

Decimal	Octal	Hexadecimal	Binary
0	0	0	0
1	1	1	01
2	2	2	10
3	3	3	11
4	4	4	100
5	5	5	101
6	6	6	
7	7	7	
8	10	8	
9	11	9	
10	12	A	
	13	B	
19	20	C	
20		D	
		E	
29	27	F	

* * Decimal to Binary

(i) Here, the decimal number is repeatedly divided by 2 till the quotient becomes '0' and remainder after each division is used to indicate the coefficient of binary number to be formed.
The binary numbers are written from bottom to top.

(ii) Last remainder is msb and first remainder is lsb.

(iii) If any fractional numbers are there then multiply the number repeatedly by 2 till the fractional part becomes zero.

$$(41.8125)_{10} = (\quad)_2$$

$$\begin{array}{r}
 2 \overline{) 41} \\
 \underline{20} - 1 \quad (\text{Least significant bit}) \\
 2 \overline{) 10} - 0 \\
 2 \overline{) 5} - 0 \\
 2 \overline{) 2} - 1 \\
 \underline{1} - 0 \quad (\text{Most significant bit}) \\
 \text{MSB}
 \end{array}$$

~~Read~~

101001

Ans. 101001.1101.

$$\begin{array}{l}
 0.8125 \times 2 = 1.6250 \quad \text{① (MSB)} \\
 0.6250 \times 2 = 1.2500 \quad \text{①} \\
 0.2500 \times 2 = 0.5000 \quad \text{①} \\
 0.5000 \times 2 = 1.0000 \quad \text{① (LSB)}
 \end{array}$$

Binary to Decimal

→ Any binary number can be converted into its equivalent decimal number using weight assigned to each bit position.

$$Q. \text{ Convert } (101001.1101)_2 = (\quad)_{10}$$

$$\begin{array}{r}
 \begin{array}{cccccc}
 2^5 & 2^4 & 2^3 & 2^2 & 2^1 & 2^0 \\
 1 & 0 & 1 & 0 & 0 & 1
 \end{array}
 & = & 1 \times 2^5 + 1 \times 2^3 + 1 \times 1 + 1 \times 2^{-1} + 1 \times 2^{-2} + 1 \times 2^{-4} \\
 & = & 32 + 8 + 1 \\
 & = & 41
 \end{array}$$

$$\begin{array}{l}
 = 41 + \frac{1}{2} + \frac{1}{4} + \frac{1}{16} \\
 = 41 + (0.5 + 0.25 + 0.0625) \\
 = 41.8125
 \end{array}$$

* Decimal to Octal:-

In octal system base is 8.

- ① First divide the ~~octal~~ number repeatedly by 8, till the quotient becomes '0' and record its remainder.

$$(153)_{10} = ()_8$$

$$\begin{array}{r} 8 \overline{) 153} \\ \underline{8 } 19 \\ \underline{16} 3 \\ \underline{24} 0 \end{array} \quad \begin{array}{l} \text{LSB} \\ \uparrow \\ \text{MSB} \end{array} \quad (231)_8$$

$$(153.26)_{10} = (231.2050)_8$$

$$\begin{array}{rcl} 0.26 \times 8 & = & 2.08 \quad \textcircled{2} \\ 0.08 \times 8 & = & 0.64 \quad \textcircled{0} \\ 0.64 \times 8 & = & 5.12 \quad \textcircled{5} \\ 0.12 \times 8 & = & 0.96 \quad \textcircled{0} \end{array}$$

* Octal to Decimal

$$(231.2050)_8 = ()_{10}$$

$$\begin{aligned} &= (2 \times 8^2 + 3 \times 8^1 + 1 \times 8^0 + 2 \times 8^{-1} + 0 + 5 \times 8^{-3} + 0) \\ &= (153.26)_{10} \end{aligned}$$

$$\begin{array}{r} 16 \\ 2 \\ \hline 32 \end{array} \quad \begin{array}{r} 16 \\ 3 \\ \hline 48 \end{array}$$

* Decimal to Hexadecimal

$$(489)_{10} = (\quad)_{16}$$

$$\begin{array}{r} 16 \overline{) 489} \\ 16 \overline{) 30} - 9 \text{ (LSB)} \\ 16 \overline{) 1} - 1 \text{ (MSB)} \\ 0 \rightarrow 1 \end{array}$$

$$\begin{array}{r} 0 \\ 16 \overline{) 1} \\ 16 \overline{) 0} \\ 1 \end{array}$$

$$\begin{array}{r} 16 \overline{) 30} \\ 16 \\ \hline 14 \end{array}$$

$$\begin{array}{r} 36 \\ 16 \overline{) 489} \\ 481 \\ \hline 89 \\ 80 \\ \hline 9 \end{array}$$

$$(1E9)_{16}$$

* Hexadecimal to Decimal

$$(1E9)_{16} = (\quad)_{10}$$

$$\begin{aligned} &= (1 \times 16^2 + E \times 16^1 + 9 \times 16^0) \\ &= (256 + 224 + 9) = \underline{489} \end{aligned}$$

$$\begin{array}{r} 2 \\ 14 \\ \hline 16 \\ 89 \\ 16 \\ \hline 224 \\ 256 \\ \hline 489 \end{array}$$

