Tuning the magnetic properties of oleic-acid-coated cobalt ferrite nanoparticles by varying the surfactant coverage

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ABSTRACT

Organic coatings on magnetic nanoparticles are extensively used in various applications. As demonstrated recently, these coatings affect the magnetic behavior of the nanoparticles. The modification of the magnetic properties of the nanoparticles and nanoparticle assemblies, as the percentage of the oleic acid (OA) coverage of a cobalt ferrite nanoparticle increases, is investigated numerically using a multiscale modeling approach that combines density functional theory (DFT) and Monte Carlo simulations. The DFT calculations show that the increase in OA coverage results in a monotonic decrease of the mean magneto-crystalline anisotropy and in a reduction of the atomic magnetic moments and the exchange coupling constants in the nanoparticle. These effects are attributed to the gradual recovery of the bulk spinel structure at the coated surface, as the OA

coverage increases. Input from the DFT calculations is used in the mesoscopic modeling for the study of the magnetic behavior of an assembly of these nanoparticles by employing the Monte Carlo simulations technique. The results demonstrate that despite the decrease of magnetic anisotropy, the coercive field increases with the increase in percentage of OA coverage in the assembly, in agreement with experimental findings. This study suggests the possibility of tailoring the magnetic properties of cobalt ferrite nanoparticles for high-performance applications by varying the organic coating concentration.

1. Introduction

In recent decades, magnetic nanoparticles (MNPs) have greatly contributed to the development of a variety of cutting-edge technologies in fields such as biomedicine [1–3], environment [4,5] and energy [6], in the form of solid nanostructures and ferrofluids [7,8]. In these applications, nanoparticles exist in assemblies and tend to aggregate, often deteriorating the magnetic properties of the system [9]. To prevent this major drawback, one solution is coverage of the surface of these MNPs with an organic coating during or after their preparation.

The choice of organic coating is of great importance since it affects single and consequently collective magnetic properties of the nanoparticles. Indeed, the presence of a surfactant is often associated with different surface ion distribution [10] or surface spin arrangement, leading to the increase [11] or decrease of surface disorder [12–14]. This also influences the local effective magnetic anisotropy [15,16], the exchange coupling forces between the surface spins [10] and the particle saturation magnetization [10,17,18]. As a result, different ligands bonded at the surface of the MNPs affect the coercive field [19,20], the blocking temperature [21] and their magneto-hydrodynamic response [22]. In some cases, clustering of MNPs occurs during the coating process,

resulting in additional magnetic effects in an assembly [23–25]. The coating affects both the intraparticle characteristics and the interparticle interactions, offering the possibility of controlling the nanoparticles' magnetic behavior. The choice of an appropriate coating is essential for applications, particularly those requiring good colloidal stability of MNPs in liquids [26] and particles' biocompatibility [27,28].

The growing interest in coated MNPs, mainly iron-oxide based nanoparticles [21,25,29–36], focuses mainly on the fundamental understanding of the effect of the surfactant molecules on their magnetic properties. Less attention has been given to the effect of the amount of surface coverage, which is related to the particle synthesis protocol by which different MNP parameters (e.g. shape and size) are changed simultaneously. Although electronic structure calculations have been performed on uncoated spinel ferrite nanoparticles [25,37–39] in recent years, very few electronic structure calculations are reported on nanoparticles covered with organic ligands (see [40,41] on small Co clusters coated with varying percentage of organic or C–O molecules attached at their surface). These studies demonstrated that the different percentage of these molecules can affect their magnetic behavior. Furthermore, the effect of the coating depends on its type and on the MNP type (size and structure). The study of magnetic behavior becomes more complicated when ferrite nanoparticles are involved, because the bonding between metal atoms is replaced by the complex bonding between the transition metal (TM) ion and the O ion.

