B.Tech-5th(IT)

Design & Analysis of Algorithms

Full Marks: 50

Time: $2\frac{1}{2}$ hours

Answer all questions

The figures in the right-hand margin indicate marks

Symbols carry usual meaning

1. Answer all questions:

- 2×5
- (a) What do you mean by time complexity and space complexity of an algorithm?
- (b) Differentiate between dynamic programming and divide-and-conquer algorithm.
- (c) What is the worst case time complexity of QUICK SORT algorithm and on what input data does it exhibit its worst behavior?

- (d) Find the time complexity of brute force algorithm for string matching problem if text and pattern are of length n and m respectively.
- (e) Explain the differences between decision and optimization problems.
- 2. (a) Write the Insertion sort algorithm and find the time complexity using Apriori analysis.
 - (b) Apply Merge Sort algorithm to sort the given list < 10, 1, 15, 8, 20, 7, 5, 30, 25>. 4

Or

(c) How many comparisons are needed to find the element 10 in the list <15, 10, 15, 20, 25, 30, 35> using Binary Search algorithm. Mention the low, mid and high index at each step.

- (d) Apply QuickSort algorithm to sort the given list <10, 1, 15, 5, 25, 30, 20>. Take the first element as the pivot element.
- 3. (a) Find the asymptotic bound for the following recurrence:

$$T(n) = 1$$
, if $n \le 4$
 $T(n) = 7T(n/2) + n^2$, if $n > 4$

- (b) Represent the amount of time using the θ notation for the following code segments:
 - (i) $for(i=n/2; i \le n; i++)$ $for(j=1; j \le n; j = 2)$ $for(k=1; k \le n; k = 2)$ x = x + 1;
 - (ii) for(i=1;i<=n;i++) { for (j=1;j<=n;j++) x=x+1; for(j=1;j<=n;j=2*j) x=x+1;

B.Tech-5th(IT)/Design & Analysis of Algorithms

(Turn Over)

Or

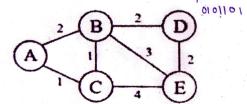
- (c) Compare Strassen's Matrix Multiplication with normal Matrix Multiplication in terms of number of additions and multiplications involved and their complexities.
- (d) Find the asymptotic bound for the following recurrence:

$$T(n)=1, \text{ if } n \le 4$$

$$T(n)=2T(\sqrt{n}) + \log n, \text{ if } n > 4$$

4. (a) Determine an LCS of <0, 1, 0, 0, 1, 0, - 4, 1, 0, 1> and <0, 1, 0, 1, 1, 0, 1, 1>. 4

(b)

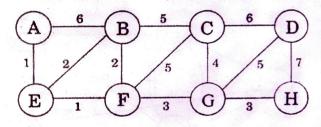


For the graph drawn above apply Prim's algorithm to find the minimum spanning tree.

(Continued)

Or

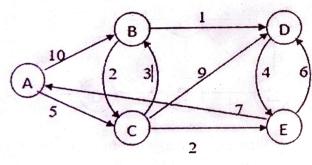
- (c) For the graph drawn below
 - (i) What is the cost of the minimum spanning tree?
 - (ii) If Kruskal's algorithm is applied, in what order are the edges added to the MST?



- (d) Find an optimal parenthesization of a matrix-chain product whose sequence of dimensions are <2,3,5,4,2>.
- 5. (a) There are 3 items, and the knapsack can hold 50 pounds. Item 1 weighs 10 pounds and is worth 60 dollars. Item

2 weighs 20 pounds and is worth 100 dollars. Item 3 weighs 30 pounds and is worth 120 dollars. Use greedy-choice property (fractional knapsack) to achieve maximum benefit.

(b) Find out the shortest path from vertex 'A' to all remaining vertices for the following graph using Dijkstra algorithm. 4



Or

(c) Find the least cost path for the travelling salesman problem for the below table.

Take node 1 as the source node.

C	1	2	3	4
1	0	10	15	20
2	5	0	9	10
3	6	13	0	12
4	8	8	9	0

- (d) A document is made up of characters a, b, c, d, e each occurring 22, 14, 20, 19 and 25 times respectively. What is the average length of the optimal Huffman code?
- 6. (a) Working modulo q = 11, how many spurious hits does the Rabin-Karp matcher encounter in the text T = 3141592653589793 when looking for the pattern P = 26?
 - (b) Discuss the relationship between the class P, NP, NP-complete, NP-hard problem with suitable example.

(Turn Over)

Or

- (c) Compute the prefix function (Pi) for the pattern P = abcaby and find the pattern in the text T = abxabcabcaby.
- (d) Approximate the Travelling salesman problem using MST.

