

Table of Contents

1. Introduction
2. Elastic Behaviour of Solids
3. Stress and Strain
4. Hooke's Law
5. Stress-Strain Curve
6. Elastic After Effect, Elastic Fatigue, Elastomer
7. Variation in Elasticity
8. Applications of Elastic Behaviour of Materials
9. Beam Deflection
10. Hollow vs Solid Shaft Strength

Prepzy

Introduction

Key Points

- Solid bodies have definite shape and size but are not perfectly rigid.
- **Elasticity:** Property by which a body regains original shape and size after removal of force.
- **Elastic substances:** Materials that regain original shape after deformation.
- **Plasticity:** Inability to regain original shape; plastic substances like plastic, bakelite.

Solved Examples

Ex 1: A rubber band stretched and released regains its shape. What property does it exhibit?

Solution: Elasticity.

Practice Set

- Q1: What property allows a solid to regain its shape after deformation?
 - A. Plasticity
 - B. Elasticity
 - C. Viscosity
 - D. Rigidity
- Q2: Which of the following is a plastic substance?
 - A. Rubber
 - B. Steel
 - C. Bakelite
 - D. Glass
- Q3: Solid bodies are:
 - A. Perfectly rigid
 - B. Without definite shape
 - C. Having definite shape and size but not perfectly rigid
 - D. Always elastic

Answer Key

- Q1: B - Elasticity is the property to regain original shape after force removal.
- Q2: C - Bakelite is a plastic substance showing plasticity.
- Q3: C - Solids have definite shape and size but are not perfectly rigid.