Cobalt ferrite (CoFe₂O₄) nanoparticles are among the most promising materials for biomedical (hyperthermia and magnetic particle imaging), environmental and technological applications [2,4,6,42-46] because of their high magneto-crystalline anisotropy. An oleic acid (OA, C₁₇H₃₃COOH) coating is commonly used for the preparation of CoFe₂O₄ nanoparticles, which provides steric stabilization against van der Waals and magnetic dipolar forces and thereby

prevents agglomerations; it also reduces the toxic effects of these nanoparticles [47,48]. Experimental results on the effect of the OA coating concentration on the magnetic behavior of the CoFe₂O₄ nanoparticles by Limaye et al. [51] showed that as the concentration of OA increases, the coercivity also increases. However, Jovanovitch et al. [50] found that the OA covalently bonded to the CoFe₂O₄ nanoparticle surface decreases the surface anisotropy and the coercive field of the ~6-nm OA-coated nanoparticles with the increase in OA surface coverage.

In this work, we investigate the effect of the OA surface coating concentration on the magnetic behavior of CoFe₂O₄ nanoparticle assemblies to elucidate the intriguing role of the increase of the number of OA molecules on the magnetic properties of the CoFe₂O₄ nanoparticles when bonded on their surface. Previous atomic- and mesoscopic-scale studies on the magnetic behavior of uncoated spinel ferrite nanoparticles introduced in the spin Hamiltonian the relevant intraparticle exchange coupling constants extracted from density functional theory (DFT) calculations on the corresponding bulk materials or from experimental considerations [24,52–54]. Here we take a step forward, by extracting the intraparticle magnetic parameters from DFT calculations, explicitly performed on OA-coated CoFe₂O₄ nanoparticles, taking into account the spinel structure and the core/surface morphology at the atomic (single particle) and the mesoscopic scale (assembly) [10]. We propose a multiscale modeling approach at three length scales: (1) DFT calculations on an OA-capped spherical CoFe₂O₄ particle of \sim 2 nm size with varying OA surface coverage, (2) atomic-scale calculations using input from the DFT results, for a spherical core/surface nanoparticle with the inverse spinel ferrite structure of 5 nm size (as in the experimental situation of [10,50]) with modified surface properties due to the OA coating and (3) a mesoscopic-scale approach for assemblies of core/surface nanoparticles of 5 nm size each, by rescaling the atomicscale parameters and including interparticle interactions. Our systematic study provides a thorough understanding of the underlying mechanism of the coating–nanoparticle interaction along the organic–inorganic interface and its effect on the macroscopic behavior of the assemblies. Thus, we can achieve better control of the magnetic properties of the CoFe₂O₄ nanoparticles covered with OA.

2. Theoretical calculations

Multiscale modeling is employed to investigate the hysteresis behavior of CoFe₂O₄ nanoparticles in the presence of OA coating by varying the percentage of surface coverage.

2.1 Electronic structure calculation of MNP parameters

The DFT calculations are performed based on spin-polarized DFT [55,56], implemented by the Vienna Ab Initio Simulation Package (VASP) code, in an inverse spinel ferrite nanoparticle with stoichiometric chemical formula CoFe₂O₄.

In our calculations the electronic charge density and the local potential are expressed in plane wave basis sets. The exchange correlation functional chosen is the one proposed by Perdew– Burke–Ernzerhof. The interactions between the electrons and ions are described using the projector augmented wave method and the GGA + U approach to treat localized states as proposed by Dudarev et al. [57]. All studied geometries are fully optimized (electronic relaxation, 10^{-4} eV; ionic relaxation, 10^{-3} eV). The initial structures are formed by replication of the bulk unit cell followed by a trimming procedure in order to obtain the spherical shape for the nanoparticles. The resulting structure is a spherical nanoparticle with inverse spinel structure and diameter $D \sim 2$ nm containing 246 atoms (70 Fe, 36 Co and 140 O atoms). Moreover, an empty space of 1.5 nm is used in all directions in order to avoid interaction with periodic images. For this CoFe₂O₄ nanoparticle, different numbers of bonded organic acid molecules (each containing 18 C, 2 O and 34 H atoms) per nanoparticle's surface area, are considered for the different percentages of the surface coverage. The spins of the TM ions between the A-sites and between the B-sites are ordered ferromagnetically and antiferromagnetically between the A–B sites in the initial spin configuration [59]. **Fig. 1** shows the most stable energy configuration (where the carboxylic acid coordinates with the metal ions as a monodentate ligand) found after several simulated structural relaxations, starting from different initial configurations.