* Octal Number to binary

$$(237)_8 = (\quad)_2$$

For converting octal to binary express each octal digits into its 3 bit binary notation.

$$\begin{array}{c} (2 \ 3 \ 7)_8 = (\quad)_2 \\ \swarrow \quad \downarrow \quad \searrow \\ (010 \ 011 \ 111)_2 \end{array}$$

$$\begin{array}{c} 237.67 \\ \downarrow \quad \searrow \\ 110 \quad 111 \end{array}$$

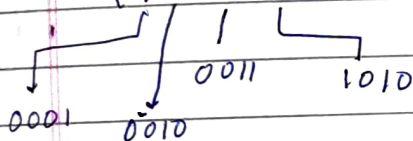
* Binary to Octal

$$0(01101101101)_2 = (1555)_8$$

$$0.101011100 = (\quad)_8$$

* Hexadecimal to binary

$$(123A)_{16} = (\quad)_2$$

* Binary to HexadecimalAddition in Number SystemBinary

$$\begin{array}{r} 101101 \\ 100001 \\ \hline 1001110 \end{array}$$

$$\begin{array}{r} 10111 \\ + 01110 \\ \hline 100101 \end{array}$$

$$\begin{aligned} 0+0 &= 0 \\ 0+1 &= 1 \\ 1+0 &= 1 \\ 1+1 &= \textcircled{1}0 \text{ carry} \end{aligned}$$

1

$$\begin{array}{r} 1001110 \\ 1001110 \\ \hline 1001110 \end{array}$$

$$\begin{array}{r} 10111011 \\ 10101011 \\ \hline 10110010 \\ 10110010 \end{array}$$

→ Octal addition

$$(235)_8 + (164)_8 = (\quad)_8$$

$$\begin{array}{r} 1 \text{ } \textcircled{1} \\ 2 \ 3 \ 5 \\ 1 \ 6 \ 4 \\ \hline 4 \ 2 \ 1 \end{array}$$

Direct

$$\begin{array}{r} 11 \quad 110 \\ 010 \ 011 \ 101 \\ 001 \ 110 \ 100 \\ \hline 100 \ 010 \ 001 \rightarrow 4 \ 2 \ 1 \end{array}$$

through binary.

→ Hexadecimal addition

$$(123A)_{16} + (EA45)_{16} = (\quad)_{16}$$

$$\begin{array}{r} 1 \ 2 \ 3 \ A \\ E \ A \ 4 \ 5 \\ \hline F \ C \ 7 \ F \end{array}$$

$$Q. (1567)_8 + (AEC D)_{16} = (\quad)_{16}$$

$$(1567)_8 = (\quad)_{16}$$

Diagram showing conversion of octal 1567 to binary and then to hexadecimal:

1 (001) → 1
5 (101) → 5
6 (110) → 6
7 (111) → 7

Resulting in 1567 in hexadecimal.

$$\begin{array}{r} 1 \ 1 \\ 1 \ 3 \ 7 \ 7 \\ + \ A \ E \ C \ D \\ \hline 2 \ 4 \ 4 \end{array}$$

0	
1	
2	
3	
4	
5	
6	
7	
8	
9	
A	- 10
B	- 11
C	- 12
D	- 13
E	- 14
F	- 15
10	- 16
11	- 17
12	- 18
13	- 19
14	- 20
15	- 21
16	- 22
17	- 23
18	- 24
19	- 25
20	- 26
21	- 27
22	- 28
23	- 29
24	- 30
25	- 31

1+2+4

$$\begin{array}{r} 12 \\ 14 \\ 16 \\ 18 \end{array}$$

Signed magnitude representation $(+5)$ (-5) $\downarrow$ $(0, 101)$ $(1, 101)$

$$-20 = \left(\underset{\substack{\uparrow \\ \text{sign}}}{1}, \underbrace{10100}_{b_{20}} \right)$$