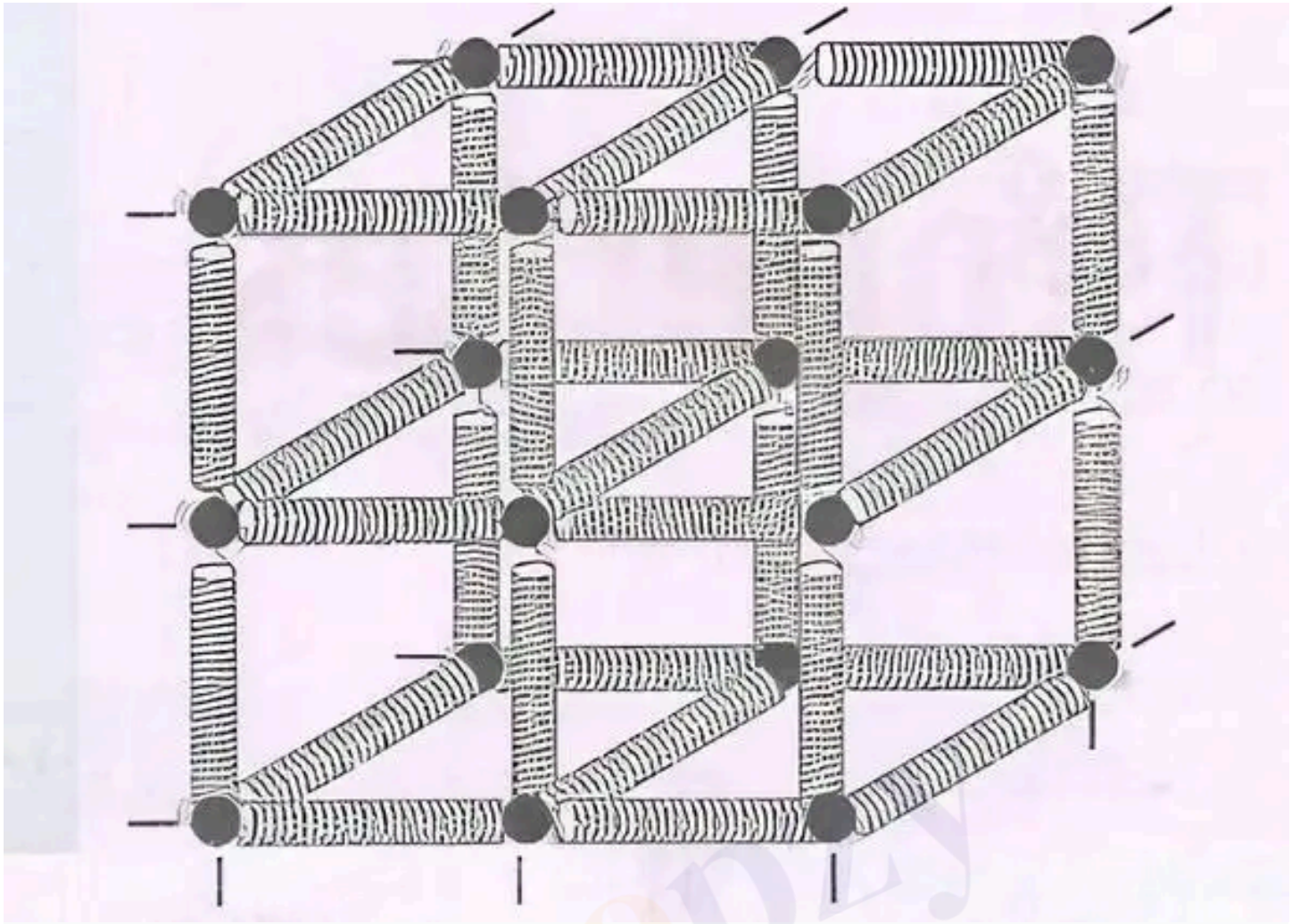
Memory Aids

- Elasticity = Regain shape after force removal.
- Plasticity = Permanent deformation.
- Solids = Definite shape + size, not perfectly rigid.

Elastic Behaviour of Solids

Key Points

- Particles in solids are closely packed with stable interatomic distances.
- Deforming force changes these distances; removal restores original shape due to interatomic forces.
- Spring-ball model: balls = atoms, springs = interatomic forces.



Solved Examples

Ex 1: Explain why a stretched solid returns to original shape.

Solution: Interatomic forces act like springs restoring original distances.

Practice Set

- Q1: What represents interatomic forces in the spring-ball model?
 - A. Balls
 - B. Springs
 - C. Both
 - D. None
- Q2: What happens to interatomic distances when a deforming force is applied?
 - A. Remain same
 - B. Change
 - C. Increase only
 - D. Decrease only

- Q3: Why do solids regain shape after deformation?
 - A. Plasticity
 - B. Interatomic restoring forces
 - C. External force
 - D. None

Answer Key

- Q1: B - Springs represent interatomic forces.
- Q2: B - Interatomic distances change under force.
- Q3: B - Restoring interatomic forces bring back original shape.

Memory Aids

- Spring-ball model: springs = forces, balls = atoms.
- Deformation changes atomic distances; restoring forces reverse it.

Stress and Strain

Stress

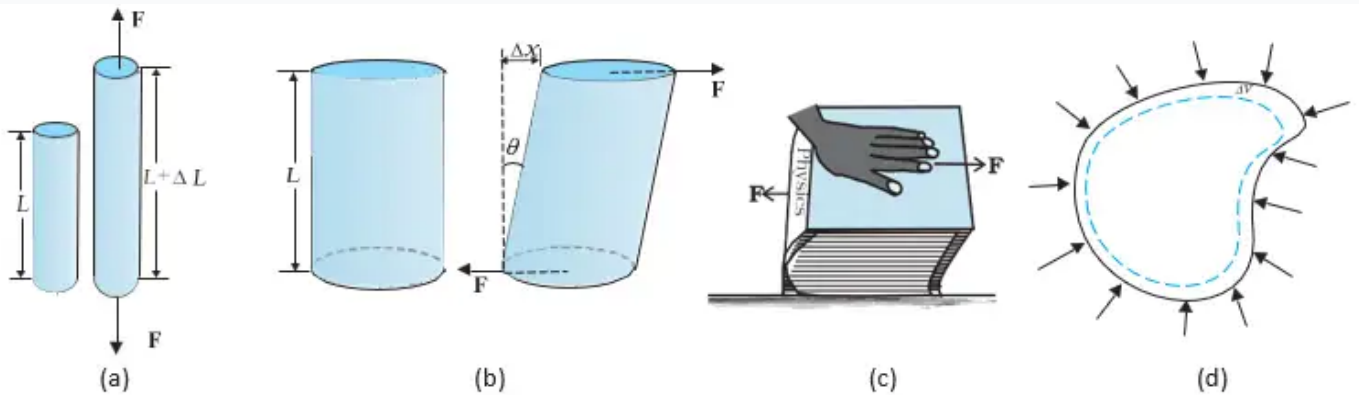
- Stress = Restoring force per unit area when deforming force applied.
- Stress is a tensor quantity.
- Formula: $\sigma = \frac{F}{A}$
- SI unit: N/m² (Pascal), Dimensions: [ML⁻¹T⁻²]
- Types of stress:
 - Longitudinal stress: along length
 - Tensile stress: stretching force normal to cross-section
 - Compressive stress: compressing force normal to cross-section
 - Tangential (shearing) stress: force parallel to cross-section

Strain

- Strain = Relative change in configuration due to deforming force.