We calculate the magnetic moments, the magneto-crystalline anisotropy energy (MAE) and the exchange coupling constants for the CoFe₂O₄ nanoparticle covered with 2, 3, 4, 6, 8, 11, 16, 19 and 22 OA molecules corresponding to 2.5%, 3.75%, 5%, 7.5%, 10%, 14%, 20%, 24% and 27% percentage of surface coverage, respectively. In **Fig. 1**, the relaxed structures for 5% and 7.5% surface coverage are shown.



Fig. 1. Relaxed structures of $CoFe_2O_4$ spherical nanoparticles with increasing number of organic molecules attached on their surface, corresponding to OA coverage of 5% (a) and 7.5% (b) (Fe (yellow), Co (bleu), O (red), C(brown), H(white)). For simplicity, OA molecules are not fully shown.

In **Table 1**, we calculate the total mean magnetic moment of the nanoparticle and the mean magnetic moment for each of the metal ions as a function of the OA surface coverage. In the calculation, the induced magnetic moment of the O atoms is also included. The total mean magnetic moment decreases as OA coverage increases. The decrease is faster with the increase of coverage up to 10% and then much slower up to 27%. The same decreasing trend is also observed for the mean magnetic moments of Fe^{3+}_A and Co^{2+}_B , with the Co moments to decrease faster than those of the tetrahedral Fe ions, with the increase of surface coverage. The effect of the OA coverage on the mean magnetic moments of the octahedral Fe ions is slightly different. The rate of decrease is slower than the other metal ions and it increases above 20%. In addition, the MAE in the ground state of the system is calculated for several spin orientations, including spin–orbit coupling, by rotating all spins coherently along different directions. In **Table 1**, we show the change in the magnetic anisotropy energy (MAE) with the increase of OA molecules. We observe that MAE decreases slowly with the increase of OA surface coverage.

Table 1 DFT calculations of the total mean magnetic moment and for each metal ion and the corresponding magnetic anisotropy energy (MAE) with the increase of OA molecules coating.

Oleic Acid coverage (%)	Mean Moment(µв)	Fe ³⁺ _A (µ _B /atom)	Fe ³⁺ B (µB/atom)	Co ²⁺ B (µB/atom)	MAE (meV)
0.00	125.8	4.190	4.250	2.780	11.50
2.50	124.4	4.150	4.200	2.750	11.40
3.75	123.2	4.090	4.120	2.710	11.30
5.00	122.4	4.010	4.080	2.660	11.20
7.50	122.5	3.800	4.050	2.400	11.10
10.00	121.4	3.599	3.909	2.241	10.90
14.00	120.8	3.587	3.890	2.230	10.86
20.00	120.4	3.579	3.890	2.231	10.80
24.00	120.1	3.578	3.789	2.231	10.72
27.00	119.5	3.570	3.570	2.212	10.70

In order to calculate the magnetic exchange coupling constants, different magnetic configurations are mapped on a Heisenberg model with first-neighbor interactions. The mapped magnetic configurations are created by randomly flipping the magnetic moments of both sublattices starting from the ground state configuration of the system [10]. In this way we determine the mean exchange coupling constants between A–A, B–B and A–B ions for the uncoated nanoparticles ($J_{AA} = 13.759$ meV, $J_{BB} = 16.758$ meV and $J_{AB} = -22.62$ meV, respectively) and for the OA-coated nanoparticles ($J_{AA} = 10.72$ meV, $J_{BB} = 12.96$ meV and $J_{AB} = -17.28$ meV, respectively).

