R_5(ABD)$
 $R_2(ADGHT)$ $R_4(AI)$

3NF:- (i) 2NF

(ii) No transitive dependency

$R(ABCD)$

$AB \rightarrow C$ (F.F.D) $AB^+ = \{ABCD\}_{ck}$

$C \rightarrow D$ (-) A, B are prime
 C, D are N.Prime

The above one is in 2NF

Here there is transitive dependency
(N.P $\rightarrow$ N.P)

$R_1(ABC)$ $R_2(CD)$] $\rightarrow$ 3NF

AB se 'C' mil utarti aarti 'C' null hua to h 'D' mil
 and it violates the rule that AB ~~can~~ can key nikal part

Q(1) $R(ABCDE)$

$AB \rightarrow C$ (F.F.D)
 $B \rightarrow D$ (P.D)
 $D \rightarrow E$ (-)

$AB^+ = \{ABCDE\}_{ck}$

A, B are Prime attr.
 C, D, E are Non Prime

Not in 2NF

$R_1(ABC)$
 $R_2(BDE)$ $R_{12}(BD)$
 $R_{12}(DE)$
 ~~$R_3(AB)$~~

2) $R(AB C D E F G H I J)$

$AB \rightarrow C$ (P.F.D)

$A \rightarrow DE$ (P.P)

$B \rightarrow F$

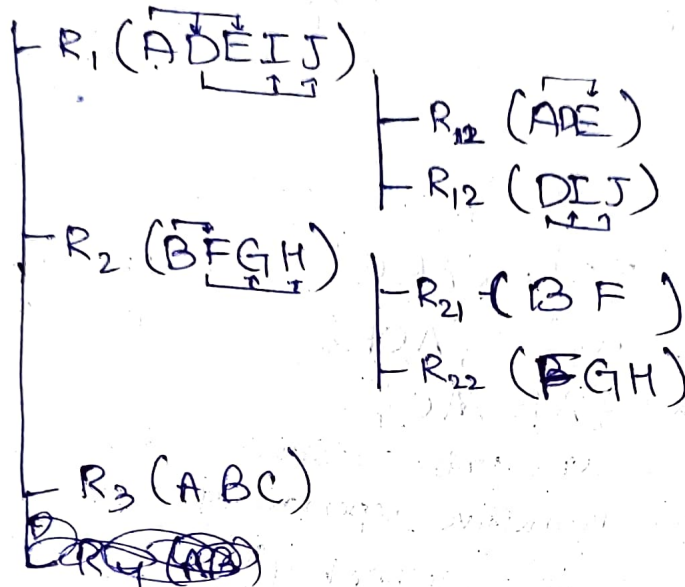
$F \rightarrow GH$

$D \rightarrow IJ$

$AB^+ = \{AB C D E F G H I J\}$

A, B are prime

C, D, E, F, G, H, I, J are N.P



3) $R(AB C D E F G H I J)$

$AB \rightarrow C$

$BD \rightarrow EF$ (P.F)

$AD \rightarrow GH$ (P.P)

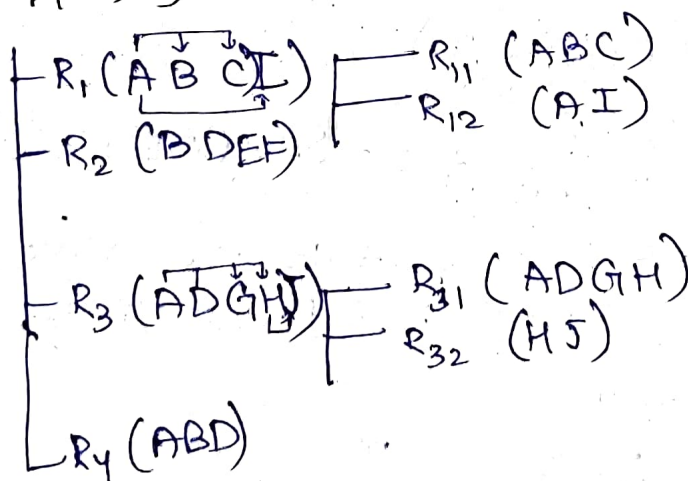
$A \rightarrow I$ (P.P)