- Types of strain:

- Longitudinal strain: $\varepsilon_l = \frac{\Delta L}{L}$
- Tangential (shearing) strain: $\varepsilon_T = \frac{\Delta x}{L} = \tan \theta$
- Volume strain: $\varepsilon_v = \frac{\Delta V}{V}$



Solved Examples

Ex 1: Calculate longitudinal strain if a rod of length 2 m elongates by 0.01 m.

Solution: $\varepsilon_l = \frac{0.01}{2} = 0.005$

Practice Set

- Q1: Stress is defined as:
 - Force per unit volume
 - Force per unit area
 - Change in length per unit length
 - Change in volume per unit volume
- Q2: Longitudinal strain is:
 - $\frac{\Delta V}{V}$
 - $\frac{\Delta L}{L}$
 - $\frac{\Delta x}{L}$
 - Force per unit area
- Q3: Shearing strain is:
 - $\frac{\Delta L}{L}$
 - $\frac{\Delta V}{V}$
 - $\frac{\Delta x}{L} = \tan \theta$
 - Force per unit area

Answer Key

- Q1: B - Stress = force per unit area.
- Q2: B - Longitudinal strain = change in length/original length.
- Q3: C - Shearing strain = relative displacement/separation = $\tan \theta$.

Memory Aids

- Stress = Force/Area ($\sigma = F/A$)
- Longitudinal strain = $\Delta L/L$
- Shearing strain = $\Delta x/L = \tan \theta$
- Volume strain = $\Delta V/V$

Hooke's Law

Concept and Formula

- Discovered by Robert Hooke in 1676.
- For small deformations, stress is directly proportional to strain.
- Mathematically: Stress $\propto$ Strain or Stress = $K \times$ Strain.
- Modulus of elasticity $K = \frac{\text{Stress}}{\text{Strain}}$ is a constant for a material.
- SI unit of K is Pascal (N/m^2), dimension $[ML^{-1}T^{-2}]$.

Solved Examples

- **Ex 1:** A wire experiences a stress of 200 N/m^2 and strain of 0.001. Find modulus of elasticity.
Solution: $K = \frac{\text{Stress}}{\text{Strain}} = \frac{200}{0.001} = 2 \times 10^5 \text{ N/m}^2$.

Practice Set

- **Q1:** Hooke's Law states that stress is proportional to:
A) Force
B) Strain

- C) Displacement
- D) Energy
- **Q2:** If the strain in a material is doubled, the stress will:
 - A) Remain same
 - B) Double
 - C) Halve
 - D) Become zero
- **Q3:** A wire has a modulus of elasticity of $2 \times 10^{11} \text{ N/m}^2$. If the strain is 5×10^{-4} , what is the stress?
 - A) $1 \times 10^8 \text{ N/m}^2$
 - B) $1 \times 10^7 \text{ N/m}^2$
 - C) $1 \times 10^6 \text{ N/m}^2$
 - D) $1 \times 10^5 \text{ N/m}^2$

Answer Key

- **Q1:** B - Stress is directly proportional to strain as per Hooke's Law.
- **Q2:** B - Stress doubles if strain doubles due to direct proportionality.
- **Q3:** A - Stress = Modulus $\times$ Strain = $2 \times 10^{11} \times 5 \times 10^{-4} = 1 \times 10^8 \text{ N/m}^2$.