There is a decrease in the exchange coupling constants of the coated nanoparticles that can be attributed to the variation of the surface structure. Comparing these exchange coupling constants with their bulk values [60] shows a gradual decrease of the exchange coupling strength between B–B octahedral ions and between A–B sites, because of the surface modifications (lattice distortions and coordination number).

In the uncoated nanoparticle, the symmetry breaking at the surface of the $CoFe_2O_4$ nanoparticles due to the absence of some oxygen atoms results in the increase of the spin–orbit coupling, which is responsible for enhanced magneto-crystalline surface anisotropy [61,62]. The OA can be considered as effectively taking the position of these missing atoms. Indeed, as the metal cations at the surface of nanoparticles are coordinated with OA, the spin–orbit coupling and the magnetic moment become smaller as previously demonstrated [62]. The reduced spin–orbit coupling also leads to the decrease of the surface anisotropy affecting MAE (see **Table 1**).

The results of our DFT calculations for the magnetic moments, the exchange coupling constants and the anisotropies are used as input data in the atomic-scale modeling for the hysteresis

behavior of a nanoparticle and in the mesoscopic-scale modeling of the corresponding nanoparticle assemblies.

2.2 Atomic-scale simulations of a CoFe₂O₄ nanoparticle

The nanoparticle size of D = 2 nm in our DFT calculations is the maximum size, we could achieve, because of the computational cost (time and size) of these electronic structure calculations. Next, we model a spherical CoFe₂O₄ nanoparticle of 5 nm size and cubic inverse spinel structure with lattice constant 0.835 nm (as found in our DFT calculations). The 5 nm particle size is selected for comparison with previous experimental findings [10]. In **Fig. 2**, the model of the CoFe₂O₄ nanoparticle of cubic inverse spinel is shown. All the magnetic atoms are placed at the lattice sites and they are represented by classical spins **s**_i with $|\mathbf{s}_i| = 1$. Oxygen atoms are not shown in **Fig. 2**, however, their magnetic moments, though almost negligible, they have been already incorporated into our calculations. We consider a core/surface structure with a disordered surface layer of thickness equal to one lattice constant [63,64].



Fig. 2. Two-dimensional schematic representation of the simulated model of $CoFe_2O_4$ spherical nanoparticle of 5 nm size. The metal ions in the core and at the surface are shown.

The energy of the system (Eq. 1) includes the Heisenberg exchange interaction term between nearest neighbors in the core and at the surface (first and second term, respectively), the Zeeman energy (third term) and the anisotropy energy of the core (with cubic magneto-crystalline anisotropy) and at the surface (uniaxial with random orientation of the easy axis at each site i given by the random unit vector $\hat{\mathbf{e}}_i$) (fourth and fifth term, respectively).

$$\mathcal{E} = -\sum_{\langle i, j \in core \rangle}^{N} J_c \vec{s}_i \cdot \vec{s}_j - \sum_{\langle i, j \in srf \rangle}^{N} J_{srf} \vec{s}_i \cdot \vec{s}_j - \mu_0 \vec{H} \cdot \sum_{i=1}^{N} \vec{s}_i$$
$$-\sum_{i \in core}^{N} K_{i_core} \left(s_{x,i}^2 \cdot s_{y,i}^2 + s_{y,i}^2 \cdot s_{z,i}^2 + s_{z,i}^2 \cdot s_{x,i}^2 \right) - \sum_{i \in srf}^{N} K_{i_srf} \left(\vec{s}_i \cdot \hat{e}_i \right)^2$$
(1)

In equation (1) the core exchange coupling constant $J_{\rm C}$ is calculated from the bulk $J_{\rm AA}$, $J_{\rm BB}$ and $J_{\rm AB}$ of the A–A, B–B and A–B interactions [60], respectively. For the calculation of the core anisotropy constants for the Fe (K_{Fe_core}) and Co atoms (K_{Co_core}), we start from the bulk value for the cubic magnetocrystalline anisotropy of CoFe₂O₄, $K = 20 \times 10^4$ J m⁻³ [65]. The core of the particle contains 24 metal ions, therefore the calculation of the bulk anisotropy of the core gives K_{core} = 0.2976 meV. From there, we get K_{Co_core}=0.031 and K_{Fe_core}=0.0031, taking into account that K_{Co_core}= 10 × K_{Fe_core} [65].