1's complement

$$(-101101)_2$$

$$1's \rightarrow 010010$$

$$2's \rightarrow 1's + 1$$

$$= 010011$$

$$\begin{array}{r} 010010 \\ + 1 \\ \hline 010011 \end{array}$$

$$100100$$

$$\begin{array}{r} 1's \rightarrow 011011 \\ + \\ \hline 011010 \end{array}$$

8 bit

Q. Represent -9 in signed magnitude representation, 1's complement, 2's complement

$$\begin{array}{cccc} 2^3 & 2^2 & 2^1 & 2^0 \\ 1 & 0 & 0 & 1 \end{array}$$

$$-9 = (1001)_2$$

$$= (1, 0001001)_2$$

$$-9(1's) = 1, 1110110$$

$$-9(2's) = 1, 10111$$

Binary Subtraction :-

$$\begin{array}{r} (1000)_2 \\ 11 \end{array}$$

$$0 - 0 = 0$$

$$1 - 1 = 0$$

$$1 - 0 = 1$$

$$0 - 1 = 1$$

Subtraction

The subtraction of unsigned number $m-n$ in base r can be done as follows :-

$M \rightarrow$ minued bit

$N \rightarrow$ Subtrahend bit.

- (i) Both no. i.e. 'minued & subtrahend must have same number of digits, if it is not, add 0 to the left side of the number, add the minued 'm' to the RS complement of Subtrahend 'N'.
- (ii) If $m > n$,

Q. 10's complement subtract $(72532 - 3250)$

$$M \rightarrow 72532$$

$$N \rightarrow 03250$$

$$M + (-N)$$

$$\begin{array}{r} 72532 \\ - 3250 \\ \hline 69282 \end{array}$$

$$\begin{array}{r} 10\text{'s of } N \rightarrow 99910 \\ \quad \quad \quad 03250 \\ \hline 96750 \end{array}$$

M + 10's of N

$$\begin{array}{r} 72532 \\ + 96750 \\ \hline 69282 \end{array}$$

Q. $3250 - 72532$

$$M = 03250$$

$$N = 72532$$

$$10\text{'s of } N = \overset{99910}{\cancel{72532}}$$

Q. 9's complement Subtract $(72532 - 3250)$

$$M = 72532 \quad M + (-N)$$

$$N = 3250$$

$$\begin{array}{r} 72532 \\ - 3250 \\ \hline 69282 \end{array}$$

$$\begin{array}{r} 9\text{'s of } N \\ 99999 \\ - 03250 \\ \hline 96749 \end{array}$$

M + 9's of N

$$\begin{array}{r} 72532 \\ + 96749 \\ \hline 69281 \end{array}$$

Q. $(7188 - 3049)$ using complement method.

$$M = 7188$$

$$N = 3049$$

$$\begin{array}{r} 7188 \\ - 3049 \\ \hline 4139 \end{array}$$

$$M > N$$

$$\begin{array}{r} 10's \text{ complement of } N, \quad 999 \quad 10 \\ \quad \quad \quad 3049 \\ \hline \quad \quad \quad 6951 \end{array}$$

$M + 10's \text{ complement}$

$$\begin{array}{r} 7188 \\ 6951 \\ \hline 14139 \\ \hline \end{array}$$

remove $\leftarrow$ ①

Q. $(2997 - 7992)$

$$M = 2997$$

$$N = 7992$$

$$M < N$$

$$\begin{array}{r} 10's \text{ complement of } N, \rightarrow 999 \quad 10 \\ \quad \quad \quad 7992 \\ \hline \quad \quad \quad 2008 \end{array}$$

$M + 10's \text{ complement}$

$$\begin{array}{r} 2997 \\ 2008 \\ \hline 5005 \end{array}$$

$$\begin{array}{r} 10's \text{ complement} \quad 999 \quad 10 \\ \quad \quad \quad 5005 \\ \hline - 4995 \\ \hline \end{array}$$

$$Q. \quad (11011 - 11001)_2$$

$$M - 11011$$

$$N - 11001$$

$$\begin{array}{r} 2's \text{ complement} - 00110 \\ + 1 \\ \hline 00111 \end{array}$$

$$\begin{array}{r} M + 2's \text{ complement} \\ 11011 \\ 00111 \\ \hline \end{array}$$