$H \rightarrow J$

~~$AB^+ = \{AB C D E F G H I J\}$~~

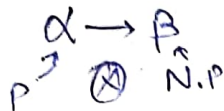
$ABD^+ = \{AB D C E F G H I J\}$

~~$ABC I$~~



BCNF:-

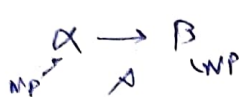
2NF



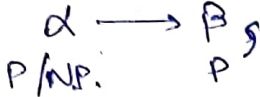
(i) 3NF

(ii) All determinants must be candidate key

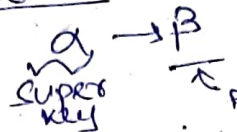
3NF



BCNF



BCNF



$R(ABC)$

$AB \rightarrow C$

$AB^+ = \{ABC\}$

$B \rightarrow A$

$AC^+ = \{ACB\}$

$C.k = \{AB, AC\}$

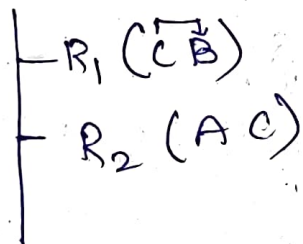
A, B, C are prime attr.

No transitive dependency

in 3NF

but not in BCNF

$C \rightarrow B \Rightarrow (C \text{ is not a superkey})$



Q) $R(\overline{A}\overline{B}\overline{C}\overline{D}\overline{E}\overline{F}\overline{G}\overline{H}\overline{I}\overline{J})$

$AB \rightarrow C$ (F.D)

$A \rightarrow DE$ (P.D)

$B \rightarrow F$

$D \rightarrow IJ$

$F \rightarrow GH$

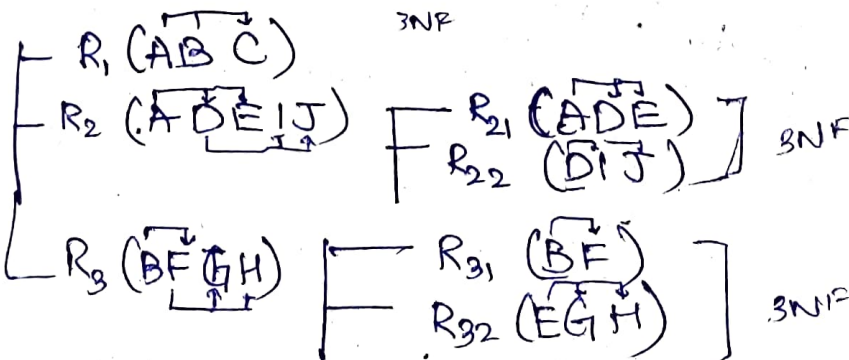
$AB^+ = \{ABCDEFGHIJ\}$

A, B are prime.

C, D, E, F, G, H, I, J are NP

1st NF ✓

Not in 2NF



Q) $R(A, B, C, D, E)$

F: $\{ AB \rightarrow C$

$B \rightarrow D$ (P.P)

$A \rightarrow E$ }

$AB^+ = \{ ABCDE \}_{CK}$

A, B are PK

C, D, E are N.P

$R_1 (A \overline{B} C \overline{E})$

$R_2 (B \overline{D})$

$R_1 (A \overline{B} C)$

$R_2 (B \overline{D})$

$R_3 (A \overline{E})$

$R_{12} (A \overline{B} C)$

$R_{12} (A \overline{E})$

Q) $R(ABCDE)$

F: $A \rightarrow BC$

$CD \rightarrow E$

$B \rightarrow D$

$E \rightarrow A$

$R_1 (ABC)$

$R_2 (ADE)$

Lossless Join proved w/Dec.