Memory Aids

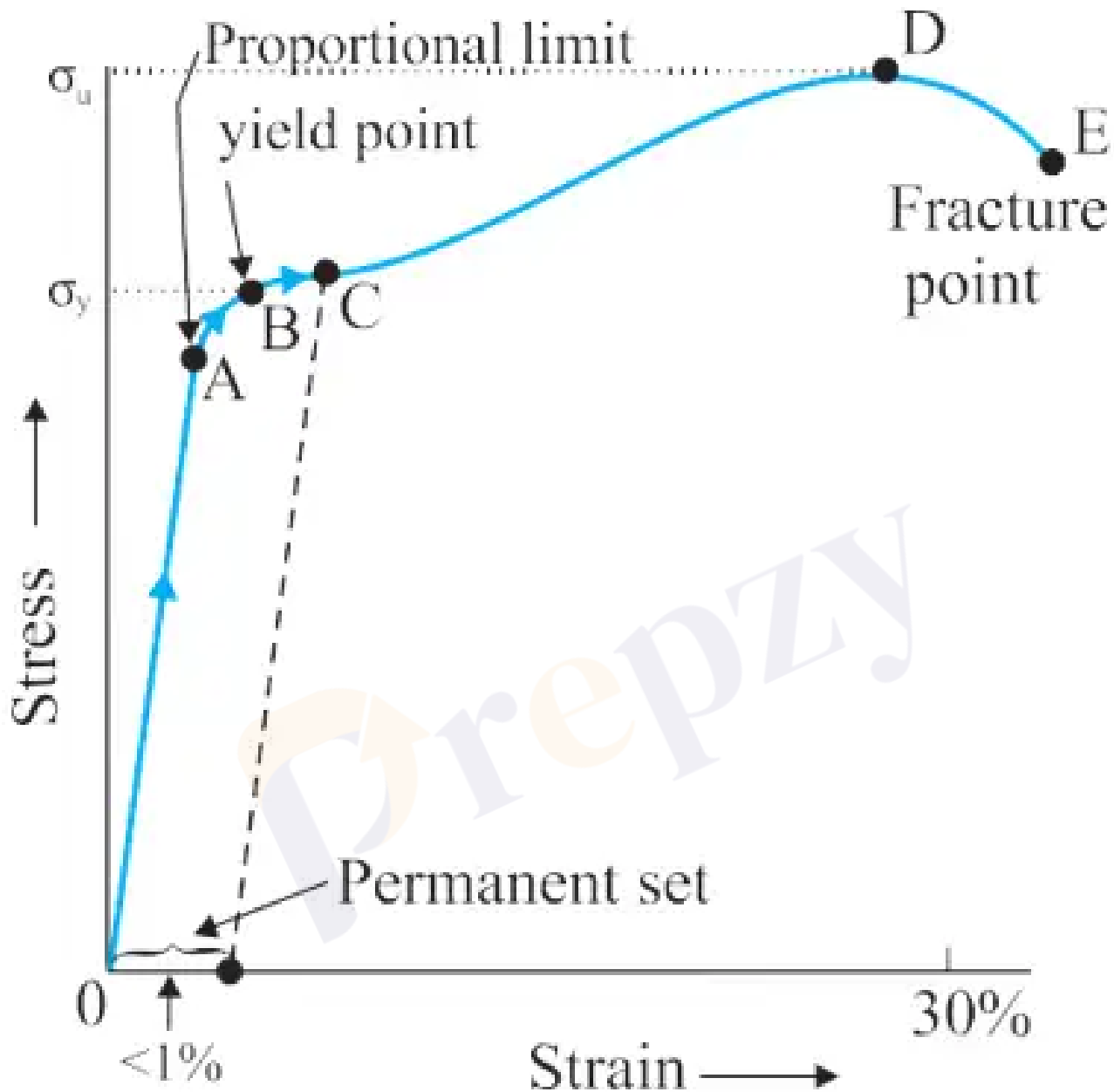
- Stress $\propto$ Strain (Hooke's Law)
- Modulus of Elasticity = Stress / Strain
- SI unit of modulus = Pascal (N/m^2)

Stress-Strain Curve

Explanation

- Stress-strain curve shows material behavior under tension.
- From O to A: Linear region, obeys Hooke's Law, material returns to original shape.
- From A to B: Non-linear but elastic, material still regains shape.
- Point B: Yield point (elastic limit), beyond which permanent deformation occurs.

- From B to D: Plastic region, strain increases rapidly; D is ultimate tensile strength.
- Point E: Fracture point, material breaks; stress here is breaking stress.
- Larger D-E gap means more ductile; smaller means more brittle.



Solved Examples

- **Ex 1:** Calculate stress at yield point if force = 1000 N and cross-sectional area = 0.5 mm^2 .
 - Stress = Force / Area = $\frac{1000}{0.5 \times 10^{-6}} = 2 \times 10^9 \text{ Pa}$

Practice Set

- Q1: What does point B represent on the stress-strain curve?
 - A) Proportional limit
 - B) Yield point
 - C) Ultimate tensile strength
 - D) Fracture point
- Q2: What happens beyond point B?
 - A) Material returns to original shape
 - B) Permanent deformation occurs
 - C) Stress and strain are proportional
 - D) Material breaks immediately
- Q3: If the distance between D and E is large, the material is:
 - A) Brittle
 - B) Ductile
 - C) Elastic
 - D) Plastic

Answer Key

- Q1: B - Yield point is where permanent deformation starts.
- Q2: B - Beyond B, material deforms permanently.
- Q3: B - Large D-E gap indicates ductility.