For the surface parameters, the corresponding exchange coupling and anisotropy constants are taken from the DFT calculations, performed on the 2-nm particle, since for this nanoparticle size more than 90% of the magnetic atoms belong to the surface. As we showed in the Section 2.1, for coverage above 10%, the MAE and the total mean magnetic moment very little vary with the increase of the OA coverage. Therefore, for the surface anisotropy constants of the Fe (K_{Fe_stf}) and Co atoms (K_{Co_stf}), we use the anisotropy constants extracted from the DFT calculation of MAE for a CoFe₂O₄ particle with 106 metal ions. We calculate the corresponding K_{Fe_stf} and K_{Co_stf} values for all OA coverage cases, using the relation $K_{stf} = 70 \times K_{Fe_stf} + 36 \times K_{Co_stf} = 70 \times K_{Fe_stf}$. Along these lines, the anisotropy constants for the different OA

concentrations are listed in **Table 2**. All the energy terms in Eq. 1 are divided by the exchange coupling of a perfect antiferromagnet $J_{AFM} = 1.0$ meV to be dimensionless.

OA surface coverage (%)	K Fe	Ксо
0	0.0267	0.267
5	0.0260	0.260
10	0.0253	0.253
20	0.0251	0.251
27	0.0249	0.249
100	0.0230	0.230

Table 2. The anisotropy constants for the surface metal atoms.

2.3 Mesoscopic-scale simulations of an assembly of CoFe₂O₄ nanoparticles

In our previous studies [10,23–25,66–68], we developed a mesoscopic model to study the magnetic behavior of assemblies of nanoparticles with core/surface morphology. This model describes each nanoparticle with a classical spin (s_{1i}) for the core and two spins (s_{2i} , s_{3i}) for the two surface sublattices as previously described [10]. We consider magnetic interparticle interactions between the nanoparticles in the assembly. Our model is based on the reduction of the number of the simulated spins to the minimum adequate to describe the core/surface morphology for each nanoparticle. The effect induced by OA molecules bonded on the nanoparticle surface is included in the magnetic moment and the anisotropy values. We use this model to simulate an assembly of CoFe₂O₄ nanoparticles each of diameter D = 5 nm. In the case of the uncoated particles, we consider a dense assembly of 50% particle concentration and a particle concentration of 20% for the OA-coated nanoparticle assemblies because the particles are dispersed in larger distances due to the presence of the OA molecules on their surface. The particles are randomly located on the

nodes of a simple cubic lattice in a box of dimensions $10\alpha \times 10\alpha \times 10\alpha$, where α is the smallest interparticle distance and is equal to particle diameter, in order to avoid particles overlapping. The energy of the system is given by the following expression [69]:

$$\begin{split} \mathcal{E} &= -\sum_{i=1}^{N} \left\{ k_{C} \left(\hat{s}_{1,i} \cdot \hat{e}_{1,i} \right)^{2} + k_{srf} / 2 \left[\left(\hat{s}_{2,i} \cdot \hat{e}_{2,i} \right)^{2} + \left(\hat{s}_{3,i} \cdot \hat{e}_{3,i} \right)^{2} \right] \right\} \\ &- \sum_{i=1}^{N} \left[j_{c1} \left(\hat{s}_{1,i} \cdot \hat{s}_{2,i} \right) + j_{c2} \left(\hat{s}_{1,i} \cdot \hat{s}_{3,i} \right) + j_{surf} \left(\hat{s}_{2,i} \cdot \hat{s}_{3,i} \right) \right] \\ &- g \sum_{\substack{i,j=1\\i \neq j}}^{N} \left(m_{1,i} \hat{s}_{1,i} + m_{2,i} \hat{s}_{2,i} + m_{3,i} \hat{s}_{3,i} \right) D_{ij} \left(m_{1,j} \hat{s}_{1,j} + m_{2,j} \hat{s}_{2,j} + m_{3,j} \hat{s}_{3,j} \right) \\ &- \sum_{\substack{i,j=1\\i \neq j}}^{N} \left[j_{ex} \left(\hat{s}_{2,i} \cdot \hat{s}_{2,j} \right) + j_{ex} \left(\hat{s}_{3,i} \cdot \hat{s}_{3,j} \right) \right] - \mu_{0} h \sum_{i=1}^{N} \left(m_{1,i} \hat{s}_{1,i} + m_{2,i} \hat{s}_{2,i} + m_{3,i} \hat{s}_{3,i} \right) \cdot \hat{e}_{h} \end{split}$$
(2)

Each spin within a nanoparticle has a uniaxial easy anisotropy axis with a random orientation (first term) and interacts via Heisenberg exchange interaction with the other two spins inside the particle (second term). Thus, the short-range intraparticle exchange interactions between the core spin and each of the two surface spins (interface coupling j_{c1} and j_{c2}) and between the two surface spins (surface coupling j_{srf}) are introduced in our energy calculations together with interparticle dipolar interactions (third term) and interparticle exchange interactions (j_{ex}) between the nanoparticles in contact (fourth term). The last term gives the Zeemann energy. We calculate the normalized magnetic moments $m_1 = M_{\text{core}}V_1/M_sV$, $m_2 = M_{\text{srfA}}V_2/M_sV$ and $m_3 = M_{\text{srfB}}V_3/M_sV$. Here M_s and V are the saturation magnetization and the volume of each particle, and M_{core} , M_{surfA} and M_{surfB} and V_1 , V_2 and V_3 are the particle magnetizations and volumes of the core spins and the two sublattices of the surface spins, respectively, calculated from the atomic-scale model. In particular, the atomic scale model gives that the total number of spins is 2680 (514 Fe spins and 268 Co spins in the core and 618 Fe_A spins, 660 Fe_B spins and 620 Co_B spins at the surface) for a 5 nm Co ferrite nanoparticle and the volume ratios are: $V_{\text{core}} / V_{\text{tot}} = 0.3$, $V_{\text{A surf}} / V_{\text{tot}} = 0.2$, $V_{\text{B surf}} / V_{\text{tot}} = 0.5$. In **Table 3**, the calculated magnetizations for the two surface sublattices normalized to the total magnetic moment M_{tot} (for OA% = 0) are given. The core magnetization is calculated as $M_{core}/M_{tot} = 0.276$.

The D_{ij} is the dipolar tensor and $g = \mu_0 (M_s V)^2 / (4\pi d^3 K_C V_1)$ is the reduced dipolar strength, we set g = 0.30.

OA surface coverage (%)	M _{surfA} /M _{tot}	MsurfB/Mtot	
0	0.969	1.694	
5	0.927	1.624	
10	0.832	1.485	
20	0.828	1.478	
27	0.825	1.394	
100	0.825	1.394	

Table 3. The calculated magnetizations normalized to M_{tot} (for OA% = 0) of the mesoscopic model for the surface for the different percentage of OA coverage.