$R_1 \cup R_2 = ABCDE$ ✓

$R_1 \cap R_2 = (A)$

$R_1 (ABC)$

$A \rightarrow BC$

$A^+ = \{ ABC \}$

$R_2 = \{ ADE \}$

$E \rightarrow A$

$DE^+ = \{ DE A \}$

$A^+ \quad DE^+$

$R_1(ABC) \quad R_2(ADE)$

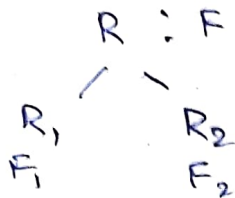
$A \rightarrow BC$
 $CD \rightarrow E$
 $B \rightarrow D$
 $E \rightarrow A$

A
 D
 $E \rightarrow A$
 AD
 DE
 AE

(A) super key
lossless hence the dec. is r/s & t

Dependency Preser:

Not mandatory



$$(F_1 \cup F_2)^+ = F^+$$

Q1) R(ABC)

$$A \rightarrow B$$

$$B \rightarrow C$$

$$C \rightarrow A$$

R₁(AB)

R₂(BC)

$$\begin{array}{l}
 F_1: A \rightarrow B \\
 B \rightarrow A \\
 (B \rightarrow C, C \rightarrow A)
 \end{array}$$

$$\begin{array}{l}
 F_2: B \rightarrow C \\
 C \rightarrow B \\
 (C \rightarrow A, A \rightarrow B)
 \end{array}$$

$$C^+ = \{CAB\}$$

$$F_1 \cup F_2 = F$$

$$(A \rightarrow B)(B \rightarrow C)(B \rightarrow A, C \rightarrow B)$$

Q2) R(ABCD)

$$AB \rightarrow CD$$

$$D \rightarrow A$$

R(AD)

$$\begin{array}{l}
 F_1: (A \rightarrow D) \times \\
 D \rightarrow A
 \end{array}$$

R(BCD)

$$\begin{array}{l}
 \cancel{B \rightarrow A} \\
 \cancel{C \rightarrow A} \\
 \cancel{D \rightarrow A} \\
 \cancel{AB \rightarrow CD} \\
 \cancel{CD \rightarrow AB} \\
 \cancel{BD \rightarrow AC}
 \end{array}$$

$$\begin{array}{c}
 \textcircled{BD} \textcircled{A} \\
 \textcircled{CD}
 \end{array}$$

$$AB^+ = \{AB\}$$

Depend $\times$

$F(PQRST)$

$F: PQ \rightarrow R$
 $S \rightarrow T$

$PQ \rightarrow R$ (P.D.)
 $S \rightarrow T$ (P.D.)

$R_1 (PQR)$

$R_2 (ST)$

$R_3 (PQS)$

$PQST = \{PQRST\}_{CR}$

P, Q, S are pr.
 R, T are NP

$R(ABC)$

~~$A \rightarrow BC$~~
 ~~$B \rightarrow C$~~
 ~~$A \rightarrow C$~~
 ~~$AB \rightarrow C$~~