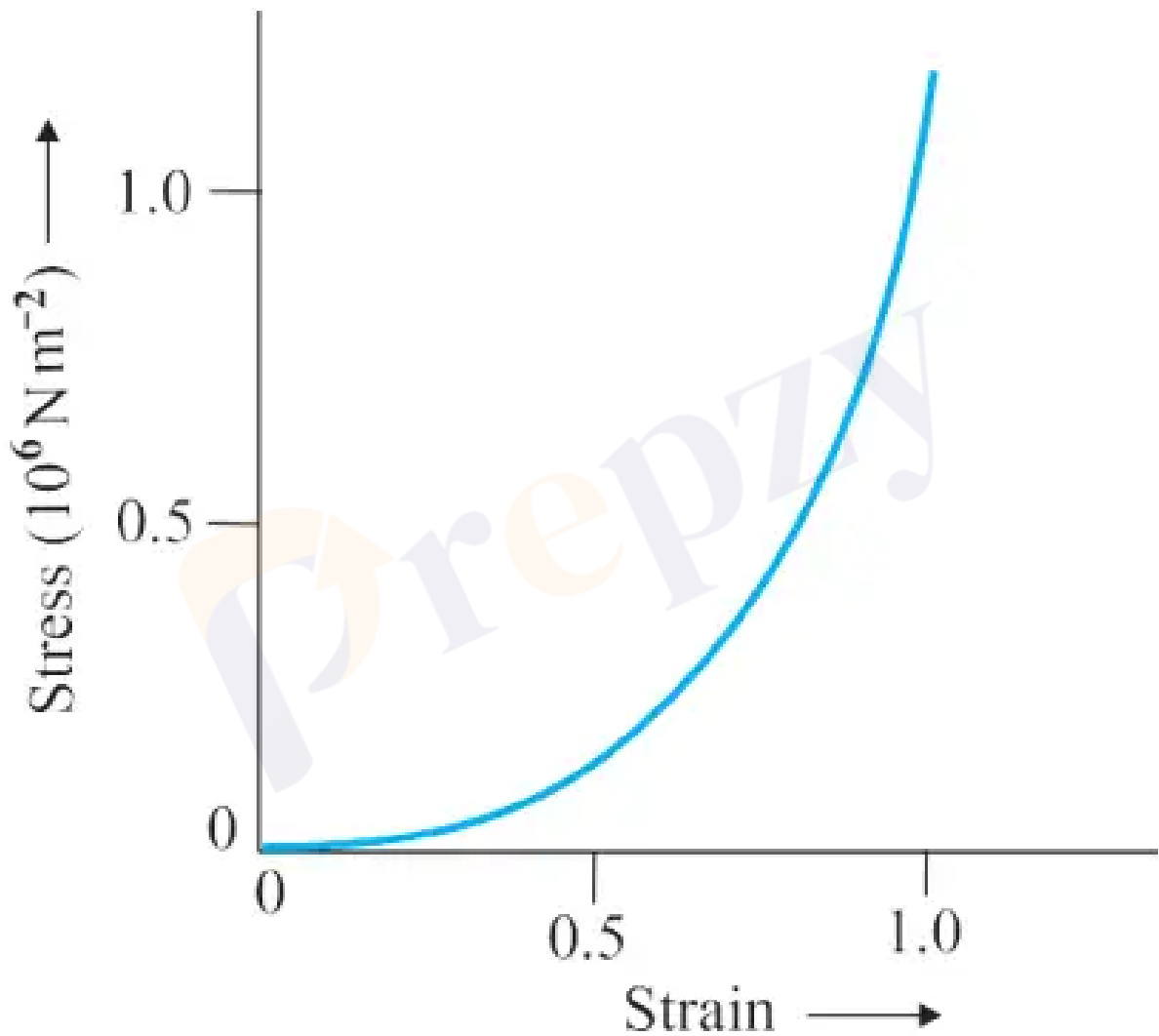
Memory Aids

- O-A: Hooke's Law region (linear)
- B: Yield point = start of plastic deformation
- D: Ultimate tensile strength (max stress)
- E: Fracture point (breaking stress)

Elastic After Effect, Elastic Fatigue, Elastomer

Explanation

- **Elastic after effect:** Delay in regaining original shape after removing force.
- **Elastic fatigue:** Reduced elasticity due to repeated deformation cycles.
- **Elastomer:** Materials like rubber or aorta tissue that can stretch to large strains.