$$\text{Remainder} \leftarrow \textcircled{100010}$$

$$Q. \quad 1011 - 110000$$

$$\begin{array}{r} 16 \\ 8 \\ 2 \\ \hline 27 \end{array}$$

$$\begin{array}{r} 16 \\ 8 \\ 1 \\ \hline 25 \end{array}$$

LOGIC GATES

AND



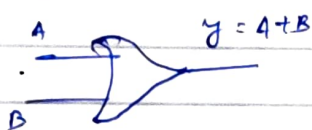
A	B	Y
0	0	0
0	1	0
1	0	0
1	1	1

NOT



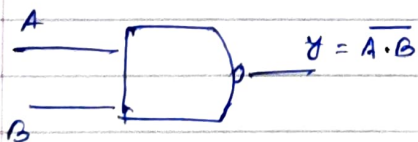
A	$\bar{A}$
0	1
1	0

OR



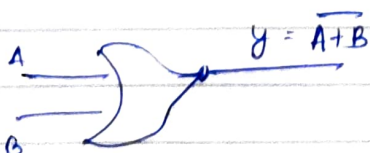
A	B	Y
0	0	0
0	1	1
1	0	1
1	1	1

NAND



A	B	Y
0	0	1
0	1	1
1	0	1
1	1	0

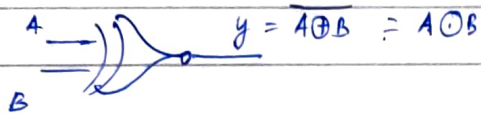
NOR



A	B	Y
0	0	1
0	1	0
1	0	0
1	1	0

Ex-OR

A	B	$y = \bar{A}B + A\bar{B}$
0	0	0
0	1	1
1	0	1
1	1	0

Ex-NOR

A	B	$y = AB + \bar{A}\bar{B}$
0	0	1
0	1	0
1	0	0
1	1	1

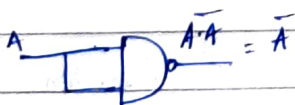
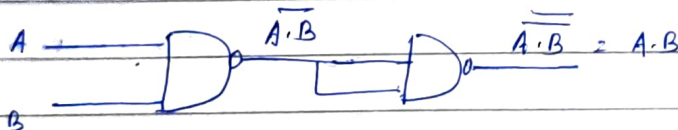
Basic gates

AND, OR, NOT, Ex-OR, Ex-NOR

Universal gates

NAND, NOR

Q. Design AND gate using NAND & NOR



Boolean Algebra is used for solⁿ of Boolean expression. These are set of rules or an algebraic structure defined on set of elements together with two binary operator (+) & ($\cdot$). These set of rules formulated by English Mathematician George Boole which outcome will be true or false.

① Complementation Law :-

$$X \cdot \bar{X} = 0$$

$$X + \bar{X} = 1$$

② Commutative Law :-

$$X + Y = Y + X$$

$$X \cdot Y = Y \cdot X$$

③ AND Law :-

$$X \cdot 0 = 0$$

$$X \cdot 1 = X$$

$$X \cdot X = X$$

$$X \cdot \bar{X} = 0$$

④ OR Law

$$X + 0 = X$$

$$X + 1 = 1$$

$$X + X = X$$

$$X + \bar{X} = 1$$

⑤ Distributive Law

$$X \cdot (Y + Z) = X \cdot Y + X \cdot Z$$

$$X + (Y \cdot Z) = (X + Y) \cdot (X + Z)$$

$$X + \bar{X} \cdot Y = X + Y$$

⑥ Associative Law :-

$$X + (Y + Z) = (X + Y) + Z$$

$$X (Y \cdot Z) = (X \cdot Y) \cdot Z$$

⑦ Absorption Law :-

$$X + X \cdot Y = X$$

$$X (X + Y) = X$$

⑧ Consensus law / Term law:-

$$x \cdot y + \bar{x}z + yz = xy + \bar{x}z$$

$$(x+y)(\bar{x}+z)(y+z) = (x+y)(\bar{x}+z)$$

⑨ Transposition law

$$xy + \bar{x}z = (x+z)(\bar{x}+y)$$

$$(\bar{x}+y)(\bar{x}+z) = xz + \bar{x}y$$

⑩ De Morgan's Theorem:-

$$\overline{x+y} = \bar{x} \cdot \bar{y}$$

$$\overline{x \cdot y} = \bar{x} + \bar{y}$$

11) Validity Theorem:-

$$Q. (a) \quad x [y + z \cdot (\overline{x \cdot y + x \cdot z})]$$

$$= x [y + z \cdot (\overline{x \cdot y} \cdot \overline{x \cdot z})]$$

$$= x [y + z \cdot \{(\bar{x} + \bar{y}) \cdot (\bar{x} + \bar{z})\}]$$

$$= x [y + z \cdot (\bar{x} + (\bar{y} \cdot \bar{z}))]$$

$$= x [y + z \cdot (\bar{x} + (\bar{y} + \bar{z}))]$$

$$= x [y + z \cdot \bar{x} + z \cdot (\bar{y} + \bar{z})]$$

$$= x [y + z \cdot \bar{x} + \cancel{z \cdot \bar{y} \cdot \bar{z}}^0]$$

$$= xy + \cancel{x \bar{x} z}^0$$