$A \rightarrow C$

$A^+ = AC$

$A^+ = A$

$A \rightarrow BC$

$A^+ = \{ABC\}$

$A^+ = \{ABC\}$

$B \rightarrow C$

$B^+ = BC$

$B^+ = B$

$AB \rightarrow C$

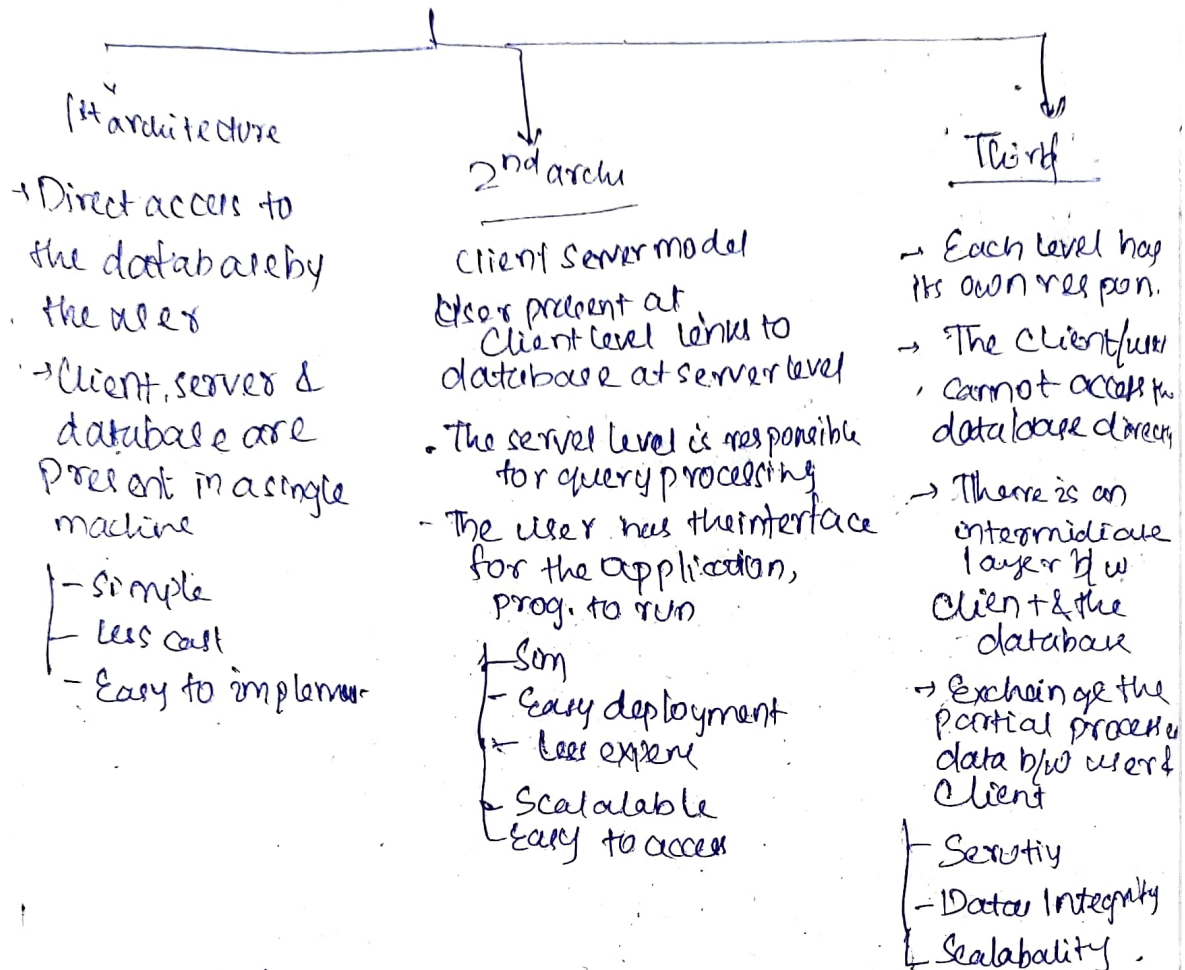
$AB^+ = \{ABC\}$

$AB^+ = \{ABC\}$

Architecture:

Focuses on managing design and administration of software that manages the actual data in the application.

→ Affects the performance



View of data:

view of data can be referred as the view the abstract data from the database

Abstract: ~ hiding irrelevant details from the user.

(i) Physical:

- lowest level of abstr
- Describes how the database is being stored in secondary memory devices like disk, tapes.
- Most of user are unaware of the locat
- Defines method to access the abstract-data

(ii) Conceptual

- Intermediate layer/level of data abstraction.
- Describes what type of data is being stored in the database & their relation
- The store of data in the form of table
- Database administrator decides what data to keep

View Highest level of

→ meant for end user to, from the user get the data by querying the query

→ Hides details

→ External level.