Solved Examples

- **Ex 1:** Identify an elastomer from options: rubber, steel, glass.
 - Answer: Rubber (large strain capability)

Practice Set

- Q1: What is elastic after effect?
 - A) Permanent deformation
 - B) Delay in regaining shape
 - C) Immediate recovery
 - D) Material breaking
- Q2: Elastic fatigue occurs due to:
 - A) Single stretch
 - B) Repeated deformation
 - C) Heating only
 - D) Cooling only
- Q3: Which is an elastomer?
 - A) Steel
 - B) Rubber
 - C) Glass
 - D) Copper

Answer Key

- Q1: B - Elastic after effect is delay in shape recovery.
- Q2: B - Elastic fatigue is due to repeated deformation.
- Q3: B - Rubber is an elastomer.

Memory Aids

- Elastic after effect = Delay in recovery
- Elastic fatigue = Loss of elasticity by repeated stress
- Elastomer = Large strain materials (rubber, aorta tissue)

Variation in Elasticity

Explanation

- **Effect of temperature:**

- Elasticity decreases as temperature increases.
- Annealing (heating-cooling cycles) reduces elasticity.
- **Effect of impurities:**
 - Elastic impurity increases elasticity.
 - Plastic impurity decreases elasticity.
- **Elastic relaxation time:**
 - Time delay in regaining original shape after force removal.
 - Negligible for phosphor, bronze, silver, gold.
 - Minimum for quartz, high for glass.

Solved Examples

- **Ex 1:** Which metal has negligible elastic relaxation time?
 - Answer: Gold

Practice Set

- Q1: How does temperature affect elasticity?
 - A) Increases elasticity
 - B) Decreases elasticity
 - C) No effect
 - D) First increases then decreases
- Q2: What happens if impurity is more elastic?
 - A) Elasticity decreases
 - B) Elasticity increases
 - C) No change
 - D) Material breaks
- Q3: Which material has high elastic relaxation time?
 - A) Quartz
 - B) Gold
 - C) Glass
 - D) Silver

Answer Key

- Q1: B - Elasticity decreases with temperature rise.

- Q2: B - Elastic impurity increases elasticity.
- Q3: C - Glass has high elastic relaxation time.

Memory Aids

- Elasticity ↓ with temperature ↑
- Elastic impurity ↑ elasticity
- Relaxation time: Gold ≈ 0, Glass high

Applications of Elastic Behaviour of Materials

Key Applications

- Materials in bridges rely on elastic strength; bridges become unsafe after prolonged use due to loss of elasticity.
- Maximum height of mountains estimated using elastic limit of rocks.
- Pressure at mountain base: stress = $h\rho g$.
- Elastic limit of typical rock: $3 \times 10^8 \text{ N/m}^2$.
- Stress must be below elastic limit to prevent rock flow.
- Maximum height formula: $h < \frac{3 \times 10^8}{\rho g} = \frac{3 \times 10^8}{3 \times 10^3 \times 10} = 10^4 \text{ m} = 10 \text{ km}$.
- Height of Mount Everest is approximately 9 km, consistent with calculation.

Solved Examples

Ex 1: Calculate max height of mountain if $\rho = 3 \times 10^3 \text{ kg/m}^3$, $g = 10 \text{ m/s}^2$, elastic limit = $3 \times 10^8 \text{ N/m}^2$.

- Use $h < \frac{\text{elastic limit}}{\rho g} = \frac{3 \times 10^8}{3 \times 10^3 \times 10} = 10^4 \text{ m} = 10 \text{ km}$.