The anisotropy constants inside the different spin regions of the nanoparticle in the mesoscopic-scale model are calculated from our atomic scaling results, by properly rescaling them, to account for the size of the core and surface regions separately. In more detail, DFT calculations of MAE correspond to the volume of a nanoparticle of diameter of 2 nm, so for the surface volume of 5 nm particle, we take $K_{\rm srf}V_{\rm srf} = 11 \times \text{MAE}$, since $V_{\rm srf}$ (D=5nm) / $V_{\rm core}$ (d=2 nm) = 11. The volume of the core size $D_{\text{core}}=3.33$ nm (D=5 nm) is 33 times larger than the core of the particle of d=2 nm with corresponding $K_{\text{core}} = 0.2976 \text{ meV}$, thus the core volume anisotropy is $K_{\text{core}}V_{\text{core}} = 33 \times 0.2976$ meV = 10.02 meV. The calculated anisotropy constants for the surface volume anisotropy are 126.5, 123.2, 119.2, 118.8, 117.7 and 93.5 for 0%, 5%, 10%, 20%, 27% and 100% respectively. These constants are normalized to the core volume anisotropy $K_{\rm C}V_1$ so they are dimensionless [10], thus the core spin is $k_c = 1.0$. The anisotropy for each of the two surface spins is $k_{srf}/2$ and for the different OA surface coverage are shown in Table 4. The 100% surface coverage corresponds to a complete layer of OA of 2-nm thickness . The reduced intraparticle exchange coupling constants are calculated from the atomic-scale constants. The interparticle exchange coupling constant j_{ex} is taken as a free parameter and it reduces as the OA surface coverage increases, taking the values 7.8, 6.0, 3.0, 1.5, 0.75 and 0.0 for OA coverage of 0%, 5%, 10%, 20%, 27% and 100%, respectively. In **Table 4** the calculated mesoscopic parameters are summarized. The normalized external magnetic field is denoted by h and the normalized temperature by t.

Table 4. Calculated magnetic moments for the core (m_1) and the surface (m_2, m_3) , the anisotropy constants of the core (k_c) and the surface (k_{srf}) and the exchange coupling constants (j_{ex}) for particles in contact of the mesoscopic model for different percentage of OA coverage.

Oleic Acid coverage (%)	m 1	<i>m</i> ₂	<i>m</i> 3	k _c	k srf	j ex
0	0.083	0.194	0.847	1	12.63	7.8
5	0.083	0.185	0.812	1	12.30	6.0
10	0.083	0.166	0.742	1	11.97	3.0
20	0.083	0.166	0.739	1	11.86	1.5
27	0.083	0.165	0.697	1	11.75	0.75
100	0.083	0.165	0.697	1	10.85	0.75

The Monte Carlo simulation technique with the implementation of the Metropolis algorithm is used to calculate the low-temperature hysteresis loops for single MNPs and their assemblies after a field cooling procedure. For the dipolar energy calculation in the assembly, the Ewald summation technique [69] is implemented. The Monte Carlo simulation results for a given temperature and an applied field were averaged over 20 samples with various spin configurations, realization of the easy-axes distribution and different spatial configurations for the nanoparticles. For every field value, the first 5×10^2 steps per spin for the assemblies and 10^3 steps per spin for the single nanoparticle are used for equilibration, and the subsequent 7×10^3 and 10^4 Monte Carlo steps per spin in the assemblies and the single nanoparticle respectively are used to obtain thermal averages.

3. Results and discussion

To shed light on the effect of OA coating on the lattice structure of the nanoparticle, we focus first on the DFT results. We compare the calculated radial distribution function (rdf) of the metal

ion-oxygen bond, on the surface of the particle for the uncoated (0% OA) and for the 10% and 20% OA surface coverage case (**Fig. 3**). In the presence of OA, the distribution of the TM–O bond lengths, increases on average, indicating an expansion of oxygen coordination of the TM ions and results in the reduction of magnetization. DFT calculations also show that with the increase of the coordination of the OA-bonded Co and Fe surface ions, the lattice distortion of the Co and Fe ions positions at the nanoparticle's surface gradually reduces. Consequently, the anisotropy and the magnetization decrease as the OA coverage of the particle surface increases. This is also reflected in the change of the exchange coupling strength.