Data Independence

change of data in one level doesn't affect the data in another level.

Logical

- Clearer of change in the conceptual schema that does not affect the external schema
- Separate
- Difficult to implement as it depends completely on the logical str of data
- ex: Adding on new attribute

Physical

- Change in internal schema without affecting the external schema
- Easy to implement
- Separate internal schema from conceptual schema
- Changing the storage type

Instance

→ Shows the data stored in the database at a particular instance of time.

→ Change free

→ Data instance can with insertion, updation & deletion

→ Extension of Schema

Schema

→ Structure of the database

→ Doesn't change from

→ Same for the whole database

→ Intension

→ Does not rep. the datatype.

Data Integrity:

Set of predefined rules used to maintain the quality of information.

→ Domain constraint (Valid set of values)

→ NOT NULL

→ Entity Integrity constraint

→ Key constraint

→ Primary key constraint

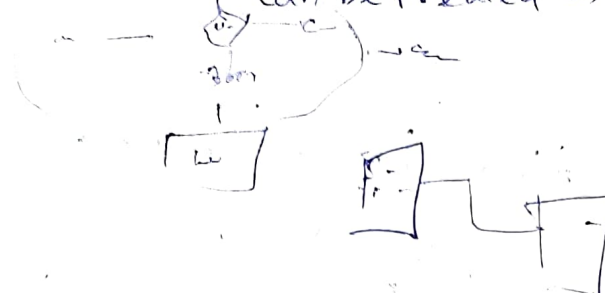
→ Reference integrity constraint

Ag.

Aggregation

→ Shows the relationship b/w two or more relationship set

→ Can be treated as single entry



Set Difference

$R - S$

All values of R are present but not in S



Natural Join

→ Common at

→ Does not have any equicondⁿ

→ Same as equi join difference is in natural join the common attribute appears only once in the relational schema

View ! Virtual set based on the result set of an SQL statement

Table & View :

- (i) Table has physical existency, view is stored ^{result} set of SQL Query.
- (ii) View is defined over the top of the table and does not hold data themselves.
- (iii) View dependence on table but table is independent

Query info. is used to measure the cost of query process in the data base.

Used to determine the selective factor for query process
Based on the Estimated cost the evaluation engine
select the best plans & makes the execution & chooses the most efficient one.

Blocking Factor:

No. of tuples fit in one block

$$\frac{N_R}{B_R}$$

Selective Attribute of A

No. of tuples in A that satisfies the equality condⁿ of A

$$\frac{\text{No. of tuple}}{\text{Total}} = \frac{N_k}{V(A, R)}$$

Measure of Query Cost :-

Execn in
① disk,
CPU

parallel or distrib. system

We chose disk access cost to compute cost query over
CPU ~~cost~~ as it is (state is slow)

Read pages from disk to memory

Write pages back to disk

So the transfer of no. of block to/from disk to
seek is used for query cost.

④ Join operation :-

Most expensive as it is used to join two or more data.

① Nested

simple
iterates over each tuple in one relation & min

$$b_2 + (t_2 \cdot b_1)$$

Index — Simple
 — Reduce the risk of full scan.
 Cost $b_R + b_P$. Cost of index lookup

Sort Merge

Efficient for large dataset & efficient when both relations are sorted.

$$b_R \log(b_R) + b_S \log(b_S) + b_R + b_S$$

Hash Join!

Efficient in equi join with unsorted data set

$$b_R + b_S + \text{hash cost}$$

Block-Index

→ process relation based on the no. of blocks rather than per tuple

Heuristic based

Simple, faster

(Quick & efficient for some)
 Basic ops

Join
 Selection
 Projection
 Agg

Logical Optimisation

- Select
- Project
- Join reordering
- Agg selection

Physical

select the best

- a) Index use - speed up
- b) Join algorithm
- c) Parallel query exec

Semantic Query Optimisation

- Eliminating redundancy
- Exploiting constraint
- Cost folding