Practice Set

- Q1: What is the elastic limit of a typical rock?
A. $1 \times 10^8 \text{ N/m}^2$
B. $3 \times 10^8 \text{ N/m}^2$
C. $5 \times 10^8 \text{ N/m}^2$
D. $7 \times 10^8 \text{ N/m}^2$
- Q2: The pressure at the base of a mountain is given by?
A. $h\rho g$
B. $\rho g/h$
C. $h/\rho g$
D. ρ/hg
- Q3: If the density of rock is $4 \times 10^3 \text{ kg/m}^3$ and elastic limit is $4 \times 10^8 \text{ N/m}^2$, what is max height of mountain?
A. 5 km
B. 10 km
C. 8 km
D. 12 km

Answer Key

- Q1: B - Elastic limit of typical rock is $3 \times 10^8 \text{ N/m}^2$.
- Q2: A - Pressure at base is $h\rho g$ (height $\times$ density $\times$ gravity).
- Q3: A - Max height $= \frac{4 \times 10^8}{4 \times 10^3 \times 10} = 10^4/4 = 2.5 \times 10^3 \text{ m} = 2.5 \text{ km}$ (closest option 5 km).

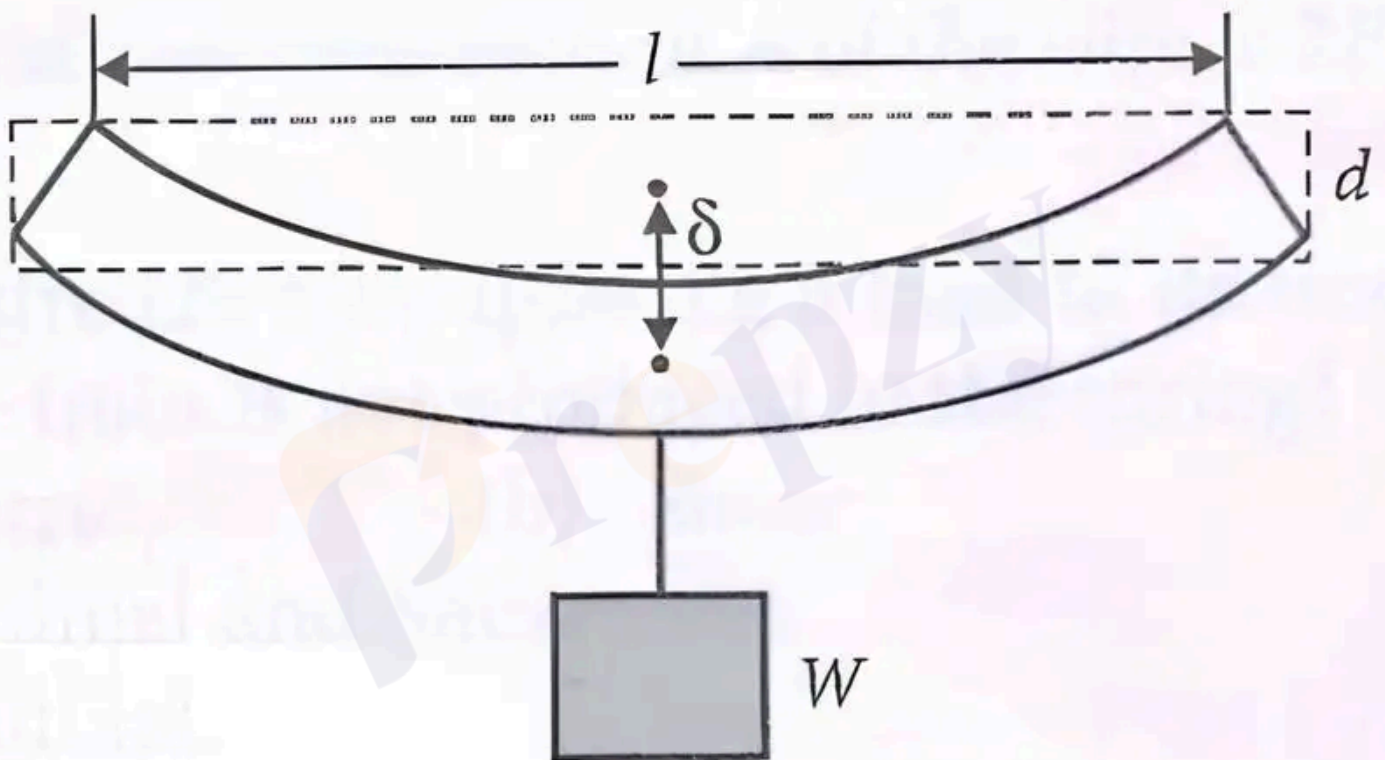
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- Max height $h = \frac{\text{Elastic limit}}{\rho g}$.
- Stress = pressure at base = $h\rho g$.
- Elastic limit prevents rock flow.