Fig. 3. Radial distribution function (rdf) of the TM–O pairs at the surface of the particle for uncoated (black line) and 10% (bleu) and 20% (red line) OA-coated nanoparticles. The rdf is calculated with a bin size of 0.05 Å.

Next we examine the effect of OA surface coverage on the magnetic behavior of a nanoparticle of size 5 nm, to compare with recent experiments [10], and for nanoparticles in an assembly, where interparticle interactions are present. We use Monte Carlo simulations with the implementation of the Metropolis algorithm [71] to calculate the hysteresis loop at low temperature. The 100%

surface coverage corresponds to the formation of a complete OA monolayer of 2 nm thickness. In **Fig. 4** we show the evolution of the coercive field as the OA surface coverage increases for uncoated and for six different OA coverages. The calculations for the 5 nm particle show that the surface behavior defines the magnetic behavior of the system (see **Inset Fig. 4**). This is expected since the surface spins dominate over the core (71% of the spins are lying on the surface). Consequently, the decrease of the surface anisotropy with the increase of the number of OA molecules is responsible for the observed decrease of the coercive field of the nanoparticle.



Fig. 4. Monte Carlo simulation results of the hysteresis loops of an assembly of $CoFe_2O_4$ nanoparticles with increasing number of organic molecules attached on their surface, after a field cooling procedure. Inset: The corresponding hysteresis loops of 5 nm Co ferrite nanoparticle. The coercive field Hc is also denoted for each case.

The results for the hysteresis loops of an assembly of nanoparticles for various percentages of OA surface coverage up to the full coverage (100% coating) show an increase of the coercive field with increased OA coverage (**Fig. 4**). This behavior is attributed to the decrease of the exchange coupling (decrease of touching) as the OA coverage at the surface of the nanoparticles increases. However, as coverage increases, the surface anisotropy of each nanoparticle in the assembly decreases and the role of the dipolar interparticle interactions becomes dominant. The dipolar interactions give an extra anisotropy in the assembly and result in the increase of the coercive field [24]. This behavior is in agreement with previous experimental findings [51] for exchange coupled dense assemblies of CoFe₂O₄ nanoparticles (~10 nm) in which the coercive field increases with increasing OA surface coverage from 20% to 80%. For the full coverage, the dipolar contribution becomes dominant and at the same time the anisotropy decreases by 20% (see **Table 2**) and the coercive field decreases. This behavior is in agreement with the experimental findings of a dense assembly of CoFe₂O₄ nanoparticles (~6 nm) in which the coercive field decreased as the OA surface coverage from 80% to 100% [50].

4. Conclusions

We study numerically, for the first time, using a multiscale modeling approach, the effect of OA surface coverage on the magnetic behavior of CoFe₂O₄ nanoparticles. Our model with the implementation of DFT calculations on uncoated CoFe₂O₄ nanoparticles reveals the surface effects induced by the strong lattice distortion of the surface metal ions. The introduction of the OA molecules bonding on the nanoparticle surface reduces this distortion and as the bonding increases, with the increase of the OA coverage, the coordination symmetry of the bulk material is gradually recovered. Furthermore, we perform Monte Carlo simulations in an atomic scale to investigate this

structural effect on the hysteresis behavior of a larger nanoparticle of 5 nm explicitly including nanoparticle core/surface morphology. The atomic-scale calculations of single CoFe₂O₄ nanoparticles further confirm that the increase in OA surface coverage recovers the bulk behavior, resulting in a decrease in the coercive field. Interestingly, our mesoscopic-scale modeling for an assembly of CoFe₂O₄ nanoparticles shows that the gradual increase of the OA surface coverage, that gradually reduces the exchange interparticle energy, results in an increase of the coercive field; only in the case of the full OA coverage, where exchange interparticle interactions are not present, is H_C reduced. Our results are in good agreement with available experimental data, paving the way for an optimization of the magnetic behavior of organic-coated MNPs for their use in energy, industrial and biomedical applications.

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Declaration of Competing Interest

The authors declare no competing financial interest.

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