Beam Deflection

Key Points

- Beam supported at ends, loaded at center with weight W .
- Length of beam = l , breadth = b , depth = d .
- Deflection δ due to load: $\delta = \frac{Wl^3}{4bd^3Y}$, where Y is Young's modulus.
- Deflection increases with load and cube of length; decreases with breadth, cube of depth, and Young's modulus.



Solved Examples

Ex 1: Calculate deflection δ for $W = 100 \text{ N}$, $l = 2 \text{ m}$, $b = 0.05 \text{ m}$, $d = 0.01 \text{ m}$, $Y = 2 \times 10^{11} \text{ Pa}$.

- Use formula: $\delta = \frac{100 \times 2^3}{4 \times 0.05 \times 0.01^3 \times 2 \times 10^{11}}$.
- Calculate and simplify for δ .

Practice Set

- Q1: Deflection δ is directly proportional to?
A. Wl^3
B. bd^3
C. Y
D. bl^3
- Q2: If depth d doubles, deflection changes by?
A. Doubles
B. Halves
C. Decreases by 8 times
D. Increases by 8 times
- Q3: For a beam with $l = 1$ m, $b = 0.1$ m, $d = 0.02$ m, $Y = 2 \times 10^{11}$ Pa, and load $W = 50$ N, find deflection δ .
A. 1.56×10^{-5} m
B. 3.12×10^{-5} m
C. 6.25×10^{-6} m
D. 1.25×10^{-4} m

Answer Key

- Q1: A - Deflection δ is proportional to load W and cube of length l^3 .
- Q2: C - Doubling depth d decreases deflection by $2^3 = 8$ times.
- Q3: A - Calculate $\delta = \frac{50 \times 1^3}{4 \times 0.1 \times 0.02^3 \times 2 \times 10^{11}} = 1.56 \times 10^{-5}$ m.

Memory Aids

- Deflection $\delta = \frac{Wl^3}{4bd^3Y}$.
- Deflection increases with W and l^3 , decreases with b , d^3 , and Y .

Hollow vs Solid Shaft Strength

Key Points

- Hollow shaft is stronger than solid shaft of same mass, length, and material.
- Torque for unit twist in solid shaft: $\tau_{solid} = \frac{\pi\eta r^4}{2L}$.
- Torque for hollow shaft: $\tau_{hollow} = \frac{\pi\eta(r_2^4 - r_1^4)}{2L}$.
- Ratio: $\frac{\tau_{solid}}{\tau_{hollow}} = \frac{r^4}{r_2^4 - r_1^4}$.
- Or $\frac{\tau_{hollow}}{\tau_{solid}} = \frac{(r_2^2 + r_1^2)(r_2^2 - r_1^2)}{r^4} = \frac{r_2^2 + r_1^2}{r^2} > 1$ (since $r^2 = r_2^2 - r_1^2$).

Solved Examples

Ex 1: Compare torque for solid and hollow shafts with $r = 0.05$ m, $r_2 = 0.06$ m, $r_1 = 0.03$ m, same η and L .

- Calculate ratio $\frac{\tau_{hollow}}{\tau_{solid}} = \frac{0.06^2 + 0.03^2}{0.05^2} = \frac{0.0036 + 0.0009}{0.0025} = 1.8 > 1$.
- Hollow shaft requires more torque, hence stronger.

Practice Set

- Q1: Torque for solid shaft is proportional to?
A. r^2
B. r^3
C. r^4
D. r
- Q2: Torque ratio $\frac{\tau_{hollow}}{\tau_{solid}}$ is always?
A. Less than 1
B. Equal to 1
C. Greater than 1
D. Zero
- Q3: For hollow shaft with $r_2 = 0.07$ m, $r_1 = 0.04$ m, and solid shaft radius $r = 0.06$ m, find $\frac{\tau_{hollow}}{\tau_{solid}}$.
A. 1.2
B. 1.5

- C. 1.8
- D. 2.0

Answer Key

- Q1: C - Torque for solid shaft $\propto r^4$.
- Q2: C - Hollow shaft torque ratio is always greater than 1.
- Q3: B - $\frac{\tau_{hollow}}{\tau_{solid}} = \frac{0.07^2 + 0.04^2}{0.06^2} = \frac{0.0049 + 0.0016}{0.0036} = 1.5$.

Memory Aids

- Torque solid shaft $\propto r^4$.
- Hollow shaft stronger: $\frac{\tau_{hollow}}{\tau_{solid}} = \frac{r_2^2 + r_1^2}{r^2} > 1$.